431 M12



CORRELATION OF SOME PSYCHO-LOGICAL AND EDUCATIONAL MEASUREMENTS

WITH SPECIAL ATTENTION TO THE MEASUREMENT OF MENTAL ABILITY

BY

WILLIAM ANDERSON McCALL

SUBMITTED IN PARTIAL FULFILLMENT OF THE REQUIREMENTS
FOR THE DEGREE OF DOCTOR OF PHILOSOPHY, IN THE
FACULTY OF PHILOSOPHY, COLUMBIA UNIV. RSITY

PUBLISHED BY

Teachers College, Columbia University NEW YORK CITY

191



CORRELATION OF SOME PSYCHO-LOGICAL AND EDUCATIONAL MEASUREMENTS

WITH SPECIAL ATTENTION TO THE MEASUREMENT OF MENTAL ABILITY

BY
WILLIAM ANDERSON McCALL
"

SUBMITTED IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY, IN THE FACULTY OF PHILOSOPHY, COLUMBIA UNIVERSITY

PUBLISHED BY

Teachers College, Columbia University

NEW YORK CITY

1916

BF 431

Copyright, 1916, by WILLIAM ANDERSON McCALL

Columbia Conth. & Educ.

ACKNOWLEDGMENTS Aid in this study is but one of a hundred things for which I

am grateful to Professor E. L. Thorndike. Nor shall I forget the kindness of Professor H. A. Ruger. I also wish to thank Misses Genevieve L. Coy and Alma R. Huestis for much helpful assistance. It was by the courtesy of the New York State Commission on Ventilation that I could use the data for this study.

W. A. M.



CONTENTS

PAGE

CHAPTER

I.	PROBLEMS	1
ıI.	EXPERIMENTAL MATERIAL AND METHOD 1. Subjects. 2 Tests with Their Administration and Scoring.	3
III.	STATISTICAL TREATMENT OF RESULTS 1. Raw and Corrected Arrays. 2. Deviations and Their Combination. 3. Calculation of Raw Coefficients of Correlation. 4. Calculation of Corrected Coefficients of Correlation. 5. Reliability Coefficients.	10
IV.	CONSIDERATION OF PROBLEMS AND COMPARISON OF RESULTS WITH THOSE OF OTHER EXPEMIENTERS: 1. What Are the Intercorrelation among Some Recent Educational and Vocational Measurements and Certain Traditional Tests? 1. What Is the Order of Each Test's Correlation with Mennal Ability? 2. What Is the Practical Significance of These Tests for Educational and Vocational Disgnosis and Guidance? 3. What Is the Practical Significance of These Tests for Educational and Vocational Disgnosis and Guidance? 4. What Are Some Theoretical Considerations Growing out of This Study?	35
V.	Conclusion	67
VI.	Bibliography	69
VII.	APPENDIX	71



CORRELATION OF SOME PSYCHOLOGICAL AND EDUCATIONAL MEASUREMENTS

т

PROBLEMS

"The results of all good experimental work will live, but as yet most of them are like hicroglyphics awaiting their deciphering Rosetta Stone." These are the words of Spearman. Such words are true of all fields of research, but they are worse than true of the field of Correlational Psychology. The Rosetta Stone of Correlational Psychology must do more than interpret; it must reconcile. For this nothing less than a Philosopher's Stone will suffice, and Science, succeeding Black Magic, fully realizes that such a stone will not be found, but must be formed by a slow and laborious process. It is the hope that this study will contribute it is small part to the making.

Correlational Psychology is in this more or less chaotic condition, not only because of poor experimental technique and divergate and inadequate statistical methods, but also because of the very great complexity, importance, and number of the problems which it has elected to attack. Such complexity, importance, and number of problems is revealed by a very brief survey of the literature on correlation. But not to go farther afield, it is excellently illustrated by the problems which it is the purpose of this research to examine. These problems follow:

- 1. What are the intercorrelations among our psychological and educational tests or the functions which they measure?
- 2. What is the relative value of each test as a measure of mental ability?
- 3. In the practical measurement of mental ability for educational and vocational purposes which tests are the more valuable?

2 Correlation of Psychological and Educational Measurements

4. In the construction and in the application of psychological tests for the measurement of mental ability, do 'speed' tests or 'power' tests offer more promise, whether as to correlation, convenience, or time spent?

5. What characteristics in a test make for high correlation with mental ability?

6. What is the value of improvement as a measure of mental ability?

7. What is the significance of chronological age as an intellectual index?
8. Is there such a thing as a negative correlation between de-

sirable traits? Is the law of human nature correlation or compensation?

9. Do our results support Spearman's "Theorem of the Universal Unity of Intellective Function," or Burt's "Hierarchy of the Specific Intelligences"?

These problems have been attacked experimentally. The following pages describe the experiment, the use made of the data, and the results obtained. This experiment was devised originally to study problems other than those considered here. In fact, this study was not even conceived until the experiment was completed. While this means a certain roughness of technique, it has the advantage of guaranteeing the impartiality of the data.

EXPERIMENTAL MATERIAL AND METHOD

1. Subjects

The subjects for this experiment were eighty-eight public school children of an average age of about twelve and one-half years and about equally divided as to sex. These eighty-eight children were two typical 6B classes in a typical elementary school in New York City. The two class rooms adjoined and the teachers who had charge of the children used the departmental method of instruction. That is, the two teachers divided the subjects to be taught equally between them and each taught her allotted subjects to both classes. In this way both classes received exactly the same instruction. The classes were equal in mental ability as measured by what is later described as the six preliminary tests, though the last fact is not essential to this study. Further, it should be noted that while children were at the beginning shifted from one room to the other in order to make the classes equal in ability, in no case were children specially brought in from other classes. The eighty-eight children who made up the two classes were the children the experimenter found there when he began the experiment-they were typical classes.

2. TESTS WITH THEIR ADMINISTRATION AND SCORING

The general plan of the experiment was to give six preliminary tests, to follow these with an extended practice series, and to conclude with six final tests which were to be similar to, but not identical with, the six preliminary ones. Certain special tests were given along with the practice series without interrupting it.

In the administration of the tests every effort was made to treat both classes exactly alike. This was all the easier because a test in one room was followed immediately by the same test in the other room. Written instructions were used at the beginning of each new test to avoid unconscious variation. During the practice series each class was tested for about half an hour. The testing began in one room half an hour after lunch and was concluded in the other room half an hour after lunch and was concluded in the other room half an hour before the children were dismissed. The beginning class on one day would be the concluding class on the following day. A teacher was always present when the children were being tested, though she took no part in the administration of the tests. The entire experiment was conducted by the author with the exception of the six preliminary and six final tests. Each of these sets was given to both classes in one day. This required an assistant, but even here the writer started every test and left the assistant to collect the papers.

This experiment was throughout a group experiment, there being no individual testing. The detailed method for the practice series was as follows: The experimenter entered the class room and announced the names of the three pupils making the highest scores in each of the tests on the previous day. In addition to the regular procedure, if a new test were beginning, instructions were read and what was to be done was illustrated: Otherwise, the monitors distributed material face down. At the signal: Hands Up! all raised their hands. At the signal: Go! all began the test. At the signal: Stop! all ceased inumediately, wrotheir mames and identification numbers on the sheets and turned them over to the monitors, who did the collecting. This was repeated for the other tests of that day, after which the experimenter went through a similar procedure with the other class.

The tests used on any one day during the practice series, the number of days they were used, the dates they were used, together with the average score made by both classes in each test are all shown in Table A. A brief description of the tests employed, the time allowed for each, and the method of scoring are given below.

Preliminary and Final Tests

Visual Vocabulary: The children were given the Thorndike Reading Scale A, which contains forty-three words. The first five words are easy and equally difficult. Each succeeding group of five words grows progressively more difficult. The last group, consisting of only three words, is the most difficult of all. Thus both the lower and upper limits of the ability of the children were measured. The children were to write the letter F under every word that meant a flower, and the letter A under every word that meant an animal, and so on. In this as in all the preliminary and final tests the time allowance was thirty minutes. If a child completed a test, leaving nothing undone, before the expiration of the half-hour, he could hand his paper to the experimenter. This last rule held not only for all the preliminary and final tests but also for the special tests which were sprinkled along during the practice experiment. The Visual Vocabulary was secored in terms of penalties:

Score = Errors + Omissions.

The final Visual Vocabulary Test was similar to, though not identical with, the one just described. The two tests were administered and scored in exactly the same way.

Reading: Thorndike's Reading Seale Alpha was used. This scale contains four paragraphs, each one being more difficult to comprehend than the preceding. Each paragraph was followed by several questions. The child's written answers to these questions were taken as a measure of his comprehension of the paragraph. A complete sentence was not required of the child, one word sometimes being sufficient to express the idea. Time allowed: 3 on minutes.

Score == 2 (correct answers) + 1 (semi-correct answers).

The final Reading Test is similar. I, J, K and L of Thorndike's longer Reading Scale were used. The scoring was identical.

Completion: The Trabue Completion Test, consisting of twenty-eight mutilated sentences, was used. The difficulty of completing the first sentence is small, but there is a gradual increase in difficulty with each succeeding one. The child was to write in the missing word or words. Time allowed: 30 minutes. Score = 2 (sentences completed correctly) + I (sentences

Score = 2 (sentences completed correctly) + 1 (sentence completed semi-correctly).

A similar set of twenty-eight sentences was employed in the same way for the final test.

Arithmetic: Six problems in arithmetic, which grew progressively more difficult, were selected for this test. The child

handed in his work with his answers, but only the answers which were correct received a score

Score - Number of problems correctly solved.

Six similar problems were used for the final test.

Osmibus I. A: The Omnibus Test is so called because it represents a compilation by Professor Thorndike of several tests which psychology has found valuable. These are Easy and Hard Opposites, Verb-Object, Supraordinate, Mixed Relation, Easy and Hard Direction, and Addition. Time allowed: Thirty minutes. The method of scoring this as all the other Omnibus Tests varied with each special part, hence it would be tedious to give it. The method used was that devised by Professor Thorndike. Anyone who desires to use these tests is referred, for a copy of the method of scoring, to the Department of Educational Psychology. Teachers College.

The Final Test was Omnibus I B which includes the same tests as the one just described, the only difference being a slight variation of the tasks.

Omnibus II A: This tested reasoning ability, the ability to give the opposites to certain hard words, the ability to give a verb to a specified subject and to add the proper letters to unfinished words, and the ability to solve certain problems in arithmetic. Time allowed: Thirty minutes.

Omnibus II B or the Final Test is a slight variation of Omnibus II A.

Special Tests

Prosest: The Proverb Test was recently devised by Professor H. A. Ruger. It consists of thirteen English proverbs followed by their corresponding African proverbs. In some the similarity is easy to perceive; in others it is more difficult. The children were to match the proverbs. Time allowed: Fifteen minutes.

Score == Number correctly matched.

Other special tests were given from time to time but since these tests were not given twice they have not been used in this study. It is necessary that there be two measures of a function if a correlation is to be corrected for attenuation. The Ruger Provert Test has been retained just because it was recently devised.

Age: Because of its possible significance, the age of reaching

the grade has been used as a measure of the children. This age measure was taken from the official school record, and is expressed in months.

School Mark: This measure was an average of all the marks given by the two teachers to each child in each subject taught during the semester in which this experiment was being carried on. No previous marks have been used.

Teacher Rank: The two teachers were each asked to rank the eighty-eight children for mental ability. These ratings were made independently, although it must be remembered that the teachers had often talked together concerning the children.

Practice Tests

Cancellation of z's: For this the Woodworth-Wells Cancellation Sheet was used. This sheet contains a series of groups of five figures arranged in random order. The children were directed to cancel the figure 2. Time allowed: One minute.

Score = 2 (number cancelled correctly) - 2 (number omitted) - 3 (number wrongly marked).

Cancellation of 3's: Exactly the same test as the above, except that the children cancelled the figure 3.

Cancellation of A's: On the Cancellation A Sheet fifty capital letter A's were arranged at random among other letters of the alphabet of which there were fifty each. The children cancelled the letter A. The time allowed and the scoring were as in the Cancelling 2 Test.

Cancellation of S's: In every respect the same as the preceding test except that the letter S was cancelled.

Addition: The Addition sheet employed by Thorndike, Kirby, and others was used in this test. It is made up of columns of ten one-place numbers arranged in random order, no figure less than 2 being used. The children were to write the sum of each column of figures. Four similar sheets were rotated to prevent memorizing. Time allowed: Ten minutes

Score = Number of columns added correctly.

Copying Addresses: This test was recently devised by Professor Thorndike. A sheet containing twenty-five names arranged in alphabetical order was given to each child, together with the small directory from which the names were taken. The children

found in the directory the New York City address and wrote it beside the appropriate name. A different list of names was

used each day. Time allowed: Ten minutes. Score == Number of addresses correctly copied.

Handwriting: Similar paragraphs were cut from the Youth's Companion and pasted on cards. Each child was given a paragraph and a sheet of blank paper with directions to copy as much of the paragraph as he could while writing as well as he could. This test was given twice each day, a new paragraph being used each time. It need hardly be said that in this test as well as the others all the children did exactly the same thing in any one test. Time allowed: Four minutes for each test.

Score = 1 (number of lines or fraction of lines copied) minus 1-10 (each omission or error).

Each omission or error counted as one (1).

Any word or words omitted were of course deducted from

the gross number of lines covered to get the figure which was substituted in the first parenthesis above. Miscellaneous Arithmetic: The children worked for twenty minutes each day in Thorndike's booklet "Exercises in Arithmetic No. 5." Since this test has never been accurately scored

it was of little value for this study, consequently no further mention will be made of it.

TABLE A

Practice Series: Average score made by 88 individuals in the tests hown at the top on the days shown at the left.

5110 WII		p on the da		Can. A	Can. S	Cop.	Hand- writing
	Add.	Can. 2	Can. 3		Can. S	Add.	writing
2/4	32.1	70.1	88.7	26.6			
2/5	37.8	78.5	99.8	35.2			
2/8	37.8	85.2	102.7	38.8			
2/9	40.2	90.3	105.0	44-4			
2/10	41.6	92.7	105.5	47.4			
2/11	44-4	94.9	114.5	55-4	420		
2/15	43.0	97 3	116.0	54-4	49.0		
2/16	45.4	101.6	118.9	55.2	54.1		
2/17	47.9	108 2	123.3	59.3	58.6		
2/18	50.0	1104	126.9	62.5	63.6		-
2/19						11.0	7.38
2/23						13.4	6.82
2/24						14.8	6.52
2/25						17.8	7.20
2/26						18.5	7.06
3/1						18.0	6.96
3/2						170	6.61
3/3						18.4	6.62
3/4						18.6	6.41
3/5						22.2	6.84
3/6-4/	14 Misce	llaneous A	rithmetic	101	12	021	
4/14	46.1			61.3	64.4	21.6	
4/15	48.8			64.0	69.9	229	
4/16	51 4			70.8	72.6	21.8	
4/19	48 I			70.4	73.3	210	
4/20	50.3	106.9	1245			228	
4/21	53.I	110.8	128.3			23.4	
4/22	54.1	114.9	129.4			24.8	
4/23	56 3	122.6	136.0			25.8	
4/26	54.I	125.1	1387			27 5	
4/27	56.4	122.3	135.0			25.4	

ш

STATISTICAL TREATMENT OF RESULTS

I. RAW AND CORRECTED ARRAYS

The net original scores from the tests used in this study are given in the Appendix. In order that a coefficient of correlation might be calculated from these original data, it was necessary to reduce to one figure the many measures obtained from a practice test. No such reduction was necessary for the data obtained from the preliminary, final, and special tests, because each of these was given but once. Further, in order to get a true coefficient of correlation two measures of every function were necessary for each individual tested. This was simple in the case of the preliminary tests. The score made by each child in the preliminary test which was given February 3 was paired with the score made by the same child in the corresponding final test given April 28. The ability rank given by one teacher was paired with the rank of that same child given by the other teacher. School marks made in arithmetic, geography, and spelling were totaled and paired with the total of marks made in grammar, composition, and reading. Omnibus I A and Omnibus I B, being so much alike, were combined and paired with the sum of Omnibus II A and Omnibus II B. Of the other special measures-Ruger Proverb and the Age of Reaching the Grade-no second measure was available. In the case of the practice tests the scores made by any one child on days 1, 3, 5, etc., were added and averaged. With this was paired the number obtained from summing and averaging the scores made by that same child on days 2, 4, 6, etc. The practice test-Cancellation of S's-was given an odd number of days, so day I was omitted as being the one most likely to be unreliable.

An 'array' is simply a column of figures to be correlated with some other column which permits of pairing by individuals. These arrays may be measures of the same function or of different functions. The preceding paragraph describes the method used in constructing what may be called the 'raw arrays.' Obviously, many factors may enter to make it impracticable or impossible to calculate a coefficient of correlation from such arrays. In the case of a practice test, for example, an individual might be absent on the last few odd days. This would probably make the first member of the pair smaller than the second. Or. again, one or more individuals might be absent on a day when a preliminary, final, or special test was given. Since each of these tests was given but once, obviously the absent individuals would have no score at all in that function. Since it was desired that every test be correlated with every other test, the raw arrays were examined, and whenever any individual was found who lacked a score for any preliminary, final, or special test, that individual was entirely eliminated from this study. Whenever, in the case of the practice tests, any individual had been absent more than two odd days or two even days, that individual was also eliminated. The absences just mentioned refer, of course, to those days on which the particular test under consideration was given. Any other absence standard might have been employed. The more-than-two-days-absent standard seemed to be the one which would give the maximum accuracy of the scores with the maximum number of subjects.

But the pairing in arrays was still more refined in the practice tests. We may take Addition as an example of all of these. Suppose an individual were absent two days out of the ten odd days while he was present the ten even days. An average from the remaining eight odd days would be unduly decreased or increased as compared to the corresponding average from the ten days, according to whether the two absences were near the beginning or near the end of the practice. In order to overcome this difficulty, at least in part, the two scores which that individual would probably have made were padded in. Table A offers a means for determining this probability for any day in the practice. From Table A was calculated the average per cent of each day's increase or decrease with respect to the preceding day.

Using this per cent, the score which would probably have been made on the day when the individual was absent, was calculated from the last score made before or the first score made letter the absence. Table B gives the raw arrays for all the tests used for the entire eighty-eight subjects. By eliminating the individuals who were absent on single-test days and also those who were absent more than two odd or two even days for any one practice test, the eighty-eight subjects were reduced to sixty-three subjects. When the two or less absent days were filled in with the probable scores, Table C resulted. Let us call Table C the 'corrected arrays.'

In closing this discussion one further remark is necessary. The original intention was to use more special tests than are shown in Table B. While these were dropped later, they figured in the elimination of pupils. Still another fact must be noticed. The teachers, who gave their opinion of the children's mental ability, ranked them in order from one to eighty-eight. When many individuals were eliminated gaps occurred in their ranks. It was decided to close up these gaps and make the range from one to sixty-three.

TABLE B

RAW ARRAYS: Scores or average scores made by 88 children in the tests shown at the top of each column. Under the practice tests: Column I = average from odd days; column 2 = average from even days; figure to left of a parenthesis = total score from number of tests shown in the parenthesis.

Ind.	Addit	ion	Cancel	ling 2	Cancelling 3		
	10 tests	10 tests	8 tests	8 tests	8 tests	8 tests	
	1	2	1	2	1	2	
1 2 3 4	102.7 38.3 71.1 36.0	105.7 356.0[9] 71 9 38 7	138.0 92.3 98.8 87.3	142 0 696.0[7] 103.5 91.8	153.5 111.5 117.5 103.5	160.0 804.0[7] 119.5 106.1	
5 6 7	261.0[9] 348.0[9] 42.1	268.0[8] 356 0[9] 45.9	720.0[7] 580.0[7]	721.0[7] 92.0	120.8	897.0[7] 134.0[1] 110.3	
9	30.0 56.5	264 0[8] 58 5	80.3 132.0	54 2[6] 136.5	102.3 133.3	696 0[6] 135.8	
10 11 12	9.8 18 4 120.0[6]	12.0 16.5 125 0[6]	70.0 98 5 602.0[6]	74.0 111.8 692.0[6]	92.0 840.0[7] 814.0[6]	104 8 864.0[7] 814.0[6]	
13	91 3 71.4	94.9 76.4	130 3 113.8	138.9	157 5 121 8	162 5 120 5	
15 16 17	27.8 47.0 28.3	31.8 49.8 266.0F91	105.3 752.0[7] 96.0	106.0 115 0 728 0[7]	138.0 125.8 115.5	132.0 878.0[7]	
18 19	61.4 80.7	64 6 84.7	87.5 93.5	96 5 94.0	103.8 101.5	822.0[7] 105 5 748 0[7]	
20 21 22	57.6 23.5 268.0[9]	63.3 26.5 315.0[9]	95 5 111.8 682 0[7]	106.3 114.3 650.0[7]	123.5 120.5 744.0[7]	124.9 125.3 747.0[7]	

Ind.	Addition		Cance	lling 2	Cancelling 2 8 texts 8 texts 1 2 114 8 125 (77) 900.0(5) 900.0(5) 900.0(5) 900.0(5) 900.0(5) 900.0(5) 900.0(5) 900.0(5) 900.0(5) 900.0(5) 111.0 900.0(5) 112.0 900.		
	10 tests	10 tests	8 tests	8 tests	8 tests	8 tests	
	1	2	1	2	1	2	
23	54 3	54.9	100.0	107 3	114 8	124.5	
24	50.8	612.0[9]	105 5	102 9	122.0	860.0[7]	
25 28	228.0[5]	270 0[5]	524.0[5]	492 0[5]	595.0[5]	626 0[5]	
27	57.4	50 4	100 8	91 8	99.8	106.3	
28	191 0191	23 0	97.5	103.8	117.0	116.3	
29	36.2	36.5	124.0	112.9	133.0	128 3	
30	527 0[9]	56.4	530 0[7]	76.8	654 0[7]	92.5	
31	14 5	14 7	82.3	93 8	101.5	105 3	
32	42.5	44 1	760 0[7]	111.8	122 8	125.3	
34	140 0021	100 0021	210.0121	222 0	214 0503	139.8	
35	40.2	40.8	76.5	86.8	914 0[9]	101.8	
38	24.9	223 0191	93 3	710 0171	107.4	826 0[7]	
37	64.6	70 4	100.8	110 4	806.0[7]	842.0[7]	
38	20.6	201 0[9]	82 8	813	97.5	100.3	
39 40	52 7	58 2	88 8	90 3	111.3	112 0	
41	25.5	27 8	00 0513	95.0	07.0[1]	201,0[2]	
42	634 0197	592 0(81	674.0171	618,0[6]	803 0171	704 0063	
43	70.8	75 0	94.5	98.8	113.3	113.0	
44	33.1	33.7	122 3	120 8	132 0	135,5	
50	39.2	41.6	134 3	143 3	1024.0[7]	150 8	
51	86.8	82 9	422 017	36.0	62.0	79 8	
53	1910 029	280 0183	1910 088	128 0[6]	192.0061	178 0181	
54	50.6	53 7	150 5	145 5	145.3	1079 0171	
54 55	37 1	40 0	93.8	96.5	116 0	121 3	
56	207 0E8]	221 0[9]	794 0[7]	810 0[6]	832.0[6]	902 0[6]	
57 58	21.9	211 0[9]	58.3	548 0[7]	89,3	918	
59	49.0	45.9	82.0	84.0	116 2	121 4	
60	23 0	25.3	87.5	90.3	99.3	650.0123	
61	27 0	257,0[9]	94.3	105 5	103,9	101 3	
62	89.2	948	115 0	119.5	129 3	132 9	
83	31.6	28.2	98 5	108 3	125.5	129 3	
64 65	284 0[9]	283 0[9]	89 8	610 0[7]	704 8	740 0171	
66	57.2	59 8	87.0	33 3	108.0	108 5	
67	48.0	51 9	127 5	133.8	145.3	149 3	
68	501 0[9]	445 0[8]	478 8[6]	494.0[8]	564 0[8]	602 0[6]	
69	66.0[2]	[0]	170 0[2]	170 0[2]	275 0[3]	204 0[2]	
70	29 9	30.9	78 5	85 3	692 0[7]	106.5	
71 72	97.0	900	103.3	105 8	115.0	191 3	
73	40.6	43.7	118.9	125.5	129 0	126.5	
74	22 7	24 6	93 3	97 8	735.0[7]	107 0	
75	29 3	27 3	142 8	139 5	141 8	148 5	
76 77	50 5	55.8	112.8	126.3	128.3	136 3	
78	40.6	42.0	120 3	01.5	102.8	111 0	
79	708 0191	80.8	752 0[7]	114.1	900.0071	129.3	
80	93 8	.99 4	722 0[7]	736 0[7]	106.3	117.0	
81	65 6	66.6	111 5	120 3	132 0	132 3	
82	44 9	429 0[9]	113.1	732 0[6]	132.5	980 0[7]	
83 84	277.018]	283 0[6]	565 0[6]	246 0101	con of al	813 0101	
85	151 0157	204 0[6]	272 0[4]	354 0051	378 0[4]	404 0141	
86	19.9	19 3	162 0	101 8	118.0	118 5	
87	29 4	303.0[9]	108 0	110.8	130.5	139 8	
88	26 7	27 9	82.8	90 3	87.8	97 8	
89	264.0[4]	197 0[3]	350 0[4]	298 0[3]	454 0[4]	332 0[3]	
90 91	55.0	249 0707	101.0	704 0177	100 6	050 0177	
92	45.4	416.0[0]	89.0	91.3	109.5	111.8	
93	423 0[9]	439,0[9]	572 0[7]	484 0[6]	708 0[7]	804 0[7]	
	100		10.00	500		15000	

14 Correlation of Psychological and Educational Measurements

Ind.	Cancelli	TA		continued)		11
ing.			Cancelli		Copying Ac	10 tests
	7 tests		4 tests	4 tests	10 tests	2
1	1 54.6	85.7	65.5	2	1 19.6	18.3
2	42 0		52.0	73.5	19.6 22.5	230 0[9]
3	47.3			46.0		18.2
2 3 4 5 6 7	50.9	54.1	63.0	82.6	14 7 22 1 11.8	16.6
8	253,0[6]	270 0[8]	210 0[3] -5.0	226.0[3] 86.0[3]	22 1	188 0[8] 117.0[9]
7	43 7	56 6		35,0	13.5	15 8
8	45.1	54 1 270 0[5] 275 0[6] 56 6 277.0[5] 444 0[6]	57.3 78 0	60 0	23.5	25.4 23.0
9 10	404 0[5]	444 0[6]	78 0	77.0	21 0 14.9	16.5
11	39 4 51 9	46.0 338.0[6] 342.0[5] 70.0	51 0 49 5 126 0[2] 61.0	55 3 148 0[3]	21.4 58 0[5]	245 0[9]
12	303.0151	342 0[5]	126 0[2]	164.0[21	58 0[5]	89.0[6] 28 4
13 14	69.1 58.0	70.0	61.0 75.3	86.0 80.5	25 8 17.1	17.6
15	88 1	58.9 87.7	85.5	83 0 70.8		19.3
16	57.1	58 1	65.3	70.8	19 0	20 1
17	29 4 53.7	35 1 56.6	34 5 59.0	44 5	16 6	157 0[9] 25 2
19	49.4	51 9		52.5	17 4	19.4
20	46.6	46.6	71.8	77.5	22 1	22 8
21	56 0 298,0161	58 0 46.3	71.8 77.5 84.0	77.5	17.4 19.0 16.6 22.3 17.4 22.1 13.8 18.5	14.6 160 0[9]
21 22 23 21	54.0	51.4	56 0	70.8 44.5 62.5 52.5 77.5 77.5 78.3 68.5	17.4	187 0191
21	70 6	432.0161	93.5	284 0[3] 146.0[2]	28.3	246.0[9]
25	259 0[5]	304 0[5] 65,1	128 0[2] 75 5	75.5	91 0[5]	96.0[5]
28 27	376.0[8] 60.6	65.3	73 0	64.5	98.9	22 4 29.3 18.5
28	250.0161	44 6	160 0[3]	61 5 58.0 74.5	146.0[9] 26 6 25 5	18.5
29	59 7 258 0[6]	324 0[6]	73 5 58 5	74.5	26 6	28.9 25.7
30 31	38 6	37.7 232.0[6] 52 4 71 7	80.5	64 0 62.5 66 5		16 5 23 5
32	49.4	52 4		66.5	23 1 16 8	
33	72 9 132 0[3]	71 7 151 0[3]	71.5 57.0 (8) 18.5 83.0 52.0 77.5 (9) 132.0(3) 145.0(2) 63.5 68.5	60.5 62.0 [0] 59.5 108.0[3] 87.0 56.5 81.0	16 8	15.3 [0] 23.2 158.0[9]
34 35	46.9	41 4	55 0	59 5	20.8	23.2
36	36 9	40 6	18 5	108 0[3]	17 0 21.1	158.0[9]
37	80 6 41 7	90 9 38 6	82 0 52 0	56.5	15.6	21.7 16.0
39		46.0	77.5	81.0	15.6 18.5 [0] 18.9 29.7	20.2
40	0113	46 0 36 0[2]	[0]	[0]	[0]	188
41	50 3 318.0[6]	50 6 358.0[5]	145 0[3]	228.0[3]	29.7	28.1
43	58.3	68 3 73 4	63 5	64 5 67 0		16.8
44	58 3 75 4	73 4	68 5	67 0 86 D	148.0[8]	182 0[9] 249.0[9] 23 3 142 0[9]
50 51	55 4 45.1	65 4 55 4	70.8	157 9131	25 3 21.8	23 3
52	21.1		42.0 178 0[3]	157 0[3] 44 0		142 0[9] 210.0[9]
53	280 0[6]	316 0[6] 73.0	178 0[3] 49.0	200 0[3] 55 5 49 5	178.0[8]	210.0[9]
54	55 9 34.9	44.9		49.5	22 6 16 2	23 1 19.1 203 0(9)
54 55 56	256,0[6]	58.3	80.5 52.5 68.5 72.0	\$2.0 59.5 69.3	184 0[9]	203 0[9] 18,0
57	44 6 65.3	46 3 70.9	52 5 ee b	60.2	17 4 21,5	23.0
58 59	29.7	44.9	72.0	76.0	18.1	18 8
60	42.3 48.9	43.7	48.5 66.0	53 0	19 1 14 4	19.1
61	48 9 58.0	334.0[6]	69.8	204.0[3] 76.0		24.4
63	64.6	60 3 62 0	65.5	68.5	17.3	24.4 16.2
64	267.0161	49.7 47.7	170 0[3] 43.5	62 0 59.0	204.0[9] 113.0[9]	204,0[9] 88.0[7]
65	44.3 85.1	42.0	68.0	71.0	15 0	
67	48 7		60.5		18.5	19.9
68	206.0[5]	210 0[5]	156 0[3] 26 0[1]	174.0[3]	175.0[9]	21 8
70	100.0[3] 50 9	210 0[5] 84 0[2] 54 9	49.5	174.0[3] [0] 53.5 68.5	[0] 19.9	22.4
71 72	58.1		66.0	68.5	164.0[9] 20.5	19.9 22 6
	51 7 53.7	53.7 58.3	53 0 73 0	60.0 212 0[3]	20.5	15.9
74	43.1	48.9	68 0		14.1 17.8	18.8
74 75 76	76 3 50.3	87 3 55,7	89.3 64.5	91 5 70.0	18.8 29 8	20.5 29.9
77	57.4	56.9	71.0	77.0	22.7	23.5
78	41.4	43.7	45 0	54.5	19.5	20.7

	,	Statistica	1 1764	ment of	1/6211112		
Ind	Cancelli 7 tests	7 tests	Cance 4 tests	4 tests	10 tests	g Addresses 10 tests 2	
79 80 81 82 83 84 85 86 87 88 89 90 91 92 93	1 -31.1 52.1 79.1 68.9 228.0[5] 55.6 6[1] 58.6 45.1 41.7 186.0[4] 7.2 3 324.0[6] 43.1 65.6	2 -28.6 54.4 83 1 432.0[6] 268 0[5] 66 0 156.0[3] 59.4 239 0[6] 42 9 168 0[3] 83 1 322 0[5] 278 0[6] 69 7	1 26 0 62.5 68.5 44 5 184 0[2] 52.5 32 0[1] 58.0 58.0 51.5 60 0[1] 86.0 252 0[3] 184.0[3]	2 27 0 61 0 69.5 178.0[3] 164 0[2] 78.5 200.0[3] 67 5 194 0[3] 59.0 94.0 284.0[3] 184 0[3]	1 178.0[9] 21.9 30.5 22.0 202.0[9] 19.9 102.0[7] 16 i 17.5 13 6 21 9 178.0[9] 22 2 171.0[8]	187.0[5 23 0 32.5 24.7 206 0[7 22.6 1 130 0[16 3] 187.0[5 15 3] 187.0[5 15 3] [1 24 7 194.0[5 207.0[5	90 71 90 91
Ind.		dwriting 10 tes		Visual Vecabular		Completion	
	10 tests	2	ts	1	2	1	2
1 2 3 4 6 6 7 7 8 9 9 10 11 12 12 14 15 16 17 18 19 19 12 12 12 12 12 12 12 12 12 12 12 12 12	6.387 7.70144 6.647 7.70144 6.647 7.70144 6.647	6 40 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	[8] [8] [8] [8] [8]	1 12 14 22 20 17 23 20 11 12 18 14 16 10 11 11 11 11 11 11 11 11 11 11 11 11	* 115113007577211416200 = 922001331491151 11512217322 15775151 179223161315771 22243	· 的是我们是不是我们就是我们们是我们的,我们就是我们的我们就是我们的我们就是我们就是我们就是我们就是我们就是我们就是我们就是我们的,我们们们们的,我们们们们们们们们们们们们们们们们们们们们们们们们	177732344152665255555337333253133319 — 2244556653333333 — 2333 —

16 Correlation of Psychological and Educational Measurements TABLE B (continued)

Ind.	Handw	riting		Visual		
	10 tests	10 tests		ocabulary		pletion
	1	2	1	2	1	2
61	5.16	5.07	15	26	29 33	28 37
62	7.33	7 62 5.78	12 18	15 29	30	30
64	5 43 7.03	6 92	6	100	39	
65 66	7.89	63.00[8]	7	28	19	22
67	7 12 7 87	7.30 8.32	16 19	24 30	27 25	22 28 25
68	7.72	8 56	9	13	43	
69	6 99	[0]	35	57	25	27
70 71 72 73	5.58	7 13 6 19	22 18	28	25 29 31 38	30 32
72	5.58 7 10	8.91	14	23 22 33	38	32
73	7.05 6.08	7.08 6.88	14 15 16	33 23	22	20 25 20 33
74 75 76	8 21	8 06	24	25	22	20
76	9 41	8.93	14	24	30 32 30 29 35 28 42 38 37 36 31 34 25	33
77	7.15 5.60	7.35 5.45	15 14	24 21	35	35
79 80	6.52	6.60	15	33	28	23
80 81	8 14	7.85 9.60	11 12	17 20	42	42
82	9 47	7,47	17	30	35	33
83	7,41 53 70[8]	60 80181	9	22	36	28
84 85	6.29 36 10[6]	6,52 37,30[6]	11	21 24	31	35 23 42 37 33 28 33 30 28 33 32 28
88	6 90	7.04	16	18	25	28
87	6 17	6.48	2(31	19	33
88 89	5.63	5 91	14 20	25	29	28
90	7.23	7.47	21	19	29 33 22	30
91	7.35	7 39	22 12	3 20	28 34	-
92 93	8.42 60.10[8]	7 39 8 41 7.32	15	2 16 5 23	31	36 23
Ind.	Arithm	etic	Rea	ding	Omnib	
		200	Part		A 1	B
61	1	2	1	2		410
1 2	1	5	21 30	36	41.0 20 0	19.0
2345578	1 4 2 4 1 2 5	555221224522463413222442344	23	24 36 28 27 31 12	42 5	39.5
4	2	2	23 27 24 17	27	43 0 30.0	46.0 30.0
6	1	î	17	12	66 0	64.0 43.5
7	2	2	19		43.0	43.5 22.5
8	5	4	29	28 16	29.5 32 0	39.5
10	2	2	22	31	37 5	43.0
11	4	4	31	31 37 43 26 23 28 32 32 32 32 33 31	32.0	43.0 47.5 28.0
12 13	4	3	27 18	43	30 0	41.0
14	3	4	21 28	23	32,0 46 0 32.0 39 0	43.0
15 16	3 1 5	1	28 31	28	32.0	31.5 42.0
17	ő	2	29	28		44.0
18	3 3 2	2	28 26	32	27 5 35 5 20 5	26 0
	2	å	21	28	35.5	35.0 34.5
21	Ĩ 5	2	26	31	54.0	44.0
22	5	3	28	31 37	34 0 25 0	40 0 33.0
24	2	i	29	34	31.5	27.0
20 21 22 23 24 25 26	2	man.	29	25	31.5	-
27	4 2 2 2 4	5	32	43	30.0 7.5	39.0 19.5
28	ī	3	25	27 35	39.5	
29	4 3	5 3 4 3	23	35 31	50.0	42 0 25 5
31	4	3 2	27	28	25 5 44.0	29.5
32	1 2	2	24 29 29 24 32 25 23 26 27 25 27 26	39 28	17.5 42.5	29.0
33	2		28	40	25.0	33 0

Ind.	Arith	metic	Readin	ø	Omi	nibus 1
			1		A	B
35 36	5 5 1	2 2 2 3	31	46	10.5	16.0
37	1	8	20	21 26	51.0 28.5	44.0 25.5
38	5	4	25	37	42.5	30.5
40	5 4 0	4	25 27 25 25 26 20 25	33	27.0 36.0	33.5
41 42	5	4	25	41	15 5 18 0	4.5
43	4	3	26	40	18 0 32.0	30.0
44	4 4 2 8 3	3	26 28 24 22 28	38	33.0	30.0
50	2 2	1 5	22	22	34 0 28.0	35 0 13.5
51 52 53	ä	43431	27	22 35 32	42.0	30 0
53	2	4	23	31 19	38 0 43.0	34.5
54 55 56	4	å	27 23 21 28 23	37	28.5 31.0	37.0 36.5
56 57	4 2 4 3 2 5	-	23 30	77	31.0	
58	3	3 3 2 4 4 3	24	41 30	30 0 51 5 22 5	33.0 27 5 35.0
59 60	2	3	26 20		22.5	35.0
61	1	4	76	28 28 39	40.5 55.5	35 0 25.0
62	3	4	25	39	55.5 28.5	19.5
63 64	1 3 1 3	3	25 25 30	25	59 5 9.0	44.0
65	3	2 3 3 4	24	20	69.0	8 0 53.0
66 67 68	3 1 1 5	3	24 25 24 28	40 26	26.0 31.5	34 0 35.5
68	5	4	28	-	18.5 50 0	17 0
69 70 71 72	2 4 2 6	-	27 23	22	50 0 30 0	_
71	2	3 4 6		33 34 34 22 31	28.0 17 0	25.5 30 0
72	6	6	25	34	17 0 39.5	24.5
74	5	5	27	31	35.0	44 0 26 5
73 74 75 76	2542244553025113	4534251533845355	25 27 23 22 21 23 25 25 28 27 21 27 29	33	48 0 37.0 36 0	
77 78	2	2	21	-	37.0 36.0	34 0 26 0 30 5
78	4	5	23	35	28.5 59 0 28.5 23 0	30 5
79 80	8	5	20	15	59 0	64.0
81	5	3	28	45	23 0	18.0 13.5
82 83 84	0	3	21	28 32 32	29 5 28.0	17.0 41 0
84	2	4	27	32	34.5	24 5 27.0
85 88	5	5	29	43	27.0	27.0 23.0
87	î	5	25	33 35	34.5 38.5	30.0 23.0
88 89	3 5		25 29 24	37	37.5 34.0	23.0
90	1	4	9	27	38.0 35.5	39 5
91 92	3	4 2 4 5	28 23	50	35.5 25.5	45 0 31.0
93	3	5	26	38 27	36.5	38.5
Ind.	AOmn	ibus II	Proverb		her Rank	Age in months
	89.5	B 2 78.0	2	54	2 53 28	155
123459786	45.0	45.5	4	54 39 29 72 25 88	28	155 153
3	71.0 82.0	73.5 63.0	4 3 2 10 3 2 6 2 1	29	41 71 80	145 153
5	63.0	63.0 52.5 82.0	10	25	80	155
9	94.0 69.5	82.0 65.5	3		88 80	172 156
ž	20 0	60.0	6	16	14	137
6	69.5 64.5 75.0	62.0	2	16 33 42	20 38	151 163
10 11	75.0	68 5 51 0	4	37	54 44	153
12 13		51 0		44	44	173
13	82.0 82.0	76.0 85.0	4 6 3 5	82	49 84	136 148
15	82.0	73.5	3	41		134
14 15 18 17	91 0 79.0	66.5 59.5		37 44 50 82 41 70 64 13	81 69	166 159
18 19	53 0	59 5 48.5	3 3	18	29	137
19	65.5	70.5	8	76	68	165

Correlation of Psychological and Educational Measurements TABLE B (continued) Omnibus II Teacher Rank Age in months Proverb Ind. A 1 2 80.0 3 1 5 4 3 11 3 7 2 3 4 2 11 6 5 2 11 631671811188247068679625778843766112323315593348840785631683285527712733345975615513525752356774747179 21 618260 778 184231455760 4712522 1833 228499155408858138 9 455543440912751748234455760 4712522856 228489155408858138 9 455543440912751748241979115747221856 2575688774733 54 0 78.0 49.5 49.5 79.0 34.5 76.0 81.0 42.0 78.0 68.0 22.0 57.5 63.0 54.0 65.0 51 0 39.0 40 0 74.0 31 5 60.0 44.5 76.0 5.5 60 1.5 29.0 72 0 147 457534 | 15414035523 | 543 | 529543482 | 721284157 | 4394 51.0 70 0 44 5 64 0 55 0 77.0 63.5 146 140 150 147 163 153 32.0 65 0 73.0 75.5 72 0 43.0 61.5 34.5 89.0 60 0 72.0 39.0 65.0 61.5 62.5 62.5 67.0 64.5 86.0 38.0 63.5 63.5 65.0 63.5 65.0 61.5 68.0 73.0 73.0 65.0 64.0 94.0 73.5 62.0 64.0

83.5

TABLE C

Corrected Arrays: Scores or average scores made by 63 children in the tests shown at the top of the column. Under the practice tests: Column I = average score from odd days; column 2 = average score from even days. The number of days is shown at the top. B = boy; G = girl.

TABLE C (continued)

	C	111mm A	Cone	Copying Cancelling S Addresses				Handwriting	
	7	7	4	4	10	10	10	10	
Ind.	tests	tests	tests	tests	tests	tests		tests	
	1	2	1	2	1	2	1	2	
1B.	54.6 42.0	65.7	65.5 52.0	73 5 60 0	19 6 22.5	18 3 24 9	6.4 7.3	7.3	
2B. 3B.	47.3	50 3	43.3	46,0	16 3	18.2	7.6	7.0	
4G.	50.9	54 1	63.0	65.5	14 7	16.6	6.0	6.2	
7G.	43.7	56 6	40 0	35 0	13.5	15 8	6.7	6.8	
9B.	71.9 39 4	77 3	78.0	77 0 55 3	21.0	23.0	7.6	7.2 5.7	
10B.	51.9	46.0 56.2	51.0 49.5	50 1	21.4	16.5	5.6	5 6	
11B. 13B.	69 1	70.0	61.0	66.0	25.8	28 4	9.4	9.2	
14B.	58 0	58 9	75.3	80.5	17.1	17 6	6.5	6.6	
15G.	88.1	87.7	85 5	83 0	17 4	19.3	47	45	
16B.	57.1 53.7	58 1 56 6	65.3 59.0	70 S 62 5	19 0 22 3	20 1 25 2	7 2 6 2	69	
18G. 19G.	49.4	51 9	60 0	52 5	17.4	19 4	6.5	64	
20G.	46.6	48 6	71.8	77.5	23 1	22 8	6.8	6 4	
21G	56 0	58 0	77.5	77 5	13 8	14 6	60	66	
23B.	54 0 70 6	51 4 74 7	56 0 93 5	66.5 97.8	17 4 26 3	19 7 20 6	6.4	6.0	
24G. 28G.	59.2	65 1	75.5	75.5	20 5	22 4	5.9	60	
27G.	60 6	68 3	72.0	64.5	28.9	29.3	7.9	80	
28G.	43.6	14.6	53.6	58 0	16 4	18 5	7.0	7.1	
29B.	59 7 39 7	58 7 37 7	73.5 58 5	74 5 64 0	26 6 25 5	28 9 25.7	73	7.3 5.4	
30B.	38 6	40 2	60.5	62.5	17 3	16.5	50	59	
32B.	49 4	52 4	71.5	66.5	23.1	23 5	8 4	8.7	
35B	40 9	41 4	55.0	59 5	20.8	23 2	7.0	87	
37G.	80 6 41 7	90.9 38.6	82 0 52 0	87 0 56 5	21.1 15 6	21 7 16 0	7 0	6.8	
38B 39G.	41 7	46.0	77.5	81.0	18 5	20 2	6.4	61	
41B	50.3	50 6	43.3	51.5	18 9	16.8	7.5	71	
42B.	55.0	60.0	51.3	61 5	29 7	28 I 27 3 23 3	79	68	
50G 51G	55 1 45 4	65 1 55 4	76,8 39.8	86 0 52 9	25 3 21 H	27 3	67	8 2 6 7 5 5	
51G	31 1	33 1	42 0	44 0	14 7	14 4	54	5.5	
54G	55.9	73 0	49.0	55.5	22.6	23 1	54	76	
5518	34 9	44.9	51 5	49 5	16 2	19.1	58	6.4	
57(;.	41 6 65 3	16 3 70 9	52 5 68 5	59 5 69 3	17 1 21 5	18 0 23 0	53	50	
58B 59B	39 7	44.9	72 0	76 0	18 1	18 8	7.3	67	
6013.	42 3	43 7	48.5	53.0	19 1	19.1	68	6.7	
61B	48 9	55 4	66.0	69 5	14 4	15.7	52	5.1	
62B	59.0	60 3	65 5	76 0 66 5	23 5 17 3	24 4 16 2	54	. 0	
66B	35.1	42 0	68.0	71 0	15.0	16.7	7.1	7.3	
67B	43 7	45.0	60.5	61.8	18.5	19 9	7.1	58 73 83	
700	50.0	54.9	49.5	53 5	19 9	22 4	70	7.1	
7118	54 1	56.7	68 0 53 0	68 5 60 0	21 3 20 5	19 9 23 6	56	71 62 69	
72B 73R	93 7	53 7	73 0	73 7	11 1	10 9	71	7.1	
746.	13.1	48.9	68.0	68 0	17 9	18.8	6.1	6.9	
750	78 3	87.3	89 3	91 5	15 8	20 5 20 9	82	5 1	
7013.	50 1	35 7 13 7	64.5	70 0 54 5	29 8 19 5	29.9	9 1 5 0	55	
7#B 80B	52.1	51 1	62 5	61.0	21.9	20 7 23 0	51	79	
h25 .	Ex 11	733	11 5	56 1	22 0	24.7	7.4	7.5	
836	10-1	52.7	713	77 4	21 0	11.3	6.8	- 5	
SIG	58 11	66.0	62.5	78 5	10 1	20 6	63	6.5	
800 C	35.0	59 4	66 0 58 0	67.3	12.5	18 6	62	6.5	
6761 6015	11 7	12.9	51.5	500	156	111	5 6	5.9	
160.75	123	5.1	96.0	24 0	21.0	210	5 6	7.5	
91.13	1 1 1	16.3	54 9	617	21.2	23 1	7.5	7 3	
513 13	65.6	69.7	61.0	65.0	19.4	199	67	8.8	
Av	50 12 1	50 7	0.3.0	201.0					

	010			7 6 6617	10672	· Uj	116.	mond
In	d. Voca	isual	Com	aletion		ith.	D	ding
	1	2	1	2	1	2	1	2
1 2 3 4 7 9 10 11 13 14 5 6 8 9 12 12 13 12 14 15 15 19 10 11 13 14 15 15 19 10 12 12 12 12 12 12 12 12 12 12 12 12 12	124 222 224 1 1 1 1 1 1 1 1 1 2 2 2 2 1 1 1 1	213 212 22 22 23 24 24 24 25 25 25 24 24 25 25 25 25 25 25 25 25 25 25 25 25 25	9899981789977289998675598843818817999988878244322339778938239238878244323397789838239239887887898438	177 223 24 24 25 25 277 22 25 25 25 25 25 25 25 25 25 25 25 25 2	1442252443155321422414341515454233244325131114252542453021131432	55522524841324424445848823344453154348882445333464554553345554458	231 237 1192 237 1192 233 1121 253 253 254 255 255 255 255 255 255 255 255 255	248 227 16 6 13 13 22 22 22 23 23 24 24 25 23 24 24 25 25 24 27 25 25 25 25 25 25 25 25 25 25 25 25 25

TABLE C (continued)

Ind.		Omi	nibus	Pro- verb	Age in M'nths	T'ch'	Rank	Scho	ol Mark
		1	2			1	2	1	2
1	12	0.5	119 0	2	155	42	41	46	48
2		50	64.5	4	153	20	23	55	58
3		3.5	113.0	3	145	22	32	55	51
4	12	5.0	109 0	2	153	53	54	43	41
7	11	2.5	109 0	2	156	60	58	41	45
9		1.5	103 0	2	151	25	15	61	51
10	10	20	105.0	1	163	32	27	61	49
11	10	7.0	116.0	- 4	153	28	42	49	56
13	11	40	117 0	4	136	38	37	56	56
14	12	80	128 0	6	148	61	62	38	31
15		4.0	105 0	3	134	31	38	59	61
16		0.0	108.5	5	166	52	59	28	47
18		0.5	74.5	3	137	9	24	68	71
19		1.0	105 5	3	165	57	52	46	4.3
21		85	93 0 108 5	1	144	49	49 48	57	66
23	10	9.0	75.0	5	145	20	13	67	63
24	10	9.5	74.0	4	143	7	9	76	72
26		9.0	107.0	3	182	58	60	48	41
27		20	41.5	11	139	1	3	74	68
28		5.5	81.5	2	155	62	56	42	52
29		10	105.0	3	154	15	21	59	52
30	6	7.5	79.5	2	150	25	30	57	54
31	12	20	91.5	3	152	35	31	50	46
32		6.5	88.5	4	162	43	47	41	55
35	4	95	56.0	11	165	3	4	LS.	72
37	9	90	57 0	6	161	23	22	58	58
38	11	80	90 5	5	142	40	26	60	54
39	8	7.5	78 0	2	130	13	28	57	61
41		45	43.5	11	134	2	1	76	76
42	- 37	0.0	102 0	4	147	17	18	62	57
50	- 11	0.5	105 0	5	146	47	43	55	65
51		55	58 0	3	110	11	7	74	69
52	16	90	910	4	150	27	25	85	€5
54		3 5	114 6	1	163	63	63	36	41
55	3	4.5	100 0 65 0	5	153	16	31	47	16
5S		20	92.5	4	147	29	41	59	66
59	10	8.5	108.0	10	160	34	29	7.2	65
60		20	110.5	3	166	50	51	51	50
61	14	5.0	97.0	5	137	23	29	57	51
62		85	62.5	5	162	10	5	62	73
63	13	7.5	105.5	2	156	51	61	50	51
66		9.0	910	5	154	32	10	62	57
67	11	73	107.5	4	155	55	97	13	50
20		6.5	91.5	5	133	19	33	19	66
71		0.0	91.5	2	110	37	46	58	56
72	7	0.0	67 0	9	151	11	6	69	69
73	- 11	85	111 5	5	180	59	45	41	39
71	11	10	89 0	4	142	8	11	€5	53
75	13	10	104 0	3	138	15	38	51	50
76	11	75	107.5	4	151	36	1.6	58	58
78		90	95 0	2	140	16	17	67	70
80	7	0.0	52 0 72 5	.7	112	5	2	73	27
82		90	4.4 3	11	132	4	N	73	76
83		65	142 5	2	155	51	53	39	53
84	11	40	88 0 88 0	8	113	11	50	16	66
36			91.5	1 5	145	12	15		63
87		15		7	137		19	65	70
88	10	25	91 0 123 0	4	111	28	20	63	68
92	15	20	89.5	9	159		12	61	57
93	10	0.5	103.0	3	131	18	11	35	10
Av		3 8	93 1	4.4	150 3	32	32	56-1	57 1
27.6	- 10	o it	- M.L	9.9	100.0	0.0	100	Seed 1	44.1

4. DEVIATIONS AND THEIR COMBINATION

The next step in calculating the coefficients of correlation was to turn all the scores in any one column of Table C into plus and minus deviations from the average shown at the foot of that column. These deviations are given in Table D. At the foot of each column is the square root of the sum of the deviations squared, which we shall find to be useful later. Further it will be remembered that Visual Vocabulary and the Omnibus tests were scored in terms of penalties, and what amounts to the same thing, a small measure by Teacher Rank means large excellence. To make these tests comparable to the others all their plus deviations were changed to minus and all their minus deviations to plus.

The reader will notice that two new tests appear in this deviation table. For reasons to be considered later it was found desirable to combine Visual Vocabulary with Completion. Column I of this new measure is the algebraic sum by individuals of the deviations of Visual Vocabulary (1) and Completion (2); Column 2 is the sum of Visual Vocabulary (2) and Completion (1). The second of these tests or measures is a Composite. Column 1 of this Composite is an algebraic total by individuals of all the column I's of all the tests shown in Table E. Column 2 of the Composite is the same thing for all the column 2's. But contrary to the Visual Vocabulary and Completion combination, not all the tests in Table E received equal weight. The weight actually given to each half of each test is shown under "Weight given," in Table E. These weights were guesses, guided by what experimental evidence was then available, as to the relative value of each test as a measure of mental ability. Now the desired weighting was obtained by multiplying or dividing the deviations in any one column by the figure under "Multiple" in Table E. These figures were those which, when divided or multiplied into the square root of the sum of the deviations squared divided by ten, changed these square roots to the relative sizes shown under "Weight given" in Table E. In psychological literature such a Composite is usually taken as a measure of general mental ability. ¹ This weight was given before our own coefficients were calculated.

24 Correlation of Psychological and Educational Measurements

TABLE D

DEVIATIONS FROM THE AVERAGE OF EACH TEST

Ind.	Add	dition 2	Canc	elling 2	Canc	elling 3	Canc	elling A
1 2 2 3 4 7 9 9 10 11 11 11 11 11 11 11 11 11 11 11 11	55.0 - 9.8 in 1.0 in 1.	58.6 1 10.5 1 10	58 2 2 - 7.0 2 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	37.0 - 6.04 - 6.	37 0 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	40.2 - 1.0 -	2004-0-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-	

Ind.	Cance	Cancelling S		Copying Addresses		Handwriting	
	1	2	1	2	1	2	
1941							
1	3.0	8.5	- 0,2	- 1.6	- 0.3	- 04	
2 3	-10 5	- 5.0	- 3.7 - 3.5	50	0.6	05	
3	-19.2	-19 0	- 35	- 1.7	0.9	0.2	
4	0.5	0.5	- 5.1	- 3.3	- 0.7	- 0.6	
7	-22 5	-30.0	- 63	- 4.1	0.0	0.0	
9	15.5	12.0	- 63 - 12 - 4.9	31	09	0.4	
10	-11 5	- 9.7	- 4.9	- 34	- 1.2	11	
11	-13 0	-14.9	1.6	63	- 08	-1.2	
13	-13 0 - 1.5	1.0	6.0	8.5	2.7	-1.2 -0.2 -23 -0.1	
14	12.8	15.0	- 2.7	- 23	- 02	- 0.2	
15	23 0	18.0	- 2.4	- 06	- 2.0	- 23	
18	2.8	5.8	- 0.8	0.2 5 3	0.5	0.1	
18	- 35	- 3.5	2.5	5.3	- 05	- 0.5	
19	- 25 93	-12.5	- 2 4 2 3	- 0.5	- 02	- 0.4	
20	9.3	12.5	9.3	2.8	0.1	- D 4	
21	15 0	12.5	- 6.0	- 53	- 07	- 0.2	
23	- 6.5	1.5	2.4	0.2	- 0.3	0.2	
24	31 0	32 8	- 2 4 6.5	10.7	- 0.4	- 0.0	
28	13 0	10.5	0.0	- 0 2 10 7 2 5	- 0.4	- 08	
97	0.5	- 05	9 7 9 1	2.5 9.4	- 00	0.0	
27 28	9 5 — 8 9	- 70	0.1	- 14	- 08 12 03	1.4	
29	110	95	- 3 4 6.8	9.0	0.6	0.3	
30	- 40	-10	5.7	5.8	0.6	0.8 0.8 0.8 1.2 0.3 0.5 1.4	
31	- 20	- 25	3.1		= 1 8 = 1 7	1.4	
	- 20 90 - 75	- 25 15 - 55	- 2 6 3 3 1.0	- 34	- 17	- 0.9	
32	8.0	1.5	3 3	3.6	17 03	19	
33	- 75	- 55	1.0	3 3	0.3	- 0,9 1 9 0 6 0 0 - 1 9	
37	19 5	22 0 - 8 5 16 0	$-\frac{13}{42}$ $-\frac{13}{13}$	18	0.3	0.0	
38	-10 5	- 85	- 42	- 39	- 1.8	- 19	
39	150	16.0	- 13	0.3	- 0.3	- 07 03 00	
41	-19 2 -11 2 14 3		- 09	- 11	0.8	0.3	
42	11 2	- 3 3 21 0	9 9 5 5	8 2 7 4	12	0.0	
50	14.3	21.0	5 5	7.4	19	1.4	
51	-227	-12.1	2,0	3 4	0.0	- 01	
52	-20 5	-21 0	51	- 55	- 13	- 13	
54	-13 5	- 95	- 51 - 28 - 3.6	2.2	0.5	- 13 08	
55	-11 0	-15 5	- 3.6	- 08	- 09		
57	-100	- 55	- 2.4	- 1.9	- 1.4	-18	
58	6.0	43	$-\frac{2.4}{1.7}$	3.1	- 1.4 - 0.2 0.6	- 1 8 - 0 2 - 0.1	
59	9.5	11.0	- 1.7	- 1.1	0.6	- 0.1	
60	-14 0	-12.0	0.7	0.8	01	- 01	
61	3.5	4.5	- 5.4	- 4,2	- 1.5	- 17	
62	3.5 7.3	11.0	3,7	4.5	0.6	- 1.7 0.8	
63	3.0	1.5	- 25	- 37	- 1.3		
56	5.5	6.0	- 4.8	- 3.2	0.4	0.5	
67	0.0	- 32	- 1.3	0.0	1.0	1.5	
70	-20 -130	- 3 2 -11.5	0.1	2,5	0.2	0.5 1.5 0.3 — 0.6	
71	35	3.5	1.5	0.0	0.3	0.0	
71	- 9.5	- 50	0.7	2.7	$-{0.3\atop 0.3\atop 0.4\atop 0.4}$	- 00	
72 73		87	- 5 7	- 4.0	0.4	0.1 0.3 0.1	
78	10.5	87	- 57		0.5	0.3	
74	5.5 25.8	3.0	- 2 0 - 1 0	-1.1	- 06	0.1	
75		28.5	- 10	0.6	1.5	1,3	
76	20	5 0	10 0	10 0	1 5 2 7 — 1.1	2.1	
78	-17.5	-10.5	- 0.3	0.6	- 1.1	- 1.3	
80	0.0	-40	21	3 1	1.4	1.3 - 1.3 1.1 0.7 - 0.7 - 0.3	
82	-18 0	- 89	2.2	4.8	0.7	0.7	
83	11.8	12.4	1.2	24	0.1	0.7	
84	0.0	13.5	0.1	2.7	- 0.4	- 0.3	
88	3.5	25	- 3.7 - 2.3	- 3.6	02	0.2	
87		0.2	2.3	- 1.3	- 0.5	- 0.3	
88	-11.0	- 6.0	- 62	- 4.6	- 1.1	- 0.9	
20	23.5	29.0	2.1	4.8	0.6	0.7	
92	- 3.6	-3.3	2.4	3.1	17	16	
93	- 15	- 1.0	2.1	3.2	0.8	0.5	
1	_						
V & Dev	$^{2} = 99.9$	97.6	31.0	23.9	8.38	7.72	
4 4							

	TABLE D (continued)								
Ind.	Visual Ind. Vocabulary			letion	Arithmetic				
Liiu	1	2	1	2	1	2			
1 2 5 4 7 9 10 11 11 14 14 10 11 12 12 12 12 12 12 12 12 12 12 12 12		0.000 4.0100 5.0	- 0 0 1 1 1 1 2 2 4 4 2 2 2 1 1 1 4 0 0 3 3 6 0 1 1 1 6 1 1 0 0 1 1 0 0 1 1 0 0 1 1 0 0 1 1 0 0 1 1 0 0 1 1 0 0 1 1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		- 10 - 10 - 10 - 10 - 10 - 10 - 10 - 10	144 144 144 144 146 146 146 146 146 146			
V 2 D									

Ind.	Rea	ding 2	Omi	ubus 2	Proverb	Age in months	Teach	er Rank
1	- 4.2	- 7.6	25 7	25.9	- 2.4	4.7	-10	- 9
2 3	4.8	4.4	+38.8	+28.6	04	2.7	+ 2	+ 9
3	- 2.2	- 3.6	- 97	-19 9	- 1.4	- 5.3	+10	0
4 7	- 62	-15 B	-21 2 - 8 7	-15 9	- 2.4	2.7	-21	-22 -26
9	38	-15 6	+ 2.3	-15.9 - 9.9	- 2.4 - 2.4	5.7	-28	-20 -17
10	- 32	- 08	+ 18	11 9	- 34	12.7	‡ 7	‡17 5
11	5.8	5 4	- 32	-22 9	- 0.4	2.7	+ 4	-10
13 14	$-\frac{72}{42}$	- 58	-10 2	-239	- 0.4	-14 3	- 6	
15	0.8	- 8 8 - 3 6	-24 2 -10 2	-34 9 -11 9	1.4	- 2.3 -16 3	-29 + 1	30 4
16	5.8	0.4	-26 2	-15 4	0.6	15 7	-26	97
18	28	0.4	+23.3	+18 6 -12 4	-14	-13.3	+23	+ 8
19	0.8	- 3 6	+ 28	-124	- 1.4	14 7	-25	20
20 21	- 4.2 0.8	- 0 6	- 5 7 -34 7	+ 0 1 15 4	- 1.4 3.4	- 63 -11.3	-17 -16	-19 -17
23	- 1.2	5.4	+24 8	+181	0.6	- 53	+12	1.19
23 24	3.8	- 0 6	- 57	+191	0.4	- 73	+25	+23
26	- 1.2	- 66	- 52	-13 9	- 14	31.7	-26	-28
27	6.8	114	+61.8	+516	6.6	-11 3 4 7 3 7	+31	+29
28 29	- 0.2 - 2.2	- 4.4 3.4	-11.7 -27.2	+11 6 -11 9	- 1.4 2.6	9 7	+17	+11
30	0.8	- 0 6	+36 3	+13 6	- 2.4		+ 8	T 2
31	18	- 36	15 2	-14	-14	1.7	- 3	- 2
32	- 0.2	7.4	+27.3	+ 46	- 0.4	11 7 13 7	-11	-16 +28
35 37	5.8	- 5 6	+54.3 + 4.8	+37 1	6 G	10 7	⁺²⁹ ⁺⁹	710
38	- 0.2	5 1	-112	+ 26	0.6	-83	8	T-6
39	-0.2	1.4	-1 16.3	+15.1	- 2.4	- 0.3	+19	+ 4
41	- 02	9.4	+29.3	+49 6	6.6	37	+33	31
42 50	- 3.2	- 8.4 - 9.6	+33 6 - 6 7	- 89 -119	- 0 4 0 6	- 43	+15 -15	+14
51	2.8	3.4	+28 3	+35 1	-11	-10.3	+21	1.95
52	1.8	0.4	- 52	- 09	- 0.4	- 03 127 27	+ 5	+ 7
54	- 4.2	-12.6	-29.7	-20 9	- 34	12 7	-31	-31
55	2.8	5.4	+153	- 69	0.6	- 33	-14 + 3	+1
57	- 1.2	- 1.6	+ 9 3 -28 2	+28 1 + 0 6	- 3 4 - 0 4	-153	+25	1.22
59	0.8	1.4	+ 53	-14 3	5 6	97	T 2	+22 + 3
60	4.8	- 3.6	-182	-17.4	-14	15 7	-24	
61	0.8	- 36	-41.2	- 39	0.6	-13 3	-1	- 7
62	- 0 2	- 6 6	+25 3	+30 6 -12.4	- 2 d	11 7 5 7	+22 -19	+27 -29
66	- 0 2 - 0 2	8.4	+14.8	- 09	0.6	37	- 7	- 8
67	-1.2	- 56	13 7	-144	- 04	4.7	-23	-25
70	- 2.2	1.4	-127	-1-16	0.6	-17.3	+13	- 1
71	0.8	- 9 6	- 62	+ 16	- 24	-10 3	- 5	-15
72 73	- 0.2 - 0.2	9.6	+33.8	+20.1 -18.4	4.6 0.6	0,3 29.7	+18 -27	+28 -14
74	1.8	- 06	-7.2	+ 4.1	- 0.4	- 83	+24	+21
75	- 2.2	1.4	-27.2	-10 9	-14	7.7	-13	- 6
76	- 32	4.4	-13 7	14 4	- 0.4	0.7	- 4	+16
78 80	- 2 2 - 0.2	3.4 8.4	+14 8 +33 8	- 19 +411	- 24 26	-10 3 - 8 3	+16 +27	+15 +30
82	1.8	- 36	+24 8	+20 6	66	-183	+28	T24
83	-4.2	0.4	-47	-49 4	- 24	4.7	-22	-21
84	18	0.4	-10 2	+ 51	3.6	- 73	-12	18
86	28	1.4	-14.7	+ 5.1	- 3.4	- 2.3	-18	-23
87 88	- 0 2 3.8	3.4 5.4	- 7.7 + 1.3	+ 1.6	0.6 2.6	-13 3 - 6 3	±20 6	+13 +12
90	m-16.2	- 4.6	-28 2	0.00	- 04	- 03	- 9	-3
92	- 2 2 0.8	6 4	+16.3	+ 36	4.6	- 0.3	+11	+-20
93	0.8	- 4.6	+ 33	-119	- 0.4	3.7	+14	+18
Σ Dev 2	= 28.7	49.5	180.0	164.0	20.7	82.6	144.3	144.3

	TABLE D (continued)								
Ind.	School Mark			posite	Visual Vocabular +Completion				
1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		0.44 0.41 0.41 0.41 0.41 0.41 0.41 0.41	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	2 40.5 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	# # # # # # # # # # # # # # # # # # #	11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			
88 90 92 93	- 6.9 - 41 - 7.9 - 1.1	- 8 4 - 0.4 - 1 4	5 9 89.6 46.2 14 8	40.5 12.0 12.5 51.3 21.6	- 0 3 0 7 - 4 3 10,7 - 5.3	-19 - 4 - 4. 10 6.			

TABLE E

Weights Given to Each Test in Evolving a Composite Measure Multiple = the number by which the deviations of the tests to the left were multiplied or divided to secure the desired weighting.

	Sa.			Multiple		Weight Given
Addition	1	16.73		4	2000	4.2
	2	17.38	÷	4	Ξ	4.3
Cancelling 2	1	15.90		5		3.2
- "	2	15.70	-	5	=	3.1
Cancelling 3	1	15.00		5	Ξ	30
	2	14.72		5 5	=	2.9
Cancelling A	1	9.17	-	5	=	1.8
	2	9.96	-	5	=	2.0
Cancelling S	1	9.99		5	-	2.0
	2	9.76	+	5	=	2.0
Copying Addresses	1	3.10	×	1	March	3.1
	2	3-39	×	1	=	3.4
Visual Vocabulary	1	3.98	×	1	=	4.0
	2	4 39	X	1	=	4.4
Completion	1	4.29	×	3	=	12.9
	2	4.09	×	3		12.3
Arithmetic	I	1.13	×	3 8 8	==	9.0
	2	0.86	×	8	=	6.9
Reading	1	2.87	×	2	=	5.7
	2	4.95	X	2	=	9.9
Omnibus	I	18.00	×	1	=	18.0
	2	16.45	X	1	=	16.5
Teacher Rank	1	14.43	-	2	==	7.2
There is	2	14.43	÷	2	=	7.2
School Mark	1	8.72	+++++++++	1	=	87
* This Games has an ex-	2	8.03	×	1	*****	8.0

*This figure has no special significance.

3. CALCULATION OF RAW COEFFICIENTS OF CORRELATION

A coefficient of correlation is a numerical statement of the proportionality between two series of measures. If the excellence of the scores made by a number of individuals in one test is exactly proportional to the excellence attained by the same individuals in another test, the correlation is positive and perfect. Using r as an abbreviation for correlation r = +1. If the proportionality is exactly inverse, r = -1. If there is no tendency to proportionality r is either a positive or negative decimal according to the direction of the tendency.

The standard method ¹ has been used in calculating all the coefficients of correlation. This method is expressed by the Pearson formula:

$$r = \frac{\sum x y}{\sqrt{\sum x^2} \sqrt{\sum y^2}}$$

1 The Brayais-Galton-Pearson method

Referring to Table D the method of calculating the r for, say, Addition (t) and Cancelling 2 (1) was, viz.: The deviations in the Addition (t) column were considered x's while the deviations in the other column were y's. The numerator of the formula was obtained by getting an algebraic sum of the products of every x multiplied by its corresponding y. The figures at the foot of the two columns being correlated were the denominators of the formula. Given these, r was easily calculated. By employing this method the first measure of every test was correlated with its second measure; some measure of every test was correlated with some measure of every other test; in certain instances, every column of a few tests was correlated with every other column of a few tests was correlated with every other column of certain other tests. These first coefficients are called raw coefficients.

4. CALCULATION OF CORRECTED COEFFICIENTS OF CORRELATION

Thanks to the excellent work of Spearman, we now know that these raw coefficients are not true representations of the proportionality between measures or functions. He discovered that chance inaccuracies in the original scores did not balance themselves out but that they always tended to reduce the correlation toward zero. The correlation was said to be "attenuated." The next step in this study was to correct the raw coefficients for attenuation. There was used for this purpose Spearman's formula:

$$r_{pq} = rac{\hat{\sqrt{(r_{p_1q_1})} \ (r_{p_1q_2}) \ (r_{p_2q_1}) \ (r_{p_2q_2})}}{\sqrt{(r_{p_1p_2}) \ (r_{q_1q_2})}}$$

where, if A and B are the facts to be related, p is a series of exact measures of A, q is a related series of exact measures of B. r_{pq} is the coefficient of correlation of A and B, obtainable from the two series p and q, thus being the true coefficient. p, and p, are two independent series of measures of A. q_1 and q_2 are two independent series of measures of B. r_{pqq} , is the correlation when the first measure of A and the first measure of A are used. r_{pqq} is the correlation when the first measure of A and the first measure of A and the first measure of A and the second measure of A are used and so on for the remaining the second measure of A are used and so on for the remaining

¹ For a criticism of Spearman's assumption see Brown, The Essentials of Mental Measurement.

symbols. It is now clear why two measures for each individual in every test were necessary. Without two measures the raw coefficient is the best measure obtainable.

The raw intercorrelations among all the tests (except the practice tests) for which there were double measures, were calculated for every column with every other column in that group. This group also included the Composite. These raw coefficients supplied all the necessary data for calculating the true coefficients from the Spearman formula. Now the practice tests gave much more reliable measures for each individual; hence, whenever a practice test was being correlated with any other test just enough coefficients were calculated to satisfy the shorter correction formula:

$$r_{pq} = rac{\sqrt{(r_{p_1q_1}) \ (r_{p_2q_2})}}{\sqrt{(r_{p_1p_2}) \ (r_{q_1q_2})}}$$

By the use of either of these two formulas the corrected coefficient or the true correlation was found for every test or function which was measured twice. The Age of Reaching the Grade, while really one measure, was treated as though split exactly in two, $r_{\rm top}$ in the shorter formula thus being considered as + 1. This left only one test uncorrected. Table F gives the corrected coefficients or the true correlations between the tests and the functions which they measured. A gap in the table means that the true coefficient is substantially zero. The correction at that place was impossible either because one of the raw coefficient turned out zero or because one was a small positive and the other a small negative. In either of these cases the correction formula fails to work.

The shorter correction formula above is the same as the longer formula except that two symbols have been omitted from the numerator. Theoretically, it would have been better to have retained the omitted and omitted the retained symbols, but, practically, the difference in correction is insignificant. The longer formula is to be preferred but the time required often makes its use prohibitive.

CORRECTED PEARSON COEFFICIENTS OF CORRELATION

JSCA

sassa

Composite	### ##################################
School Mark	Har se akatekse s
Teacher Rank	Yes cessicities es
Age	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
eudinmO	21-11-1
Reading	
Arithmetic	Nice214 8 8 8 8 9 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5 6 5
Completion	1888 8288 8288 1888 1888 1888 1888 1888
udanoV laneiV	****** *** ***************************
BaitnwbasH	244222 82 8 8
Copying Addre	###### ##### #########################
Cancelling S	1
Cancelling A	8.68 8.89 8.99 8.99
Canoelling 3	## ###################################
Cancelling 2	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
notibbA	

5. RELIABILITY COEFFICIENTS

The significance of the corrected r's shown in Table F is dependent on their reliability. This reliability is in turn dependent on the number of subjects used and the amount of correction that has been applied. The "reliability coefficient" or the raw r for two separate measures of any one test indicates the amount of this correction. The corrected r for two tests whose reliability coefficients are exceedingly small is of doubtful value. Some of the factors which make for high reliability coefficients are: that the function tested be narrow; that the time spent in testing be long; that the test material and experimental technique for the two tests be identical; and that there be no large variation in the condition of the subjects. The reliability coefficient for every test having a double measure is shown in the table of raw coefficients further on in this book, but for convenience they are summarized below.

TABLE G

RELIABILITY COEFFICIENTS, TOGETHER WITH THE TOTAL TIME SPENT ON THE TEST OR TESTS COMPOSING EITHER ONE OF THE TWO CORRELATED MEASURES MEASURES

Addition, 100 minutes (10	tests)										
Cancelling 2, 8 minutes (8											
Cancelling 3, 8 minutes (8	tests)					 	 	 ٠.	 	٠.	
Cancelling A, 7 minutes (7											
Cancelling S, 4 minutes (4	tests)					 	 	 	 		
Copying Addresses, 100 mir	nutes	(10	tests	3)		 	 	 	 		
Handwriting, 40 minutes (1	to test	s)				 	 		 		
Visual Vocabulary, 30 or le	ess mi	nute	s (I	tes	t).	 	 	 	 		
Completion, 30 or less minu	ites (I tes	t)			 	 	 	 		
Arithmetic, 30 or less minu	ites (tes	t)			 	 	 	 		
Reading, 30 or less minutes											
Omnibus, 60 or less minute											
School Mark, I semester											
Feacher Rank											
Composite											

The very, very high reliability of the tests from Addition through Handwriting is due chiefly to the narrowness of the functions tested, the similarity of the test material and also, in the case of Copying Addresses and Addition, to the relatively large amount of time spent on the tests. Intercorrelation among these tests scarcely needed correction. The reliability of Arith-

¹ These factors do not grow out of our data.

metic and Reading is unsatisfactory; that of Visual Vocabulary and Completion leaves something to be desired; all the rest are satisfactory. The coefficient for Teacher Rank is surprisingly large, due probably to the close coöperation of the two teachers in teaching the same children. So, with regard to reliability, the only corrected coefficients which need to be closely scrutinized are those with Arithmetic and Reading.

We have spoken of the reliability of the tests as dependent on the amount of the correction. It is important to know the reliability of any particular coefficient derived from these tests. This is dependent on the number of cases or the number of individuals. P. E. is the measure of this reliability according to the formula:

P. E. =
$$\frac{.6745 (1-r^2)}{\sqrt{n}}$$

where r = actual coefficient of correlation and

n == number of cases included. If the number of cases were infinite the reliability would be absolute. We have always used sixty-three cases, hence

P. E. =
$$\frac{.67 (1 - r^2)}{\sqrt{63}}$$

Using this formula we get:

PROBABLE ERROR OF THE COEFFICIENTS OF CORRELATION

-	P E.
r	
.1	.08
.2	.08
.1 .2 .3 .4 .5 .5 .6 .7 .8 .9	.08 .08 .07 .06 .05 .04
-4	.07
-5	.06
.6	.05
-7	.04
.8	.03
.9	.02

CONSIDERATION OF PROBLEMS AND COMPARISON OF RESULTS WITH THOSE OF OTHER EX-PERIMENTERS

1. What Are the Intercorrelations among Some Recent Educational and Vocational Measurements and Certain Traditional Tests?

The first problem which this study set out to attack has now been solved. The corrected coefficients given in Table F are the answer. Since these correlations will be considered in connection with other problems, a detailed discussion at this place would be tedious. In interpreting the corrected r's the reader should remember one fact in addition to the cautions given in the preceding chapter. Handwriting was scored by amount copied and no attention was given to the quality of the penmanship. A large score in this test might mean that the quality of the writing had been sacrificed. On the other hand, it might be contended, from a study of the penmanship of men of great ability, that increased speed and decreased quality both correlate very highly with mental power. With no evidence to offer, the author prefers to leave the matter to the opinion of the reader.

2. What Is the Order of Each Test's Correlation with Mental Ability?

Before this problem can be solved we must have some measure of mental ability. This study proposes three different standards by which to measure each test.

The first standard includes all the available measures which are outside our psychological tests. The ideal standard would be one which properly weighted all the activities in the life of an individual. A complete standard would take into account not only how well one does in a psychological test but also what kind of grade is made in school, what kind of opinion the teachers have, how well the games of ball are played, the papers sold, the errands run, etc. Of all these things there are, outside the psychological tests, just two measures available: Teacher Rank and School Mark. The value of these two measures as one of our standards consists in the fact that they represent an attempted weighting of numerous activities, and that they are measures free from any preconceived opinions of this study. The corrected r's in Table F for Teacher Rank and School Mark have been averaged for each test, and the positive size of this average has been taken as that test's correlation with mental ability.

The second standard used is the correlation of each test with the Composite. The Composite combines the standard just described with the psychological tests. Possibly the Composite gives too much weight to the Cancellation tests but, in view of the later discussions of this book, it is perhaps wiser to err in this direction. All considered, the writer believes this to be the best measure of mental ability available for this study.

The third standard by which to determine the value of a test as a measure of mental ability is the average of that test's correlations with all the other tests. But immediately we get into a difficulty, a difficulty which was minimized in connection with the use of the Composite as a standard. A glance at Table F will show that there are at least two distinct groups of tests which oppose each other: the Cancellation group and the group represented by the Complex tests. In evolving the Composite measure, this difficulty was surmounted by arbitrarily giving a relatively small weight to the Cancellation tests. But with the third standard where equal weight is given to each correlation the Cancellation group will exert an important influence. Obviously, it would not be fair to give as much weight to five Cancellation tests as to five other separate tests, especially when the Cancellation group measures such a narrow function. If there were just one such test the matter would not be so serious. If the Cancellation tests are good measures of mental ability then the Complex tests are not. In this dilemma our first standard proves its worth. Teacher Rank and School Mark, admitted by all experimenters to have considerable value as measures of mental ability, vote against the Cancellation group. Further, common sense shows that the other group measures a wider range of abilities. Moreover, any one test in the Complex group shows a wider range of positive correlation. Consequently, no test will be used for the third standard that does not show a distinct positive correlation with the first standard. This eliminates Age, Handwriting, and the Cancellation tests.

Using these three standards the order of each test's correlation with mental ability is shown in Table H.

TABLE H

Order of Correlation of Each Test with Mental Ability by Standards 1, 2 and 3 and by an Average of the Three. (Data from Table F)

19	Teacher Rank a	nd		
	School Mark	Composite	All other tests	Average
Omnibus	-75	1.00	.66	.80
Completion	-73	.96	.64	.78
Teacher Rank		.86	.63	-75
School Mark		.91	-54	.73
Reading	.68	.81	-53	.67
Arithmetic	.62	.72	49	.61
Visual Vocabulary	-44	.80	.56	.60
Copying Addresses	-34	-54	.29	.39
Addition	.23	-37	.20	.27
Handwriting	.02	.22	.13	.12
Cancelling A	.00	.00	08	03
Cancelling S	10	.00	09	06
Cancelling 2	28	18	23	23
Cancelling 3	28	18	24	23
Age	50	26	19	25

In studying Table H it is important that the reader remember that a coefficient of correlation from arrays of averages is not necessarily the same thing as an average of several coefficients of correlation. An example of the former are the coefficients in the column under Composite, while an example of the latter are the coefficients in the other three columns. But our problem is not now to discover the absolute coefficient of correlation between any one test and mental ability; it is to rank the tests relatively, i.e., which test correlates most closely, which second, which third, etc. Each of the three standards should give sustantially the same ranking to each test. In fact, the agreement

is remarkable. The average of the ranking by the three standards is practically the same as the ranking by any one of the standards. This average can be taken as the answer to our problem.

5. How Close Is the Correlation of Each Test with Mental Abulty?

The answer to the above problem depends upon which standard is accepted as the best measure of mental ability. Omnibus correlates .75 with Standard 1, 1.00 with Standard 2, and .66 with Standard 3. Which is the truest coefficient? To trust to an average of the three, as was done in section 2, would merely serve to conceal glaring differences. The Composite is better than Standard I because it includes Standard I along with many other valuable measures. Standard 3 or the correlation of each test with all others gives an equal weight to all the measures composing it, but all three standards agree that all the tests do not equally measure mental ability. The Composite gives a weighting which is, at least, roughly correct. Strictly speaking, the correlation of a test with all other tests taken separately is a measure of a test's correlational spread rather than an absolute measure of its closeness of correlation with all these separate abilities considered together. So far as the question under consideration goes. Standard 3 assumes that, disregarding chance errors in measurement, any one test is as good a measure of mental ability as any other and that any one test is as good as all averaged together. The Composite, on the other hand, considers a sum of properly weighted abilities a better measure of mental ability than any one of them taken separately. For these reasons this study considers the Composite the best available measure for determining the absolute correlation between any one test and mental ability.

Since we are hopelessly immersed in theory, we may as well consider the most important objection likely to be offered to the Composite. It might be said that the Composite causes a test to show a spuriously high correlation with mental ability because it is composed of the tests which are to be correlated with it. On the contrary it might be argued that to eliminate Completion, say, from the Composite before correlating it with the Composite would unfairly reduce the correlation, for mental ability means

the ability to do Completion as well as the ability to do the thousand and one other things which enter into complete living. To strike a true balance between these two contentions would be difficult if not impossible, consequently the Composite has been retained in its original form.

Using, then, the Composite as a standard, the closeness of the correlation of each test with mental ability is shown in column 2 of Table H. This column reveals five interesting facts:

a. Omnibus and Completion correlate perfectly with mental

- ability. To be exact, Completion correlates +.96.

 b. Seven of the tests correlate closely with mental ability.
- c. The Cancellation tests give a negative correlation with men-
- tal ability.
 d. The Age of Reaching the Grade also correlates negatively
- d. The Age of Reaching the Grade also correlates negatively with mental ability.
- e. The coefficients for the tests which measure power are in every case larger than the coefficients for the tests which measure speed.
- 4. What Is the Practical Significance of These Facts for Educational and Vocational Diagnosis and Guidance?

Before considering each of the above facts in the light of the problem just stated it is interesting to consider another question: just what is the need for measuring mental ability? The pseudophilosopher derives his greatest pleasure from discoursing upon the negative correlation which exists between the academic and the real world. In one respect at least this antagonism no longer exists. The most persistent demand that has come to the psychologist in the last few years has been, that he develop a means for measuring that most elusive yet pre-eminently valuable thing which we call mental ability. And this call comes from school and factory alike.

The school wants to adjust its training to the individual differences of the pupils. How can it measure these differences, is the question asked of the psychologist. The principal wishes to classify a group of children by ability. How measure the ability? The jumior high school wishes to put in one group the supernormal

¹ There is a statistical method by which the amount of spurious correlation can be determined. pupils, in another group the normal, and in another the subnormal. How be certain the pupil is not wrongly placed? Educators realize that some pupils simply haven't the ability to deal with mental elements, abstract symbols and the like. Which pupils? A class for mentally defective children is being formed. Who should be in the class? A college in the West is planning to select its Freshman class on the basis of mental tests. Are the tests valid measures of mental ability? Experimenters everywhere wish to form groups of equal ability. By what standard shall they be called equal? Sociologists wish to discover if unemployment is the result of mental defectiveness. How gauge the mentality? Makers of mental tests desire a standard by which to measure their own product. What standard is reliable? The youthful yet virile science of vocational guidance wants to prevent or diminish the present fearful misdirection of energy. Business is little less clamorous, but no more need be said to show the very great importance of discovering excellent measures of general ability as well as tests for special powers. Now let us return to the significance of the facts reported in the last section. The first of these was:

(a) The Omnibus and Completion Tests Correlate Perfectly with Mental Ability

The problem of measuring every single activity of an individual in order to determine his general mental ability, is, of course, impossible of solution. So psychology has been trying to find a few measures which epitomize all possible measures. So fast as the writer is informed, the test which has received the most favorable mention in this connection has been the Ebbinghaus Mutilated Text. The Completion Test, mentioned above, is a development by Dr. Trabue of Ebbinghaus' idea. This study finds ample justification for the high favor accredited the Ebbinghaus Test and it congratulates Dr. Trabue upon a modification of it which is likely to prove still more valuable. If we remember that mental ability means mental ability as measured by our Composite, the Completion Test correlates with it + .96. The correlation is not exactly perfect but it is very nearly so.

This study is equally pleased to congratulate Dr. Thorndike upon having compiled and in part devised the Omnibus Test

which correlates + 1.00 with our Composite. The Completion Test was given for thirty minutes, the Omnibus for sixty minutes. Does this correlation of + 1.00 mean that a test has at last been devised which gives a perfect measure of an intellect by one hour of testing? It must not be forgotten that the + 1.00 is a corrected coefficient. Were the 1.00 a raw coefficient and were the Composite adequate the above question could be given an affirmative answer. The corrected coefficient 4 1.00 means that were an individual measured enough times with the Omnibus Test to be certain of an accurate score, then that individual would have as perfect a measure as if he had been given all the tests composing the Composite. How many times and how long each time a person would have to be tested in order to give a perfect 1 measure of him in any one function is for a future research to determine. But granting the Composite is not an adequate measure of mental ability and granting the correction is a little too large, the fact remains that the Completion Test and Omnibus Test are very excellent ones. But because of the multiplicity of mental functions and the variability of their performances it is wise to give several types of tests and possibly to secure several measures for each type. This brings us to the second significant fact mentioned a few pages back:

(b) Seven of the Tests Correlate Closely with Mental Ability

Since it is wiser to trust to several tests than to one or two, those interested in educational and vocational diagnosis, guidance, and classification as well as vocational selection will want advice as to what tests this study would recommend. Of the fourteen measures used, we consider the following to be the best and most reliable indices of intellect: Omnibus, Completion, Visual Vocabulary, Teacher Rank, School Mark, Reading and Arithmetic. The first five tests are the best. An average from them will give a good measure of an individual's ability, and that with the expenditure of just two hours in actual testing. The difficulty of the purely psychological tests could be varied to suit the ability of the group being tested. It ought not be long until other tests are devised which can be added to this small group. It is not too much to hope that the near future will that the rear future will the proposed of the properties of the proposed of th

find psychologists able to measure general mental ability very accurately for a group of any size after one day of testing. Until that time comes we now have tests which will measure intellect roughly at least. And for many purposes such a rough measure will suffice

To the five measures recommended in the preceding paragraph three criticisms suggest themselves. In the first place, Teacher Rank and School Mark are not always available. Or in cases where they are available, it is often impossible to use them because Teacher Rank is not an absolute measurement and because School Mark varies in meaning even within one school. In the second place, the psychological tests recommended, measure, primarily, abstract ability-the ability to handle ideas and symbols rather than to deal with "things and their mechanisms." All that we know 1 about the relation between Idea Thinkers and Thing Thinkers indicates that the man who is good at manipulating ideas is potentially good in manipulating things. If the mechanical skill desired requires special training this criticism is more serious. The third criticism is that such tests as these can only be given to literate people. This is true but it is a fault which our schools are repairing every day. These three criticisms merely limit the usefulness of these measures and they emphasize the fact that even psychological testing requires the exercise of common sense

Another result of this study which may prove of practical value is:

(c) The Age of Reaching the Grade Correlates Negatively with Mental Ability

Probably every text-book on the psychology of individual differences mentions mahwify as an important factor in producing differences in mental ability. But no educational administrator now believes that mental age always coincides with chronological age. If he does so believe, he does not dare use it as the sole basis for the classification of the school children. A very common complaint among young teachers is that their chronological age weighs heavier than their mental age with school superintendents. Besides these immediately practical significances, the

¹We greatly need tests of mechanical ability to experimentally test this statement.

influence of age is of keen concern to almost everyone who is engaged in educational or psychological research. Correlational psychology, for example, is in constant fear lest its insidious influence operate to produce spurious correlation. To be brief, no one would object to this statement: below the age where senility begins, the tendency is for the older individuals to be the more able. In so far as the two sixth grades studied here are typical of all grades, we find an exactly opposite tendency, which may be summarized, viz: in any one class the tendency is for the more mature to be the less able. This is no rank heresy nor is it an unpredictable mystery. If a pupil is overage for his group it probably means that he has been retarded, and this in turn probably means that he started life with an intellectual capacity which could be expressed as a minus deviation from the average. So the influence of maturity is not a simple one, or to speak more exactly, age is no sure criterion of mental ability. The meaning of age is dependent upon the group in question. The scope of the negative correlation found in this study needs to be tested by experiments upon other grades and other groups. Even more important is the next fact growing out of this research:

(d) The Cancellation Tests Show a Negative Correlation with Mental Ability

We say above that Cancellation correlates negatively with the Composite. The zeros after Cancelling A and Cancelling S (Table H) mean that in those two cases the correction formulas could not be applied. In addition to the evidence of Table H the trustworthiness of the negative correlation is further certified to by the fact that the Cancellation tests correlated negatively with each of the seven tests which have shown themselves to be good measures of mental ability. The coefficients are small but distinct.

It is beyond the scope and data of this research to consider why, so far as psychology is concerned, there has been such a chasm between laboratory and life. We suggest that possibly we have here, in the negative correlation of Cancellation with the Composite, one element of a complete explanation. The Carellation Test is a not unfair sample of what traditional psychology

has been employing in its laboratories. In order that positively interpreted results from such a psychological test correspond to results from practical experience, what is would have to coincide with what tends not to be. But a problem of such magnitude cannot be settled by the relatively mearer data of this study.

The point of main interest for us is that the Cancellation tests are now in very common use. A Cancellation sheet is about the first one that enters a newly established laboratory. One college is trying them out, along with others, as a partial entrance test. If other researches substantiate this one and experimenters continue to use it, the test must be interpreted negatively. But even here the correlation is so low the test is just about valueless for any positive purposes.

(e) The Correlations with Mental Ability of the Tests which Measure Accuracy and Speed Are Smaller than the Similar Correlations of the Tests which Measure Accuracy, Speed, and Power

Psychological and educational tests are readily divisible into two main groups: tests which measure accuracy and speed and those which measure accuracy, speed, and power. The factors, accuracy, speed, power, are really elements of every psychological test, hence our division may seem to the reader somewhat arbitrary. The division into two groups is due not so much to differences of elements as to differences of emphasis. The emphasis in the first group is upon accuracy and speed so let us call the tests classified there, 'speed tests.' In the second group the emphasis is upon accuracy and power, so let us call these tests, 'nower tests.'

As stated before, speed tests measure accuracy and speed primarily. They are usually simple in form and easily within the ability of the group being tested. Further, all parts of the test are about equally difficult. The chief characteristic of this type of test is that its units seldom approach in difficulty to the maximal ability of the group being tested. The instructions accompanying these tests, are to work as rapidly as possible without making errors. Our own Addition is an excellent example of a speed test. Courtis's Arithmetic as usually given is another example, though with sufficient time his tests could be used in

such a way as to make them power tests. Practically all the tests employed by the older, traditional psychology, such tests for example as 'Reaction Time,' 'Cancellation,' etc., belong in this group.

The power tests involve speed, to be sure, but the chief factors are accuracy and power. By 'power test' we mean one that contains units sufficiently difficult to discover the maximal ability of the person or persons being measured. A power test is usually of a more complex nature than a speed test. The first part is so easy as to be within the ability of the stupidest member of the group being measured, while the remaining parts of the test grow progressively more difficult until the maximal ability of the brightest individual is measured. Our Trabue Completion is an excellent example of this type. The Binet Test belongs in this group also. Mr. Clifford Woody is engaged in making arithmetic tests 'of the same nature. In fact most of the recent educational and psychological tests could be classified here.

Of the tests used in this study, Cancellation, Handwriting, Addition, and Copying Addresses are speed tests, while Visual Vocabulary, Completion, Reading, Arithmetic, and Omnibus are power tests. We have called the Omnibus a power test not because it is of the same nature as Completion but because it is complex, because some of its units grow progressively more difficult, and especially because all the units of the test hover close to the maximal ability of the group tested.

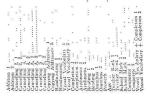
For the practical purpose of measuring mental ability which tests offer more promise, those of the speed type or the power type? The first evidence we have to offer is shown in column 2 of Table I. The coefficients in that column do not recommend the speed tests. Of the five different kinds of tests used, Copying Addresses proves itself the best as a measure of mental ability. But even it is always surpassed in correlation by what we have termed the 'power tests' Of course, this comparison, which has resulted unfavorably for the speed tests, refers only to the tests used in this research. Copying Addresses, however, probably ranks considerably above the average speed test in its correlation with mental ability. At least it probably occupies as

¹ "Measurements of Some Achievements in Arithmetic," Clifford Woody, Teachers College, Columbia University, Contributions to Education, No. 80.

favorable a position with respect to the speed tests as does, say, Visual Vocabulary with respect to the power tests. In so far as this is the case, the scope of our comparison extends to tests not employed in this study.

It is interesting to enquire into the causes for this difference in correlation between the speed and power tests. We believe that the emphasis upon bower, not as opposed to but as superior to speed, is one significant element. Much more experimentation would be required to establish this view, but so far as they go our results harmonize with such an assumption. Another significant element seems to be the complexity of the function tested. On the whole the power tests do measure more complex functions, The Omnibus is preeminent in complexity and in correlation with mental ability. The Cancellation tests are preëminent as to the narrowness of function they measure and they are last in their correlation with mental ability. The tests in Table I are arranged in the order of their correlation with mental ability. An order for complexity, so far as we can judge complexity by external appearance, would seem to correspond very closely to this arrangement by correlation. It is a matter for congratulation that the more recent mental and educational tests are embodying these elements of complexity and power. It is a pity the simple speed tests are not as valuable as the complex power tests, for they are easier to score. Furthermore, the complex power tests are not readily usable in long time practice experiments. By increasing the complexity of the speed tests we may yet make them valuable measures of mental ability.

In our comparison thus far we have considered only corrected coefficients. The practical measurer of mental ability must base his conclusions upon raw scores and not upon scores derived from many more measurements. Hence a practical comparison of speed and power tests must be made with raw as well as corrected coefficients. Table I gives the raw coefficients not only of each test with every other test, but, what concerns us most, the raw coefficients of each test with the Composite. Since each test has two or more coefficients with every other test, Table I is rather confusing, so for convenience, the reader is referred to Table J which is an average of the coefficients of each test with every other. TABLE I
RAW PEARSON COEFFICIENTS OF CORRELATION



Visual Vocabulary S S S + Completion 1 Salagasagasagas s

dravorT dissances et sient Proverb

													3				:				:	*	•		:			8			-01
	•	:		÷		v		3			3		1		3		ě			*	3	è						÷			9.5
2.0								:			:		3						00	÷		,			:	0	1	8			Completion
				1	ı.	*		:					-		:							÷		e.				ē			Ple
								:			3	•	-		:	i			:			1						9		×	5.8
5.	ż			÷			÷	1		8			1							į	•		•	ż	:		:	r	4	:	· CC
				•	o G					**	04		1	,-	oi	:	:	:	:	÷		i		ŝ		3	3		3	8	:++
					ं		3	1	1	S	83	١.		2	1					i	÷		1	•							55
		_	2	_	ni.	-	01		-	100	88			-	8			1	:	•	'n.		:			-	04	-	21	e	2 2
48			**			d	-		ij	-	ě	7	1	3	35	-	po	_	24		i		1			놡	ž	4	4		2 abulary abulary
	24			60	100		-			Ž	Ď	S. C.	3	E	20	c	c		0	_	-		64	×		3	Z	4	2		000
	c	Ë	9	ğ	Ē	i	H	É	C	·	N	E	=	>	>	2	310	7	3	be	30	å	ä.					Z	2	ij	255
2	ŝ	₹	7	17	音	F	5	품	ncell	9	2	2	3	=	70	픙	ë	E	Ë	5	2	ä	ã.	5		Ę,	ž	7	70	òd	200
dditton	Addit	Canc	n	nc	ü	n	ä	nc	ä	oby	â	Hand	Hand	1811.4	Su3	duno?	duno	1	Ë	ead	Readin	Omni	Janubus	AUL	8	eacher	eache	School	School	ошро	isua isua
V.	₹	೦	Can	ű	Ca	ű	ő	Ö	ೆ	೦	ő	Ä	H	5	5	ű	ű	₹	4	ř	ž	č	Ö	4	ď.	H	ř	ŏ	Š.	ŭ	U>>

AVERAGE RAW PEARSON CORFFICIENTS OF CORRELATION. (Data from Table I)

Visual Vocabulary + Completion	 	8 448
Composite		1888855 8
School Matk	មន់អន់នងខែមជន់ម	इस्ट्रेड हर
Teacher Rank	11 B888888	1848 984 1848
98A	24858238238	
Proverb	10000000000000000000000000000000000000	is 2438
*udinmO	1111 8282584284	455888
Reading	1888881148	445488
Arithmetic	입하다보험하용함의 5	1282282
Completion	1111 28822222	izádzás
Visual Vocabulary	111	**#8998
BaitinwbasH	844114 888	:2428288
Copying Addresses	Rusky saking	इक्षयम् स्थर
Cancelling S	28847 41988	3888888 38888888
Cancelling A	382 PESSE	1111
Cancelling \$	52 282482181	111 111
Cancelling 2	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	8222828
noitibbA	###########	ने श्चित्रं शक्ष्यं

10	0.0	2	23	12	0	œ.			og.	23	œ.	0	Composite Visual Vocabulary + Completion.

Table J permits a comparison of the closeness of raw correlation between each power test and the Composite with that between each speed test and the Composite. Consulting this table we discover that Copying Addresses, which is the best of the speed tests, shows a correlation of + 490 with the Composite, while Omnibus shows a correlation of + 480. In every instance, except in the case of Arithmetic, Copying Addresses gives a lower correlation with mental ability than do the power tests. So the raw coefficients say as emphatically as the corrected coefficients that a better idea of mental ability can be gotten by measuring with Omnibus, Completion, Visual Vocabulary and the like than could be gotten by running a practice experiment with Copying Addresses, Handwriting, Addition, or Cancellation.

The comparison of the speed and power tests is not yet complete. The speed tests as used in this study make available two important measures: an average of all the daily scores and the amount of improvement shown by subtracting the first measure of a test from the last measure. In general, a power test provides just one measure or else so few measures that improvability is too small to be of much use. Hence the power test has but one measure to balance the two obtainable from a practice test. It is conceivable that improvability with a speed test is a better intellectual index than a score from a power test. To discover if this be the case, the improvements made in the practice tests were correlated with the Composite. The improvement arrays were calculated in the following manner: the scores made on the first day by any one individual in Cancelling 2 and Cancelling 3 were combined and subtracted from the sum of the scores made on next to the last day. In order to get a reliability measure and to correct for attenuation, a second measure was calculated for each individual by subtracting the combined scores made on the second day from the combined scores of the last day. By a similar procedure a double measure was calculated for Cancelling A, for Addition, and for Copying Addresses. The absence of any individual on any one of the four critical days was corrected for as in Chapter III, Sec. 1. The improvement thus calculated was correlated with the Composite by the method described in the early part of this book, the only difference being that in correcting for attenuation the other half of Spearman's formula was used. The raw and corrected Pearson coefficients are given in Table K

TABLE K

CORRELATION OF IMPROVEMENT WITH MENTAL ABILITY (COMPOSITE)

Ruto Coepitienis	
Cancellation 2 + 3 (1) with (2) (Reliability) Cancellation 2 + 3 (1) with Composite (2) Cancellation 2 + 3 (2) with Composite (1) Cancellation A (1) with (2) (Reliability) Cancellation A (2) with Composite (1) Cancellation A (2) with Composite (1) Addition (1) with Composite (1) Addition (1) with Composite (2) Cancellation A (2) with Composite (2) Copying Addresses (1) with Composite (2) Copying Addresses (2) with Composite (2) Copying Addresses (2) with Composite (1)	.26 .13 .41 —.09
Average Raw Coefficients	
Cancellation 2 + 3 with Composite. Cancellation A with Composite. Addition with Composite. Copying Addresses with Composite.	01
Corrected Coefficients	
Cancellation 2 + 3 with Composite	.21

		COLLECTED COL	Dietenia					
Cancellatio	n 2 + 3 with (Composite				 	 	.21
Addition	n A with Co with Composite					 	 	.26
Copying A	ddresses with	Composite				 	 	
200	192		-00	21%	27			

If we compare the average raw coefficients of correlation in Table K with the column under Composite in Table J we see that improvement in the practice tests was, if anything, an even poorer measure of mental ability than was an average of all the scores. By the use of averages Copying Addresses did show a substantial correlation with the Composite, whereas by the use of an improvement measure, its correlation dropped almost to zero.

In considering the practical value of tests, other factors than those discussed should receive at least a passing mention. These are ease of administration and scoring and the amount of time required. Further it is just as important to ask what is the distribution of the time given to the test as it is to ask how much time is actually spent in testing. Thirty minutes of testing concentrated in one period, for example, is usually more convenient than fifteen minutes distributed over three days.

Of all psychological tests the Binet is the best known and the most perfectly standardized; yet for general use it will probably be supplanted by tests which require less skill and less time to apply. The problem of extending the sphere of psychological and educational measurement is very largely that of substituting group for individual testing. The speed tests and power tests used in this study are all well adapted for group measurement. They do not materially differ in ease of administration, nor is there a very great difference in ease of scoring. There is a difference, however, and this difference favors the speed tests. The speed and power tests can be compared for time and convenience by consulting Table G. This table considered in conjunction with Table J shows that one hundred minutes of Copying Addresses when distributed over ten days gives a correlation of + .40 with the Composite. Omnibus with only sixty minutes of continuous testing gives a correlation of + .80 with the Composite. In every instance the time spent upon the power tests was considerably less than that spent upon Copying Addresses. To sum up the entire discussion, the power tests give a much higher correlation with mental ability than do the speed tests: and this is true whether average score or improvement is used as the measure of the speed tests. Further, the power tests equal the speed tests in ease of administration, and they surpass them in time convenience. Ease of scoring, only, favors the speed tests, but this superiority is so slight as to be of small consequence.

The issue thus far has been drawn, on the one hand, between those of our tests which are simple in nature, which measure a relatively narrow function, which are considerably below the upper limits of ability, which have units roughly equal and which were designed and are adapted to measure speed and accuracy; and, on the other hand, those tests which are relatively complex, which measure a wider range of functions, which hover close to the upper limits of ability or else begin easy and grow progressively more difficult. Thus far we have considered the comparative excellence of these two main groups of tests as measures of mental ability. We can further draw the issue not between the two types of tests but between the two methods of administering any of them. It has been claimed that the amount of improvement shown by a practice test is a better intellectual index

than are "snap-shots" with those tests. The snap-shot test measures improvement from birth or conception, not to go back further, to the time in the life of the individual when the test is given. The practice test, on the other hand, measures improvement from the first to the last trial at that particular test. This issue could be settled fairly only by comparing the coefficients gotten by correlating the score from the first trial with mental ability and by correlating improvement, found by practice at that same test, with mental ability. But here our troubles begin. Those complex, snap-shot tests which show a high correlation with mental ability cannot conveniently be used in a practice experiment. And since only those which we have called the speed tests can be readily used for practice purposes the issue is really the same as that between the speed tests and the power tests, the speed tests representing the improvement measure and the power tests representing the snap-shot score. The decision reached in the preceding discussion favored the power tests.

It is possible, however, to view the speed tests, such as Addition, Copying Addresses, etc., as snap-shot as well as practice tests. and thus secure a comparison of the two methods. The first trial of these tests has not been correlated with mental ability but improvement has, and the results are shown in Table K. If the average from all the trials may be considered as at least a partial representative of the first trial then the coefficients for the speed tests in Table I under the Composite reveal some interesting inconsistencies. Measured by an average, Copying Addresses shows the closest correlation with mental ability of all the practice tests; measured by improvement it shows about the least correlation. The average correlates a little closer than the improvement in the cases of Addition and Cancellation of A's, while improvement has a slight advantage in the case of Cancellation of 2 and 3. However we may explain these apparent inconsistencies by differences of physiological limit, the fact remains that improvement in these tests is a very poor measure of mental ability, even poorer than an average, and probably no better than a first trial. In no case does it even approach a snapshot score for a power test.

- 5. What Are Some Theoretical Considerations Growing Out of This Study?
- (a) Is there such a thing as a negative correlation between desirable functions? Is the law of human nature correlation or compensation?

Rightly or wrongly Emerson is usually held responsible for a philosophic statement of the law of compensation. The law has been given a more scientific terminology by certain German psychologists, especially in connection with their attempt to classify individuals into types. Stated in whatever form, the implication is that there exists a negative correlation between desirable traits. From such a doctrine springs the idea that the higher the ability in dealing with abstract things, the lower it is in dealing with concrete things; that slow learners are long rememberers; that the person endowed with beauty is by the justice of Nature left devoid of brains; in short that Nature always balances a superiority with an inferiority. In the third volume of his "Educational Psychology," Professor Thorndike vigorously assails this doctrine. "It should also be noted that in original nature the rule is correlation, not compensation." Or again, "It is very, very hard to find any case of a negative correlation between desirable mental functions. Divergencies toward what we vaguely call better adaptation to the world in any respect seems to be positively related to better adaptation in all or nearly all respects. And this seems especially true of the relations between original capacities." In the stand taken by Dr. Thorndike, the author heartily concurs. Hence it is with no small surprise that he finds himself compelled to appear as a defender of inverse correlation between desirable mental functions. The only way to avoid the necessity of advocating a theory so unpopular with recent psychology is to call the ability to cancel the figures 2 and 3 or the letters A and S, an undesirable mental trait. The ability to perceive a thing, pick it out from other things, and do something with it seems so fundamental to all our mental life that we are scarcely justified in calling such an ability undesirable. Nor can we, without outraging the best of our common sense, call undesirable the abilities to do the Visual Vocabulary, Completion, Reading, Arithmetic, and Omnibus tests, or to make good marks in school and secure the teachers' esteem. And yet between the

Cancellation tests and this more complex group we find a negative correlation.

If the reader will turn back to Table I and count the number of coefficients of correlation which have been calculated between the Cancellation group and the complex tests mentioned above, he will discover that there are 56 such coefficients. Of these 53 are negative and only 3 are positive. Further, of these 3 not one coefficient is as large a positive as +.10 while there are negative coefficients of -35, -36, -37 and -39. The average of the 3 positive r's is +.07. The average of the 53 negative r's is -.21 (P.E. .08). Some of the negative coefficients are small enough to be due to chance, but it is much easier to believe that the 3 positive ones are due to chance. In view of the size of the negative coefficients and the unanimity of results from all the tests we are forced to conclude that the inverse correlation is genuine. Nor is this genuineness unsupported by previous experimenters. Dr. Chapman ('14), "Individual Differences in Ability and Improvement and Their Correlation," using the same Cancellation 2 and 3 tests upon twenty-two college students, found correlations between Cancellation and Mental Multiplication of a three-place by a three-place number as follows: .00, .03, .16, --.05. -. 13. -.. 14. These coefficients will average a small negative.

If future results substantiate our findings, what does it mean? It means that a negative correlation can exist and that many more may exist than we at present suppose. There are those who believe that training in one mental function is transferred to another in proportion to the size of the positive correlation between the two. If there be anything in such a belief, positive transfer accompanying a positive correlation may imply 1 a negative transfer accompanying a negative correlation. Such a state of affairs existing would mean that to educate a person in one trait would be to uneducate him in all the traits correlating negatively with it. It is not impossible to conceive that some of the more or less trivial traits intensively developed by the schools correlate negatively with a hundred valuable abilities. The mere possibility argues for the future development of experimental education. Our knowledge is very meagre. The wells which man has digged in the earth are far more numerous than the borings which psychology has made into the mental life. ¹ Such an implication is not necessarily true.

Though all these things be possible, we nevertheless believe with Dr. Thorndike that the law of human nature is correlation and not compensation. Although correlational psychology is a new science, it has several thousand coefficients to show for its labors. Never before, so far as the writer is informed, has a negative coefficient been so persistently in evidence. If inverse correlations were numerous, more should have made their apparance by this time. Further, the negative correlations found in this research may not mean that the functions are intrinsically inverse. Had a sufficient reward been offered, it may be that the brighter pupils in the complex tests would have forged ahead in the Cancellation tests. In a simple test like Cancellation possibly the brighter children lost interest first. Quite conceivably, different abilities have different interest and attention levels. Simple, routine, relatively easy tasks might be just right to interest the stupid, while they bored the abler individuals unutterably. Tasks difficult and complex enough to interest the abler individuals might be beyond the interest and attention of the stupid. A complete explanation of the cause would have to explain at the same time why the average from cancelling figures gave a negative correlation with the Composite while improvement at cancelling figures shows a slightly positive correlation with the Composite,

(b) What bearing do our results have upon Spearman's Common Factor?

The reader will remember that just a few pages back we were so unwary as to become involved in a discussion of the cause for a negative correlation. Why mental functions correlate in any way, whether negatively or positively, is one of the most vital, most difficult, and most disputed problems with which correlational psychology has death. One step toward an explanation has been an attempt to determine the correlational grouping of mental traits. Here the question asked is: With respect to their intercorrelations just how do the multitude of mental traits group themselves, into one system, two systems or many systems? Concerning this there are three different theories, the "multi-focal," the "intermediate," and the "unifocal."

Spearman in an article entitled, "General Ability, Its Existence and Nature," published in Volume V of the British Journal of

Psychology, summarizes the "multifocal" theory, viz.: "According to this view, ability in any performance depends upon a complex of elementary factors; the correlation between two performances simply measures the degree in which the elementary factors demanded by the one happen to coincide with, or to be bound to, those demanded by the other. The elementary factors include both 'form' and 'content'; by form is meant the kind of mental operation, as discrimination, observation, inference, etc.; while the 'content' denotes the different sorts of data, as color, shape, number, etc., submitted to such operations."

Between the "multifocal" and "unifocal" theories there are various intermediate ones which organize mental traits into a variety of "faculties," "centers," or "levels." Psychologists who classify the mental life into "types" or "faculties" imply that the multitude of functions composing any one "faculty" or "type" show a close correlation with one another while they show a loose correlation with traits which belong in a different "faculty," "type," or "center." Dr. Thorndike seems to believe in correlational "levels" when he writes: "Correlations seem to be closer within the analytical or abstracting functions than between these and others. So also within the purely mental associative functions like adding, completing words, giving opposites or naming objects. than between one of them and one of the sensori-motor functions. The sensivities seem to interrelate only loosely; and any one of them would relate very loosely to the associative or analytical functions, even when the latter was busied with data from that sense."1

The "unifocal" theory is represented by Dr. Spearman's famous "Common Factor." To quote from Spearman himself: "Here, the view supported is that all performances depend to a certain degree upon one and the same general common factor, provisionally termed 'General Ablilty.' Correlations are thus produced between all sorts of performances, the amount of correlation being simply proportional to the extent that the performances concerned involve the use of this general common factor, or 'General Ability.'" ² This criterion proposes not as many centers as there are "clementary factors," not as many centers as there are "faculties" or "types," nor even as many centers as there are the same than the same the same the same that same the same the same the same than the same than the same than the same than the same that the same than the

¹ Educational Psychology, Vol. III, p. 370. ² British Journal of Psychology, Vol. V, p. 52.

"levels"; rather it proposes just one center. In the same article Spearman summarizes the importance of this question by saying: "This sharp divergence between the three current views appears to be of grave importance. It bars the way to all interpretation of our laboriously accumulated correlational data. It confuses all theory as to the intellectual 'make-up' of individuals. And it paralyzes our practical power of gauging the intelligence of persons, both normal and insane." Following this statement Spearman proceeds to give his proof of the existence of the "Common Factor" and of the inadequacy of all previous conceptions. After many psychological considerations he decides that the "Common Factor" is "some common fund of energy." Finally he concludes with:

"(1) At present, there exists such a great divergence of opinion about the correlation between different intellectual performances, as to impede gravely the progress of psychology.

"(2) But closer consideration of all the actual data of the different authors shows that this divergence is merely due gross misinterpretation. In reality, all the facts indicate unanimously, that the correlation arises through all the performances, however different, depending partly on a General Common Factor."

Do our results support Spearman's contention and justify his conclusions? The first evidence we have to offer is the negative correlation between the Cancellation group and the Complex tests. Correlation, according to Spearman, is produced by the General Common Factor and modified by the "specific abilities" of the traits correlated. To quote again: " . . . every intellectual performance may be regarded as proceeding from two distinct factors; on the one hand, the specific ability or disposition for that particular performance; and on the other general ability. due to the common fund of intellective energy." What Spearman meant by "specific ability" may be gathered from these quotations: "An 'ear' for melody is known to be particularly specific, that is, independent of other elementary capacities." And again, " . . . their correlations (specific) do not occur in a pure state, but only superposed upon correlation of a more general character." The theory of the Common Factor seems to require that all coefficients of correlation be positive. How two functions can

share in a Common Factor and yet show a negative correlation we are unable to see. Perhaps the Cancellation traits are ostracized from the exclusive society of the Common Factor. Perhaps in the tug of war the "specific abilities," heading in a negative direction, outpulled the Common Factor. The proved skill of Dr. Spearman could doubtless defend his theory from such a trivial attack.

In the article already referred to, Dr. Spearman proposes a remarkably ingenious and important method of treating correlational results. By this method he proved to his satisfaction the existence of a Common Factor, hence the fate of his theory depends upon the proper working of this method. We purpose to treat our results by exactly the same method to see whether they justify a belief in a General Common Factor. In his article Spearman gave a correlational table which had the general form of the one given below. (The coefficients are not the same.)



Composite	11 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
endiamO	
School Mark	11 848899444 88
Teacher Rank	22 2 1 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
Visual Vocabular + Completion	824 824 825 825 825 825 825 825 825 825 825 825
Copying Address	ध्यप्रवंश अध्यक्ष
nonibbA	धर्मात्रधं श्रद्धध्याध
SnitrawbasH	4441 8488888
Cancelling 5	8882 H822 B88
Cancelling A	ser rigisizinasiria
Cancelling 3	2 28488228888
Cancelling 2	28842888888
	ecelling 2 ecelling 2 ecelling 3 ecelling 3 ecelling 5 ecelling 5 ecelling 5 ecelling 6 ecelling 7

Concerning the table of coefficients which Spearman gave, he wrote: "The most obvious method would be to devise as criterion some direct function of all the coefficients in the table. We have, however, chosen a somewhat different course. It seemed desirable to retain the power of noting whether the whole table obeyed the same law or different parts of it behaved differently. Also we were anxious to simplify the calculations as far as possible, in order to appeal to a wider circle of readers. For these reasons, our criterion was based upon singling out from the table any pair of columns of coefficients. . . . Our criterion consists simply in the correlation between one column of figures and the other; it is the correlational coefficient between the two series of correlational coefficients; clearly this is just as easy to work out as between any other two series of values. It should be noted that this correlation between columns is quite independent of the arrangement in which the table happens to have been drawn up."

Also Spearman tells us that he threw away the two coefficients which had no corresponding coefficients in the other column. And then, a few pages further on, he says: "Such, then, is the statistical method which we have devised for deciding between the three rival theories. If the older view of Thorndike, viz., a general independence of all correlations, holds good, our correlation between columns of correlational coefficients should average about 0. If his newer view of "levels" or the almost universal belief in "types" is correct, then the mean correlation between columns should be a low minus value. If, finally, the true theory is that of a General Common Factor, the correlation between columns should be positive and very high."

Since Spearman's method has been applied to average raw coefficients it is highly desirable that the halves of a test from which the coefficients were derived measure substantially the same thing. Otherwise an average of the raw coefficients would be somewhat misleading. To this end, no test has been used which did not show a reliability coefficient of +.70. According to Table G this criterion climinates Arithmetic and Reading. Visual Vocabulary and Completion were combined, thus raising their reliability coefficient to +.69, which was accepted as satisfactory. The intercorrelations of the accepted tests are given in Table L. It is upon this table that we purpose to test the

Spearman theorem. The reliability criterion was set up and the correlation table was constructed before it ever occurred to the writer to enquire whether it would operate favorably or unfavorably to the "Common Factor."

Now. if Spearman's "unifocal" or "Common Factor" theory is

to be corroborated, the correlation between any two columns of Table L should be, to use his own words, "positive and very high." To be exact, Spearman says the average of all the correlations should be positive and very high. But Spearman himself would be the first to say that unless all parts of the table substantially agree, the use of an average would conceal rather than reveal the truth. He perceived this when he wrote: "It seemed desirable to retain the power of noting whether the whole table obeyed the same law or different parts of it behaved differently." It cannot be emphasized too strongly that, according to Spearman's statistical method, the crucial thing, in the last analysis, is not the size of the average; it is the size of the correlation between any two columns taken from the correlational table. Bearing this in mind, is the correlation between any two columns of Table L "positive and very high," or does it tend even to be "positive and very high"? Taking various pairs of perpendicular columns from Table L and correlating them we get such results as the following:

Cancelling 2 wi	th Visual Vocabulary + Completion	-95
Cancelling 3 w	ith Omnibus ith Teacher Rank	95
Cancelling S w	th Composite —	.91

Any one of the tests shown to the left paired with any one of the tests at the right would give similar coefficients to the above. The results are just exactly opposite to what is required to satisfy Spearman's theory. Instead of the coefficients being "positive and very high" they are negative and very high, What then led Spearman to believe in a Common Factor? The answer is given in the following:

Cancelling 2 with Cancelling 3 Omnibus with Visual Vocabulary + Completion	+1.00
--	-------

Many more such high positives could be given. Mere inspection of Table L will show that the correlation between any two columns from Cancelling 2 through Cancelling S would give a high positive. A high positive coefficient would also be gotten from any pair from Visual Vocabulary + Completion through Composite. On the other hand, the correlation of any column in the first group with any column in the second would be a high negative. What would the average be? A mistake!

Lest anyone should think that the coefficients from correlated columns always approximate unity, note the following smaller coefficients:

Handwriting with School Mark	56
Cancelling 2 with Copying Addresses Addition with Visual Vocabulary + Completion	.00 +.5I

Between 4-51 and --56 other intermediate coefficients could be given. By the proper selection of columns to be correlated, data could be found to support all of the three main theories, the "multifocal," the "faculty" or "type" or "level," and the "unifocal."

Objections will be urged against our correlational table (Table L). It could easily be said that Teacher Rank does not measure a mental trait at all, unless perhaps it be a mental trait of the teacher, and therefore such a measure should not be included in the table of correlations. It was retained because Dr. Spearman speaks of using "Imputed Intelligence" in his tables. But the omission of Teacher Rank would not change the general conclusion.

The only really important criticism would concern itself with the number of the Cancellation tests. Spearman would probably say that because of them our table is overloaded with "specific abilities." He himself combined two Cancellation tests which occurred in one of his tables, though he offered no justification for such a procedure, except that the tests were similar. If the tests were practically identical there could be no objection to his combining them. Likewise it would be difficult to protest had he elected to treat them separately, for they were not exactly the same test. If correlation be due to "specific ability" plus "Common Factor," we should not forget the work of Thorndike and Woodworth. They have shown experimentally that traits which seem almost identical may really not be so at all. If external similarity be our measure of "specific ability," the correlation between Cancelling A and Cancelling S would be higher

than between Visual Vocabulary — Completion and Omnibus. As a matter of fact, the correlation is +.57 in the first case and +.60 in the second. There is no more reason for combining these two Cancellation tests than for combining the Visual Vocabulary + Completion and Omnibus. But supposing we yield the point and retain only Cancellation 2 and Cancellation A, then the remaining columns can be correlated to give a result like the

But to be still more generous, we have thrown out every Cancellation test except Cancelling 2; yet we can get a result like this:

Cancelling 2 with Omnibus.....

In view of the foregoing we are forced to conclude that Speanan's theory does not have universal validity. And we have proved this by the application of his own statistical method. Dr. Spearman certainly bases his theory upon numerous data collected from many sources. His averages certainly were positive and high, and he explicitly states that no individual correlation of column with column fell appreciably below positive unity. Had we correlated every column in Table L with every other column and had we taken an average of all these correlations, the mean result would have been a substantial positive. But in view of the differential action of different parts of the table, such a summation would be not only misleading but wrong.

Dr. Spearman after advancing and defending his theory of the Common Factor proceeds to state the nature of it. Concerning the former, Burt writes: "The first of Dr. Spearman's propositions, the 'Theorem of the Universal Unity of the Intellective Function' is tested by a corollary logically issuing from it, called that of the 'Hierarchy of the Specific Intelligences.' Its principle may be most briefly expressed as follows:

$$\frac{r(A, P)}{r(B, P)} = \frac{r(A, Q)}{r(B, Q)}$$

where A, B, P, Q, represent any four capacities not obviously akin. When this formula is satisfied a correlational table can be so drawn up that the coefficients in horizontal columns grow

¹ British Journal of Psychology, Vol. III, p. 159.

smaller to the right and those in perpendicular columns grow smaller downward. Burt's coefficients did substantially satisfy the above formula, and when thrown into the usual table they formed a beautiful 'hierarchy.' Consequently, Burt agreed with Spearman's first theorem. The 'Common Factor' and the 'Hierarchy of the Specific Intelligences' must stand or fall together. Just as our results do not corroborate Spearman's contention, neither can our coefficients be so arranged as to show a hierarchy. Burt, like Spearman, claims that the above formula only holds when the capacities are 'not obviously akin.' This is the crucial point. We are insisting that external similarity is not a satisfactory measure of kinship. But even when we yielded to external similarity so far as to eliminate every Cancellation test except one, our results failed to substantiate Spearman's 'Common Factor' or Burt's 'Hierarchy of the Specific Intelligences.'

Complete fairness to Dr. Spearman makes another remark necessary. Spearman points out that what he calls "sampling errors" introduce a definite bias into the results obtained by correlating columns of coefficients, and that to determine the exact size of the coefficient this bias must be corrected for by a formula which he gives. In order that the correction may not be so great as to swamp the real difference, he sets up an arbitrary correctional standard by which he excludes those columns which have large sampling errors. Unfortunately, we have been unable to make clear to ourselves just how he applies this standard. hence our correlational table has been left unmodified. For this reason we do not correct our results by his formula but present them in their raw form. Anyway, the exact size of the coefficient is not necessary to test Spearman's theory. And even though Spearman finds that some column used by us did not quite satisfy his correctional standard, it is hardly conceivable that the sampling error could be so large as to completely reverse the direction of the coefficients upon which our conclusion is based.

In correlating two columns from a correlational table, two coefficients must be thrown away, one from each column. This is necessary because there will always be one coefficient in each column which lacks a corresponding coefficient in the other. But what is worse still is that every time a new pairing of columns is made different coefficients are eliminated. This increases enormously the labor of calculating the intercorrelation among the

66 Correlation of Psychological and Educational Measurements

columns, for with each new pairing a new average, a new set of deviations, and a new sum of deviations squared must be calculated. In calculating the Pearson coefficients for ordinary arrays

these things are done but once. To minimize labor, therefore, we suggest that the coefficient +1.00 be inserted at every place in the correlation table where there is a gap. An array will, of course, always correlate +1.00 with itself. This coefficient is usually omitted in drawing up a correlational table because to insert it would not be particularly illuminating. Where, however, we wish to apply Spearman's statistical method such an insertion would prove exceedingly serviceable. We did not use the +1.00 in calculating any of the coefficients used in our attempt to refute the two theories of Burt and Spearman. We believe that to fill up the gaps in a correlational table in this way is theoretically correct. In every case where we have tried correlating columns with and without the +1.00 the coefficient has been

very nearly the same. But even though the coefficients were not the same, the insertion of the +1.00 might still be justifiable. We merely mention it here in the hope that some one with sufficient training in the theory of correlation will test our suggestion.

CONCLUSION

The mere wording of a question may stimulate thinking which will result in experimental research. It is our only excuse for asking so many questions and giving a final answer to so few. Certain conclusions grow out of this study, but the amount of data in any one research is necessarily so meagre that universal validity can scarcely be claimed for any of them. But in view of the limitations of the study, the following seem to us worth a place in a summary:

- The corrected correlations among the educational and psychological tests and the functions which they measure continuously vary in size from --.63 to +-.08.
- a. Meaning by mental ability a Composite of all the measurements, the Omnibus and Completion tests correlate with it +Loo and +.96, respectively. That is to say, a perfect measure of an individual by Omnibus or Completion would be a substantially true index of his mental ability.
- 3. The seven best measures of mental ability together with their correlations with the Composite are: Omnibus 1.00, Completion .96, School Mark .91, Teacher Rank .86, Reading .81, Visual Vocabulary .80, and Arithmetic .72.
- Ranked in the order of their correlation with mental ability the complex educational and vocational tests come first, the relatively complex practice tests second, and the simple practice tests last.
- 5. The power tests, or those which measured the upper threshold of ability, showed a higher correlation with mental ability than the speed tests or those which measured how rapidly a relatively easy task could be accurately performed. The power tests were superior not only as to correlation but also as to time required and the distribution of that time.

68 Correlation of Psychological and Educational Measurements

- 6. The indications are that for a test to show a close correlation with mental ability it should emphasize power rather than speed and test a relatively complex function rather than a narrow mental trait.
- 7. Improvement at a speed, practice test was on the whole not so good an intellectual index as an average of the practice scores
- and not nearly so good an index as a single score from a complex, nower test. 8. In this particular 6 B school grade chronological age corre-
- lated negatively with mental ability. 9. The Cancellation tests correlated negatively not only with the Composite but also with all those tests which proved to be good measures of mental ability. This demonstrates that a nega-
- tive correlation between apparently desirable traits can exist. Heretofore, the weight of scientific evidence has been against such a possibility.
- 10. The correlation between columns of correlational coefficients does not corroborate Spearman's important "Theorem of the Universal Unity of Intellective Function."
- 11. In no way can a correlation table be so constructed from our coefficients as to satisfy Burt's "Hierarchy of the Specific Intelligences."
- 12. A suggestion was made whereby gaps in a table of coefficients can be filled. This suggestion, if justifiable, will greatly economize labor in applying to a table of coefficients Spearman's statistical method of correlating columns of correlational coefficients.

7 Y

BIBLIOGRAPHY

- BONSER (10). The Reasoning Ability of Children of the Fourth, Fifth and Sixth School Grades. Teachers College, Columbia University Contributions to Education, No. 37.
- Brown (11). Essentials of Mental Measurement. London, Cambridge University Press.
- Brown (13). The Effects of Observational Errors and Other Factors upon Correlation Coefficients in Psychology. Brit. Jour. Psy., Vol. 6, p. 223.
- Burt (09). Experimental Tests of General Intelligence. Brit. Jour. Psy., Vol. 3, p. 94.
- CHAPMAN (14). Individual Differences in Ability and Improvement and Their Correlations. Teachers College, Columbia University Contributions to Education, No. 63.
- HART and SPEARMANN (II). General Ability, Its Existence and Nature. Brit. Jour. Psy., Vol. 5, p. 51.
- HOLLINGWORTH (13). Correlation of Abilities as Affected by Practice. Jour. Ed. Psy., Sept., 1913.
- Kelley (14). Educational Guidance. Teachers College, Columbia University Contributions to Education, No. 71.
- SIMPSON (12). Correlation of Mental Abilities. Teachers College, Columbia University Contributions to Education, No. 53.
- Spearman (04). General Intelligence Objectively Determined and Measured. Amer. Jour. Psy., Vol. 15, p. 201.
- Spearman and Krueger (o6). Die Korrelation zwischen verschiedenen geistigen Leistungsfahigkeiten. Zeitschrift fur Psychologie, Bd. 44, s. 50.
- THORNDIKE and WOODWORTH (OI). The Influence of Improvement in One Mental Function upon the Efficiency of Other Functions. *Psy. Rev.*, Vol. 8, p. 247.

- 70 Correlation of Psychological and Educational Measurements
- THORNDIKE (09). The Relation of Accuracy in Sensory Discrimination to General Intelligence. Amer. Jour. Psy., Vol.
- 20, p. 364. THORNDIKE (13). An Introduction to the Theory of Mental and Social Measurements. Teachers College, Columbia University.
- THORNDIKE (13). Educational Psychology, Vol. III. Teachers College, Columbia University.
 - WHIPPLE (10). A Manual of Mental and Physical Tests. Baltimore, Warwick and York.

 WISSLER (01). The Correlation of Mental and Physical Tests,
- Wissler (oi). The Correlation of Mental and Physical Tests

 Psy. Rev., Monograph Supplement, No. 16.
- Fys. Rev., Monograph Supplement, No. 10.
 Wyart (13). The Quantitative Investigation of Higher Mental Processes. Brit. Jour. Psy., Vol. 6, p. 109.

VII

APPENDIX

GENERAL INSTRUCTIONS FOR THE SIX PRELIMINARY AND SIX FINAL TESTS:

I am going to give you several tests to find out how good a score you can make. Do your best in each test. To-morrow I shall read the names of the two making the highest total scores Notice carefully all instructions so you will not need to ask questions and thus disturb others. (Read before each series.)

Instructions for Visual Vocabulary, Reading, Completion, Arithmetic,
Omnibus and Proverb:

There will be placed before you, face down, a sheet of paper. This paper tells you what to do and how to do it. You will have go minntes in which to complete the test. When you have finished everything on the paper, bring it to me and return quietly to your seat. Don't look at your paper until I say "Go," and stop instantly when I say "Stop." Do what it says to have the says the says "Stop." Do what it says to have the says the say

(Read before each test) (Proverb: 15 min.)

INSTRUCTIONS FOR CANCELLATION:

You will be given a cancellation sheet. In this sheet a certain specified number or letter must be cancelled. Omit as few cases and cancel as many as you can in one minute. The sheet will be placed before you bottom-side up. When I say "Go," turn the sheet over and commence to cancel. When I asy "Sto," cease immediately. Your score will be as follows: 2 (number cancelled correctly) minus 2 (number wrongly marked). Watch while I show how it should be done and then you can practice at it yourself for one minute.

INSTRUCTIONS FOR ADDITION:

You will be given a sheet containing columns of one-place numbers. Place it before you hotton-side up. When I say "Co," turn the sheet over and begin adding. Write the sum of each column of ten figures under the line at the bottom of that column. Add as many columns as you can in ten minutes without making errors. If an answer is wrong you will receive no credit for that column. When you finish the examples on one sheet take another. Watch while I show you how it is done and then you can practice it yourself for five minutes.

INSTRUCTIONS FOR COPYING ADDRESSES:

You will be given a sheet containing 25 names and the directory from which these names were taken. Look in the directory for the first name

72 Correlation of Psychological and Educational Measurements

on your sheet, find the New York City address and write it after that name on your sheet. See how many of these addresses you can correct your open your sheet in ten minutes. Do not begin until I say "Go," and cease immediately when I say "Stop." Watch while I show you how it should be done.

INSTRUCTIONS FOR HANDWRITING:

There will be placed before you face downward a printed paragraph which you are to copy as much of a you can in four minutes. You will be scored for both quality and speed, so write as fast as you can while writing the best that you can. Be sure to punctuate and capitalize just as it is in the paragraph before you. Begin when I say "Go," and cease immediately when I say "Go," Watch while I show you how to do it.

Teachers College, Columbia University, publishes the Visual Vocabulary, Reading, and Completion tests. Further information concerning the other tests may be had by communicating with the author.

TABLE M

CANCELLING A: Original scores made in 1 minute by 88 children

CAN	CELLING	A:	Orig	ginal	scor	res n	nade	in I	mit	nute	by 8	8 ch	ildre	n
Ind.	2/4	2/5	2/8	2/9	2/10	2/11	2/15	2/16	2/17	2/18	4/14	4/15	4/16	4/19
1	18 32	44	38	48	48	72	56	62	64	60	80	90 48	78 60	84 70
1 2 3 4 5 6 7 8	16	38	32	40	32 44	48 54	38 45	46 50	56 68	48 62	44 54	48	74	74
4	20	24	40	48	52	54	54	58	60	63	56	58	74	74
6	20	36	4	4	40 18	48 80	46 45	50	60 45	70 52	64	66	70 80	78
7	28	32	36	52	44	56	60	70	66	76	60	48	68	62
8	34	56	36	38 58	40 74	74	42 74	48 76	50 88	54 88	50 70	68 92	74 98	69
10	26	30	30	36	36	48	48	63	44	34	40	44	52	64
11	28 28	32 58	40 58	38	46	54	52	63	53	=	60	69	84	85
12 13	74	44	48	74 64	78 66	78 74	68	68	90 68	88 74	74	74	86	92
14	20	36	48 76	54 74	64	68	64	62 92	68	76	62	100	80	46
15 16	60	51 24	48	46	96 42	100 62	100	92	97 72	94 61	92 76	100	98 80	100
17	- 4	22	24	34	30	38	44	58 34	46	38	26	40	40	40
18	38 22	38	36 32	48 36	50 42	56 52	52 80	54	68	66	60	72 60	72 62	62
20	24	36 28	38	30	34	38	46	54	60	58	52	52	74	54 68
20 21 22 23	32 32	34	42	48	50	58	66	48	66	74	52 60	52 76	76	68
22	26	28	32	44 50	54	62	48 51	38 46	56 62	62	66	44	64	60 54
24	44	40	50 52	56	64	68	70	74	84	98	62 88	50 44 96	93	-
25 26	40 24	34	50	58	52 52	74	56 74	72 70	61 76	66 70	74	74	76	74
27	28	40	28	50	56	60	72	72	76	72	76	88	88	96
28 29	24	24	25	34	26	38	46	42	62	56	Season.	40	66	80
30	32 22	36	36	40 28	52 32	62 36	68	70	78 48	48	64	68 50	88 54	52
31	26	20	30	32	38	38	28	40	44 54	44	44	48	50	
32 33	28 32	22 50	36	40 52	48	62	52 72	48	54	64	48	59	80	72
34	38	40	42	48	72 54	66	72	84	90	80	100	80	100	80
	16	28	26	34	38	34	38 38	48	52	44	52	54	64	48
36 37	16	30 58	28	30 76	40 76	96	38 84	10	20 96	52 100	46 92	54 100	70 102	64 116
38	22 22	28 24	32	44	40	18	38	40	52	44	48	44	60	52
39 40	22	24 16	28	24	32	42 20	38	42	50	52	52	68	72	70
41	38	38	44	40	48	50	56	50	52	54	48	54	68	68
42	10	arme.	48	34	50	68	62	-	52	64	66	94	92	98 76
43 44	38 36	38 72	68	60	54 74	60 74	76	54 76	66 86	70	68 94	66 S0	76 94	76 82
50	14	40	42	.50	56	58	62	62	58	66	70	78	88	104
51 52	34 10	32 22	28 34	40 30	44 34	56 36	52 24	68	56 36	24	38	64 38	68	56
53	28	34	46	40	40	48	50	64	20	38	36 54	66	62	84
54	0	34 51	64	72	60	100	84	72 42	59	70	60	68	64	44 64 70
55 56	2	30	34	36	44 58	50 62	38 52	56	50 72	56 74	42 68	44 74	34 62	56 64
57	28	34	40	44	44	50	46	46	48	52	58	46	50	52
58 59	38 12	38 24	52 28	56 24	53	68	89	68	80	84	74	86	91	96
66	16	32 20	24	36	34	48	38 50	52 42	54 68	62 56	50 48	56	48	58 46
61	28	20	40	50	44	52	68	56	64	88	52	-	42	88 80
62 63	24	44	42 52	42 48	48 52	60	60 74	50 74	72 74	80 66	66 78	68 70	80 94	80 68
64	34	40	44	40	48	50	40	56	47	54	ineter	50	54	58
65	38	42	14	40	32	12	36	48	58	66	68	66	74	60
66 67	18	26 26	18	24 34	26	48	44	46	50 48	48 62	44 52	46 62	52 72	58 66
63	-	22	32	30	30	_	_		44	52	48	50	52	56
69 70	20 38	36	36	48 48	48	54	34	-	_	-	-	-	Married	mun.
71	22	20	48	48	56 56	55	54 61	68	54 66	64 74	58 70	60 48	70 84	72 80
72	26	28	34	40	48	48	54	58	64	62	64	66	72	76
73	32 28	44 34	38 38	54 40	52 42	54	56 42	50	68	68	52 48	68	78 50	70 54
74														

74 Co	rrelati	on o	f Ps	ych	olog	ical	and	Edt	ıcat	iona	l M	easu	rem	ents
			(CANO	CELL	ING	A (c	ontin	ued)					
Ind.	2/4	2/5	2/8	2/9	2/10	2/11	2/15	2/16	2/17	2/18	4/14	4/15	4/16	4/19
75	32 24	59	48	72	74	90	94	92	94	96	90	100	102	102
76	24	28	34	40	52	64	55	60	64	68	51	62	68	50
77	34	40	48	42	52	58	54	46	68	63	72	68	74	10
78	34	30	36	33	40	48	42	40	46	98	46	46	40	40
79	-39	-58	-46	-42	-56	-45	54	-68	-93	-67	34	34	36	40
80	28	20	44	44	41	55	62	62	66	70	62	64	62	66
81	52 52	52	68	70	66	92	94	92	98	98	88	78	88	100
82	52	52	68	70	66	92	94	92	76	66	60	96	92	74
79 80 81 82 83	40	50	40	40	34	48	-	1 2	-	* ****	46	54	66	76
0.4	26	48	42	5.0	4.9	166	58	58	fi.e	6.5	70	86	82	82

			C	0 1 2 3 4 15 15 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19
40 41 42 43 44 50 51 52 53 54 55 55 57	31 32 33 34 35 36 37 38 39	25 26 27 28 29 30 31 32 33	Ind. 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 17 18 19 20 20 21 22 23 24	
			LLIN	28 52 40 36 28 28 22 24 36 40 34 28 40
52 -12 36 14 39 44 48 34 46 44 33 28 66 26	40 48 -22 50 36 52	58 46 80 62 60 34 34 48 48	2/11 50 48 24 52 38 -28 12 50 38 18 68 42 60 70 48 28 44 44 46 46	20 52 52 50 48 58 42 44 28 54 62 34 64
42 46 60 62 32 32 48 35 48 62 44	- 61 61 61	5 3 6 4 4 5 4	2// 5/4 4 3 3 5 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	44 68 68 49 42 56 40 28 30 64 36 36 56
	3	8 4 8 4	S 8 0 4 2 2 4 0 4 6 2 2 2 4 6 9 4 2 2 2 4 8 8 4 4 6 8 8 4	50 50 50 50 50 50 50 50 50 50 50 50 50 5
38 52 54 76 48 40 55 60 38 76	50 68 48 68	68 74 44 42 68 52 52 48 44	\$CO: 2/16	66 66 34 42 56 50 40 52 68 50 44 67
66 60 72 50 40 36 52 76 48	51 14 85 45 72	5654		55 92 48 66 62 60 50 68 78 56 38 64
		6 2 2 6 0	made 117 0 6 6 6 7 14 12 12 12 12 13 14 16 18 18 18 18 18 18 18 18 18 18 18 18 18	58 54 58 58 54 48 58 68 68 68
48 48 66 66 68 78 40 28 52 94	56 32 90 46 72	100 78 72 68 54 68 56 62 64 56	2/18 70 58 36 70 76 20 35 62 78 54 94 70 88 80 74 40 64 58 80 76 86	52 92 92 56 60 56 38 84 68 46 74
38 60 66 80 95 32 44 62 37 48 100 56	5. 21 81 44 84	8	4	66 76 68 53 48 74 60 46 74
	3	76 88 72 70 70 4	nute /14 72 72 65 65 68 68 68 66 66 68 67 78 88 70 70 70	70 98 66 68 64 711 50 84 82 64
58 88 70 72 100 65 46 72 68 44 44 64	70 22 94 66 88	76 72 70 68 76 66 70 72	by { 4/15 80 64 45 70 84 83 840 772 86 66 774 84 876 88 876 876	82 88 60 46 70 74 52 50 92 76 52 74
52 85 76 74 77 45 52 68 68 58 84 62	74 38 91 72 94	8 6 9 6 8 8	4	78 96 54 86 42 66 56 46 100 64 52 76
		0 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	ildr/16 22 38 44 4000 56 56 56 57 58 58 58 58 58 58 58 58 58 58 58 58 58	62 88 92 66 82 64 46 54 100 48 84
62 92 70 76 90 44 50 72 60 64 74 72	62 54 96 65 96	80 74 66 94 78 70 84 76	en. 4/19 92 65 65 72	100 74 76 82 56 72 — 58 — 104 —

			1	lppend	inx				7
Ind.	2/11	2/15	2/16	2/17	2/18	4/14	4/15	4/16	4/19
58	40	52	48	70	67	68	74	84	88
59	54	60	54	84	67 70	72	85	72	94
60	36	44	50	44	89	32	86 52	54	58 72
61	24	54	62	68	70	52 68 78	-	54 74	72
62	58	54 57	66	72	66	78	88	72	84
63	48	4.4	56	64	52 70 66 62	64	88 64	90	84 66 62 84
64	42	44 44 28 62	56	60	56	OT.	70	66	66
64	48	99	42	44	66	44	88	66 58	62
66	48	62	60	64	69	62	66 72	84	84
67	44	48	40	62	56 66 68	61	76	68	63 68
68				34	44	52	64	70	68
69	-	26		-	**	-	-		-
70	36	44	44	52	52	48	60	54 72	58
71	44	60	50	68	66	66	72	72	96
79	38	48	50	56	56	56	62	52	79
70	62	60	62	78		72	69	76	99
71 72 73 74	52	68 60 78	66	70	66 88 72 76	70	72 62 62 72 96	72	86 72 88 68
75	68	200	74	86	00	90	0.0	108	108 76 92
76	48	54	64	64	20	66	90	74	100
77	46	04	70	66	7.0	76	68 70	90	10
70	10	52 26	30	42	62	50		62	68
78 79 80	-80	-50	-60	46	50	46	58 58 57 74	62	60
19	60	-00	56	66	68	40	50	70	60
80	60	56 62 44	60	58	60	56 72	91	72 76	63 78
81	42 42	62	00	48	68 58	34	74	52	56
81 82 83 84	52	44	-			76	0.2	88	86
83	52	40	62	56	74	70	62 78 88 68	78	80
84				00	52	76 32	88		90 80
85			56	48	22	72	80	74	70
85 86 87	52	70	50	98	74	12	70	19	
87	46	50	58	64	68	52	88	66	
88 89	40	38	44	48	60	52	86	68	66
89	60	38 60 72	_	***	77	-	-	777	
90	72	72	82	80	96	100	96	92	102
91	72	78	90	84	88	90	88	27	-
92	44	-	52	60	60	60	70	64	77
93	52	44	52	64	_	64	64	72	68

76 77 78 79 80 81 83 83 84 85 85 86 87 88 90 91 92 92	48 46 -80 42 62 52 52 46 40 80 72 72 74 52	54 52 20 -50 56 62 44 40 -70 50 38 60 72 78 44	64 70 30 -60 56 60 	64 66 42 46 66 56 48 56 48 64 48 64 80 64	72 76 62 50 68 68 68 58 74 52 74 68 60 96 88 60	66 76 50 46 56 572 34 76 32 72 52 52 100 90 64	68 70 58 58 57 74 62 78 88 70 68 66 98 86 70 64	74 90 62 62 72 76 62 88 78 74 66 68 92 84 72	76 92 68 60 63 76 58 80 70 68 102
CANC	ELLING 2:	Original					CAST (CAS)		
Ind.	2/4	2/5	2/8 92	2/9 112	2/10	2/1	1	2/15 132 74	2/16 146 92 94 92
1 2	96 70	84 82 74	84		120 90 86 82 86	123 88 94 92 84		74	92
3	62	74	84 78 78	92 86	86	94			94
5	58 78	72 82	-	-	86	84		88 100	90
6		62	70	78		94		84	78
8	50 112 52 80 80 96		70 62	78 72 122	80 76 116 60 94 108 140 114 94 105 100 82 92 92			64 118 62 76 110 122 92 98 100 104 92 108 98 118 118 118 118 118	78 62 130 74 118 112 120 104 106 100 118
9	112	108	118	122	116	118 70 85 112 144 112 114 122 100 88 85 85 99 100 100 93 88 88		62	74
11	80	56 80	60 80	81	94	89		76	118
12	80	96 108 102 70	100	52 81 112 130 118 88 112	108	112		110	112
18	94	102	112	118	114	112		92	104
15	78	70	112 90 96 76 78 78	88	94	114		98	108
16	88	74 82	96 76	96	100	100		104	118
18	78 88 80 66 76 74 66	74	78	90	82	88		76	90
19	76	84	78	88 94	92	85		92	98
21	66	78 78 82	82 94	96 74	98	104		108	122
22	58 58 70 68 56 72 46	82 76	84 80	74	100	91		108	98 122 92 110 102 122 88 118 102 112 82 82
24	70	78	92	96	90	100		116	102
25	68	86 66	104 76	96 96 80 88 106 86	106	92		118	122
25	72	86	80	106	100	100		100	118
28	46	86 60	88	86	96	98		98	102
29	70 46	102 54	88	90 54 74	112	65		122 76 78	82
31	68 78	76	74	74	80	76		78	82
32	78 88	74	80	88 120 88	102 90 105 75 100 98 112 60 80 105 122	65 76 106 134 105 66		110 132	114 134
34	66 40	94 72	98 86	88	98	105		68	
35	40	61	60	64	64	96		68 96	100
1 2 3 4 4 5 6 7 7 8 8 9 9 111 11 11 11 11 11 11 11 11 11 11 1	52 62	56 74	84	64 80 94	94 104	10		114	66 100 110

Ind.	2/4	CAN 2/5	CELLLIN 2/8	G 2 (co:	ntinued) 2/10	2/11	2/15	2/16
	2/4						74	78
38	52 62 68	66	60 70	62 78	88 80	88 60	88	88
40	66	66	70	10	00	82	- 00	1000
41	58	88 78	64	74	68	78	88	82
42	60	-	94	92	92	104	-	-
43	70	82	74	96	88	96	96	96
44	84	100 122 28	114	104 130 88	112 126	128	124 126	112 144 32 60
50 51	102 30	122	126 48	130	44	134	120	199
52	50	44	50	54	58	60	52	60
52 53	2	4	4	12	12	28	28	28 152
54 55	138 78	128	126 92	130 82	12 136	138	146	152
55	78	74	92	82	86 122	92	94	96 128
56	-		74	98	122	116	126	128
57 58 59	18 70	80	74 92	60 98	46 98	100	50 106	84 100 86 90
50	48	56	68	74	78	68	78	100
60	54	58	78	88		90	90	90
61	70	94	100	122	88 108 92	84	92	0.4
62	84	82	94	100	108	110	118	94 120
63	62	80 70	78	100 88	92	84 84	84	96
64	62	70	78	88		84	96	98
65	88 52	100 50	94	100 80 118	98 84	78 78	82 88	100 84 134
67	102	98	70 104	110	112	114	128	84
68	104	46	58	68	70	114	140	109
69	76	80	printer.	90	-	-		
70	42	80 70 72 66	82	74	70	66	74	100
71	68	72	100 82	96	104	100	102 100	100
72	52	98	102	86	94	92	100	126
73	96 74	80	102	112 88	106 96	114 96	120	126
75	110	116	78 142	124	126	132	90 132	96
70 71 72 73 74 75 76	82	96	90	98	98	114	114	142
77 78	68	90	98	112	112	114	118	199
78	68	74	66	74	76	70	118 62 100	80
79	70	92	100	97	96	88	100	118
80 81	60	64 88	78	80 102 109	94	1000	98 122	122 122 80 118 102 130
82	76	84	94 104	102	100 100	116	122	130
82	106	90	96	100	78	110 88	96	-
83 84	92	88 114	122	80 100	110	124	104	134
85	96	72	-		-10	141	104	101
85 86	90	72 108 76 60	122	102	94	88	92	98
87 88	64	76	108	122 66	108	84	110	122
88	66	60	64	66	78	74	68 100 142 112	88
89	76 74	114 84	98	96	76	88	100	- 1
90 91	74	34	124 74	110 92	122 96	106	142	113
92	86 72	80	86	78	84	90	88	112
93	38	74	74	10	84	66	90	82

			CELLLIN					
Ind.	2/4	2/5	2/8	2/9	2/10	2/11	2/15	
38	52	66	60	62	88	88	74	
39	62	66	70	78	80	60	88	
40	66	88 78	64	74	68	82 78	88	
41	58	78	94	92	68	104	88	
43	70	82	74		92 88	96	96	
44	84	100	74 114	104	112	128	124	
50	102	100 122 28 44	126	104 130 88	112	124	126	
51	30	28	48	88	44	134 92	-	
52	50	44	50		58	60	52	
53	2		4	12	12	28 138	28	
54	138	128 74	126	130 82	136	138	146	
55	78	74	92	82	86 122	92	94	
56 57	18	60	74	98	46	116	126 50	
80	70	80	92	98	98	100	106	
58 59	48	56		74	78	ES	78	
60	54	58	78			90	90	
61 62 63	70	94	78 100 94	122 100 100 88	88 108 92	84	92	
62	84	82	94	100	108	84 110	116	
63	62 62 88	80		100	92	84	84	
	62	70	78	88	96	84	96	
6.5	88	100	94		98	78	82 88	
65 66 67	52 102	50 98	70 104	80 118	84 112	78	. 88	
68	102	46	58	66	70	114	128	
69	76	80	33	90	70	-	_	
70	42	70	82	74	70	66	74	
70 71	68	72	100	96	104	100	102	
72	52	66	82 102	86	94	92	100	
73	52 96	98	102	112	106	114	120	
74	74	80	78	88	96	96	90	
75	74 110 82 68	116	142	88 124	126	132	132	
76	82	96	90	98	98	114	114	
77	68	90	98	112 74	112	114	118	
72 73 74 75 76 77 78 79 80 81	70	74 92	100	97	76	70	62	
90	70	64	78	80	96 94	88	100	
91	60	88	04	100	100	116	98 122	
82	76 106 92	84	94 104	102 100	100 100 78	110	96	
83	106	88 114	96 122	80	78	88	50	
84	92	114	122	100	110	88 124	104	
82 83 84 85 86 87 88	95	72	20,000	-	1000	-	104	
86	90	108 76	122 106	102	94	88	92	
87	64	76	108	122	108	84	110	
88	66 76	60	64	66	78	74	68	
89	76	114	98	96	76	88	100	
90	74	84	124	110	122	106	142	
91 92	86 72	80	74 86	92 78	96	88	112	
93	38	74	74	18	84 84	90	88	
00	08	1.0	79	-	01	66	90	

Ind

4/20 154 96 114 94 116 92 84 140 84 142 104 104 104 104 132 104 132 104 132 104 4/21 170 102 110 88 112 92 162 158 82 120 124 96 120 114 96 120 114 4/23 178 112 138 100 116 168 188 130 122 120 106 88 132 132 144 122 121 106

4/23 4/28

> 128 108 96 108 132 130 100 112

100 112

110 116

120

136

146

80

116 114

132 76 110 106

104 172

114

CANCELLING 3: Original scores made in 1 minute by 88 children. Ind. 2/4 2/5 2/8 86 90 78 80 90 102

78

Ind

2/17 2/18

106 125 88 100 142 121 90 103

98 96 112 102

2/9 2/10

2/15

4/27

2/16

78 Corre	elation (of Psyc	hologic	al and	Educat	ional A	1easure	ments
Ind. 111111111111111111111111111111111111	2/4 60 20 110 20	0 f Ps ye 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	2/8 1707 1702 1702 1702 1702 1702 1702 1702	2/9 74 1198 21128 1155	E duc at 1 2/10 174 172 174 174 175 175 175 175 175 175 175 175 175 175	2/11 1004 1011 1011 1011 1011 1011 1011 1	2/15 132 132 133 135 135 135 135 136 138 138 138 138 138 138 138 138 138 138	2/16 102 132 146 146 146 146 146 146 146 147 148 148 148 148 148 148 148 148 148 148
65 66 67 68	150 68 128	88 130 64 126 74	126 92 124 84 136 82	104 94 140 74 128 82 96	90 100 124 96	114 100 124 96 140	110 102 104 136	126 104 126 118 150
69 70 71 72 73 74 75 76 77 78 80 81 82 83 84 84	88 70 70 80 102 136 92 114 78 92 66 100 92 136 132 138	108 92 118 80 120 84 128 118 138 108 108 102 80 78 122 140 128	118 94 122 92 130 108 144 85 132 90 122 125 104 138	84 125 104 132 92 138 118 152 84 118 100 122 122 128 124	87 84 120 94 128 104 132 120 132 130 104 123 116 96 138	94 123 104 138 90 134 130 144 106 136 132 105 152 120	100 98 118 118 128 107 140 138 158 84 122 108 135 126	102 122 126 134 116 144 152 164 112 110 122 136
86 87 88 89 90 91 92	136 104 54 100 116 112 106 60	114 158 70 102 114 96 92	114 138 64 128 124 116 100 78	116 120 76 108 138 124 94 96	108 122 76 112 124 120 106 106	120 140 84 122 132 124 124 98	132 80 114 134 134 104 112	110 128 88 — 140 138 106 128

CANCELLING 3 (continued)

		CA	NCELLIN	G 3 (con	tinued)			
Ind.	2/17	2/18	4/20	4/21	4/22	4/23	4/26	4/27
1 2	158	168	174	172	178	182	182	180
3	112 132	122 128	120	100 132	124	138	132	136
4	112	122	114	107	138 116	136	128 112	144 116
5	124	131	138	140	144	138	140	140
6 7	108	134 120	118	120	118	130	122	128
8	108	128	124	118	128	132	132	144
9	144	136	142	150	138	152	150	154
11	128	116	100	118 132	118	116 125	116 128	128 130
12	152	148	2000	****	3	200	162	140
13	156	164 118	172 136	160 132	172	176	176	184
15	148	128	140	140	142	128	128 164	136 154
18	132 128	128	146	118	138	142	144	142
18	114	124 108	118	130 166	122	126	124	128
19	112	116	108	98	112	112	108	128 124
20	136	136 132	132	140	144	148	158	148
22	110	106	134 122	130 108	140 128	138	110	150
23	124	138	118	132	134	132	132	155 130
24	124 148	132 140	130	126	132	138	144	136
20 21 22 23 24 25 26	112	110	110	120	122	132	118	126
27	116	116	124	136	138	144	140	134
28 29	128 128	138	138 168	136	134	142	138	150
30	96	108	102	148	142 110	94	148	148 122
31	105	108	100	108	120	122	126	118
32	128	124	136	132	148	142	158	170
34	144	200	150	140	144	142	134	142
35	100	102	112	116	132	128	134	132
36 37	104	148 138	136 134	132	140	130	138	158
38	102	98	120	112	108	118	126 122	128
39	118	120	124	116	128	126	132	128
40	106	98	110	98	108	112	108	100
42	118	126	124	110	128	124	136	140
43	120	118	128	124	120	126	124	120 156
44 50	146 150	142	152 148	132 162	138 158	148 172	136 176	156
51	40	46	68	78	70	96	104	176
52 53	70	72	84	82	74	90	84	86
54	140	162	26 156	30 172	46 176	169	146	30 142
55	118	128	124	116	122	133	138	138
56 57	148 72	154 88	142	162	154	164	-	-
58	124	130	104 126	102 128	116	126 134	112	110
59	126	132	132	136	148	160	144	130
60 61	110	96	100	104	122	116 101	128 112	114
62	144	150	134	140	142	134	142	108
63	122	124	138	142	152	150	150	162
64 65	122 126	114	98 120	-	118	122	126	118
66	112	128	122	122	136	136	142 138	132
67	1.50	150	148	160	172	172	168	168
68 69	90	98	100	102	112	124	108	122
70	104	114	104	120	116	123	116	124
71	136	116	122	128	138	136	-	142
72 73	128 128	132 136	128 136	133 138	136 142	142 146	142	150
74	124	122	-	122	130	120	148	150
75	136	148	146	165	158	168	156	152
76 77	154 170	138 178	136	132	134	144	148	160
78	114	108	120	196 128	126	183 132	190	200 126
79	142	140	-	138	130	148	152	154
80 81	114 136	122	114	130	126	134	128	142
	100	100	140	162	150	144	150	144

80 Correlation of Psychological and Educational Measurements

Ind.	2/17	2/18	4/20	4/21	4/22	4/23	4/26	4/27
82	142	132	142	150	144	164	172	153
83			132	126	138	118	84	28
84	164	162	162	177	150	182	186	-
85	-		162	177 76	160	104	120	120
86	94	112	122	132	134	110	142	134
87	132	136	126	140	144	146	148	142
82 83 84 85 86 87 88 89	104	106	88	116	112	124	124	118
89						-	-	-
90	119	138	142	176	176	163	174	162
91 92	150	144	132	162	138	138	150	128
92	116	120	108	114	116	112	120	128
93	118	-	116	124	118	128	-	140

89	104	100		-		112	121	121		110
90 91 92 93	119 150 116 118	135 144 120	11	12 32 38 16	176 162 114 124	176 138 116 118	163 138 112 128	174 150 120		162 128 128 140
Appr	TION: O	rigina1	scores	made	in 10	minut	es by	88 ch	ildrei	1.
Ind.	2/4	2/5	2/8	2/9	2/10	2/11	2/15	2/16	2/17	2/18
1 2 3 4 5 6 7 8	64 31 53 22 20	71 42 57 42 29 26 38	85 29 57 34	80	91 38 70 27 28 38 24 4 4 14 25 96 79 28 32 18 52 54 56 52 54	98 48 82	96	91	103	117
3	53	57	57	60	70	82	39 77 40 30 42 60 20 20 20 20 20 20 20 20 20 20 20 20 20	41 74 48 38	51 78 32 35 32 35 32 35 32 35 32 35 32 35 32 35 32 35 32 32 35 32 32 32 32 32 32 32 32 32 32 32 32 32	84
4	22	42	34	40	39	45 26 27 29	40	46	36	43
6		26	25	30	28	27	35	35	42	47
7	30	38	34	39	38		42	48	35	42
9	29	42	41	50	44	\$5	60	67	63	80
10	9	9	4	.8	.4	6	13	5	10	18
12	13	14	14	17	25	26	20	20	12	26
13	65	71	63	83	96	98	90	87	99	97
15	17	28	28	37	28	79	72	73	84	85
16	37	38	40	49	32	46	42	44	49	48
18	39	46	48	52	18 52	54	53	68	61	31
19	57	53	52	66	54	53	80	77	86	83
21	13	20	18	18	23	30	93	70 27	59	70
22	26	28	25 34 41 18 18 16 16 18 48 48 48 48 48 48 48 48 48 48 48 48 48	37		34	32	38	40	43
24	42	45	48	57	54	63	47	60	63	59
25	34	36	41	45	49	61	54	63	50	444 844 844 844 844 844 844 844 844 844
27	88	42	29	39	52	41	48	50	45	58
28	13	15	18	26	24	25	25	19	18	26
30	38	48		51	53	51	57	37 56	60	32
31	9	15	13 33 57 48 28 20 60 15 36	309 319 508 117 83 37 116 83 37 117 83 37 118 117 118 117 118 118 118 118 118 11	55 54 49 40 52 24 29 53 18 36 65 61 42 20 58 21	20	11	48 24 67 5 18 87 32 87 70 70 87 38 59 60 63 50 63 50 63 50 63 50 64 67 67 67 67 67 67 67 67 67 67 67 67 67	15	31
33	40	52	57	58	65	69	28 57	67	68	54
34	40	47	48	48	61	65	=	-	_	-
30	28	27	20	20	28	22	23	21	41	41
37	45	55	60	57	58	73	39 23 73 22 45	38 21 68 21 46	41 25 69 25 52	70
39	33	35	36	43	41	42	45	46	25	22
60	303 239 29 113 135 637 114 357 318 42 42 43 43 43 43 43 44 45 45 46 47 47 40 40 40 40 40 40 40 40 40 40 40 40 40	33	0.	-		45	27	-		
12	71	31	63	84	69	71	-	30	32 63 83 35 48 87 65	33
43	40	56	62	63	61	65	64	69	83	81
50	29	34	30	35	27	35	41	37	48	41
51	61	74	78	77	80	85	73	89	87	80
53	23	27	26	28	27	25	33	56		67
54	28	38	42	42	48	49	40	55	61	53
56		23	18	15	22	17	23	23	95	47
57	13	15	19	23	18	24	22	27	23	24
111 12 13 13 14 14 15 15 15 15 15 15 15 15 15 15 15 15 15	13 41 25 16	一位 9 18 14 17 17 22 28 18 44 28 29 22 28 44 44 45 28 28 18 18 18 18 18 18 18 18 18 18 18 18 18	25 63 62 22 30 78 54 25 42 33 18 19 54 36 15	22 84 63 29 35 77 59 28 42 38 42 38 15 52 32 32 42 23 52 24 25 29 29 29 29 20 20 20 20 20 20 20 20 20 20 20 20 20	30 69 61 26 27 80 83 27 46 37 22 18 50 38 12 25 28	62026687709662775555933445556361444125351209666542227321242445337755585644522464533775558564558564525666666666666666666666666	64 30 41 73 59 33 40 37 22 24 31 33 33 35	69 32 37 89 56 28 55 39 23 27 67 43 25 34 86 23	61 45 27 23 69 38 23 28 94 24	70
50 NT	16	20	15	24	12	21	24	25	23	27
52 53	21 52 22	74	20 74 34	76	86	51	83	86	28	41 23 70 22 25 57 33 66 81 41 51 51 53 47 24 70 25 27 29 99
53	22	21	34	29	28	29	35	23	24	94

				11						
Ind. 64 65 65 66 67 77 77 77 78 80 81 82 83 83 85 85 85 85 85 85 85 85 85 85 85 85 85	2/4 29 30 34 	2/5 25 47 35 45 46 48 79 19 19 18 48 29 19 19 18 42 29 29 29 29 29 29 29 29 29 20 20 20 20 20 20 20 20 20 20 20 20 20	2/8 31 49 39 54 46 81 31 32 45 45 46 81 31 32 45 46 46 40 35 41 41 41 41 41 41 41 41 41 41 41 41 41	2/9 27 25 48 40 21 48 80 37 12 25 48 80 37 14 22 45 67 86 69 42 43 35 15 15 15 16 16 16 16 17 18 18 18 18 18 18 18 18 18 18 18 18 18	2/10 24 22 25 51 36 47 ——————————————————————————————————	2/11 25 29 51 42 ———————————————————————————————————	2/15 31 25 51 42 37 29 48 88 33 16 41 51 67 92 45 ———————————————————————————————————	2/16 34 21 25 59 60 60 60 60 60 60 60 60 60 60 60 60 60	2/17/ 28/ 27/ 61/ 44/ 35/ 35/ 35/ 26/ 25/ 49/ 27/ 94/ 49/ 27/ 94/ 45/ 40/ 40/ 40/ 40/ 40/ 40/ 40/ 40/ 40/ 40	2/18 42 42 49 49 57 57 103 48 27 27 27 26 26 26 27 27 27 27 27 27 27 27 27 27 27 27 27
30 Ind. 1 1 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	31	4/14 1118 39 77 82 22 22 22 22 22 23 44 44 44 44 44 44 44 44 44 44 44 44 44	119 1 63 2 2 2 4 1 4 8 2 4 5 1 1 1 2 5 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	118 45 45 45 45 45 45 45 45 45 45 45 45 45	1/19 110 110 110 110 110 110 110 110 110 1	4/202 4/202 4/202 4/202 8151 8151 8233 8351 9991 144 9983 8351 9991 144 1577 777 777 888 861 161 161 161 161 161 161 161 161	4/23 4/23 4/23 4/23 4/23 4/23 4/23 4/23	4/2/2/2/2/2/2/2/2/2/2/2/2/2/2/2/2/2/2/2	100000000000000000000000000000000000000	4/27 131 235 777 40 440 440 452 88 80 14 222 113 914 577 110 228 77 120 237 120 247 120 257 66 78 27 27 28 27 28 27 28 27 28 27 28 46 30 81 31 55 57 66 59 59 59 59 59 59 59 59 59 59 59 59 59

Appendix

81

			ADD	ITION	(conti					
Ind.	4/14	4/	15	4/16	4/19	4/20	4,	/23	4/26	4/27
	98		04	102	91	92		103	93	106
51 52	_					100		-	_	=
53	28		37	31	41 51	35	6	-		35 72 48
54	53		51	57	51	55	Ę.	70	63 40	42
55	35		35	37	31 28	42		49	40	40
56	25		25	27		82		30	22	20
57	28 53 35 25 20 71 51 27 25 85		51 35 25 18 70 47 29	31 57 37 27 24 82 38 25 61 93 42 35 32 64	75	56 42 32 27 77 55 29 24 101 31 32 32 66 64	3	30 22 89 59	22 80 56 35 31 118 25 41 29 64	30 87 60 24 26 121 32 24 23 74 73 72
88	71		70	82	10	66	9	50	56	60
60	97		99	95	43 26 26 97	20	ii .	30 33 110 35 35	35	24
61	25			61	26	25	3	33	31	26
62	85		98	9.3	97	101		110	118	121
63	30		33	42	26	31		35	25	32
64			25	35	16	32	0	35	41	24
65	27		98 33 25 31 57 58	32	28 16 57 57	32			29	23
66	60		57	64	57	66	9	60	55	72
67	27 60 49 57			52 65	54 59	04		65 59 56	66	70
68			-		99	09		-		- 25
53 4 5 6 6 7 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	319 85 49 27 59 20 41 87 98 81 45 22 21 26 33		32 48 88 45 23 31 61 23 39	33	81	33		38	31	38
71	39		48	49	40	48		38 47 100 54 35 36 64 25 39 108 120 76 51	_	51
72	85		88	81 48	40 78 45 24 24 48 20 34 80 98 64 24 37 28 17	48 97		100	97	103
73	40		45	43	45	49	6 '	54	47 39 38 61 33 51	54
74	24		23		24	31 33 50 17 39		35	39	42
75	27		31	31 57 19	24	33		36	38	28
78	59		61	57	48	50		64	61	88
27	20		23	19	20	17		20	51	32
78	91		89	0.4	90			109	105	103
90	0.0		00 07	102	98	108		120	105 120	122
81	61		72	38 94 102 72 47	64	108 71 54		76	68	78
82	45		45	47	54	54		51	68 54	56
83	22		42		24	40 46 28 19		42		37
84	41		46	43	37	46		48	44	39
85	26		30	20	28	28		45	44 35 23	41
85	16		25	32		19		22	23	20
81	27		88 97 72 45 42 46 30 25 32	31	33	25 38		42 48 45 22 35 39	31 34	38 51 103 54 42 28 86 32 45 103 122 73 35 66 37 39 41 20 44 43 1
90			01	91	00	40		0.0	01	
90	62		62	73	69	68		56	73	93 58 58 56
91	62 38		49	-	-	42		53 50	52	58
92 93	44		54	58	45	47 61		50	51	58
	38		43	52				65	_	
COPYING	ADDRE	SSES:	Orig	inal s	cores 1	made i	n 10	minu	ites by	88 chi
ren.										
Ind.	2/19	2/23	2/24	2/25	2/26	3/1	3/2	3/3	3/4	3/5
1	7	10	19	18	18	16	17	17	19	15
2	7 15 3	19	13	21	18 22 14	21	18	_	22	28
3	3		10	17	14	16 21 16 15	16	17	18	18
1 2 3 4	10	10	19 13 10 14	18 21 17 17	13	15	17 18 16 13	11	22 18 14	15 28 18 15

	89 90 91 92 93	62 38 44 38		62 49 54 43	73 58 52	65		68 42 47 61	56 53 50 65	73 52 51	93 58 58 56	
	COPYING	ADDRE	SSES:	Orig	inal	scores	made	in 10	minu	tes by	88 chil	-
ire	n.											
	Ind.	2/19	2/23	2/24	2/2	5 2/26	3/1	3/2	3/3	3/4	3/5	
	1	7 15	10	19	18	18 22	16	17	17	19	15	
	1 2 3	15	19	13	21	22	21	18	-	22	28	
	3	3	9	10	17	14	16	16	17	18	18	
	5	10	10	14	17	13	15	13	11	14	15	
	5	16	18	19	24	22	-	23	21	22	24	
	6 7 8	3	7	7 5 17 17	9	11	11	16	-	6	11	
	7	1	8	5	11	13	15	8	12	14	20	
	8	13 13	14 19	17	20 21	20 18	20	15	20	23 22	25 26	
		13	19	17	21	18	20	14	16	22	26	
	10	9 5 5	11	10	12	16 22	13	10	19	12	17	
	11	5	11	14	1	22	23	17	25	25	28	
	12	- 5	11		16	15	14	10	16	12	19	
	13	15	21	25	23	20	25	22	26	25	29	
	14	12	12	9 9 15 11	14	14	13	18	17	13	15	
	15	9 11	.8 10	9	15	16	18	15	17	13	24	
	16	11	10	15	16	19	18	17	21	19	24	
	17	13	12	11	17	17	19	9	15	16	18	
	18	13	14	14	24	22	25	19	19	23	28	
	19	5	13	11	16	18	18	15	16	18	23	
	20	11	16	33	19	20	17	20	17	23	23	
	21 22	9	12	9 12 8 19	12	12	15	15	13	8	12	
	22	11	5 12	12	17	16	14	18	15	15	24 22 25	
	23	11	12	8	-	14	21	16	17	13	22	
	24	17	19	19	24	24	23 18	20	23	25 17	25	
	25	15	15	17	18	23	18	19	21	17	24	
	25 27 27 27 27	12	13	17	20	18	21	18	19	18	20	
	27	15	17	20	25	25	26	26	29	31	29	
	28	9	11	10	14	14	13	16	18	13	19	
	20	15	20	20	27	22	21	26	24	26	29	

Ind.

Ind

 $84 \quad \textit{Correlation of Psychological and Educational Measurements}$

		Co	PYING	ADDR	ESSES	(conti	nued)			
Ind. 17 18 19 20 21 22 23 24 25	4/14 19 26 21 23 18 24 21 30	4/15 17 27 20 22 16 24 23 27	4/16 19 25 13 26 17 18 20 29	14/9 17 26 18 27 14 18 19	4/20 19 22 21 24 18 21 21 29	4/21 20 26 22 28 17 16 22 32	4/22 19 28 24 31 16 22 25 34	4/23 — 31 21 25 17 — 26 35	4/28 24 31 28 33 16 28 25 36	4/27 22 32 27 29 18 27 25 38
19 20 21 22 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38	20 29 27 24 18 30 17	26 27 18 30 26 19 28 20	24 35 19 29 30 20 28 19	24 32 24 22 26 15 18	23 32 21 30 29 20 24 20	24 36 21 36 27 19 27	27 37 19 37 27 19 27 27 21	29 37 28 31 31 25 28 21	28 39 25 34 32 24 33 22	28 35 19 39 32 22 21 17
35 36 37 38 39	22 19 25 16 17	26 18 23 15 23	23 15 23 15 21	27 14 23 14 20	20 20 24 19 22	25 21 24 19 22	25 23 25 18 20	29 23 20 22	31 24 25 20 26	28 24 21 22 26
60 41 42 43 44 50 51 52 53 53 53 54 55 56 60 60 61 62 63 64 65 66 67 77 71 72 73 74 75	200 314 1420 200 338 68 68 53 25 20 71 51 51 25 85 85 25 25 27 27 25 85 85 87 87 88 88 88 88 88 88 88 88 88 88 88	20 29 17 22 28 26 29 51 35 25 18 47 29 98 33 25 31 57 61	19 32 18 20 34 28 25 21 18 25 27 21 17 21 14 18 18 18 25 27 27 21 27 21 27 27 27 27 27 27 27 27 27 27 27 27 27	17 30 15 20 25 22 17 25 22 18 23 14 28 15 18 19 29 20 20 21 21 21 22 23 23 24 23 24 25 22 23 24 25 26 27 27 28 28 28 28 28 28 28 28 28 28 28 28 28	20 333 211 223 221 244 244 223 200 223 233 155 215 216 217 218 218 219 219 219 219 219 219 219 219 219 219	23 34 177 22 22 29 18 23 24 27 27 21 26 15 20 16 31 31 31 31 32 20 21 21 22 20 21 21 22 21 22 21 22 21 22 21 22 21 21	222 37 21 23 25 25 21 34 24 20 30 25 21 18 30 25 21 29 20 25 21 21 22 20 21 21 21 21 21 21 21 21 21 21 21 21 21	21 34 24 23 30 26 20 29 20 30 22 29 25 23 18 25 25 25 25 25 25 25 25 25 25 25 25 25	24 38 24 25 34 27 22 28 18 20 36 23 22 17 29 23 28 19 21 30 24	18 32 21 27 34 30 19 31 24 27 28 21 17 24 24 24 27
09 70 71 72 73 74 75 76 777 78 80 81 82 83 84 85 80 90 91 92 93	31 30 88 40 224 25 27 25 20 20 41 81 81 22 24 41 26 33 27 —————————————————————————————————	32 48 88 45 23 31 23 29 97 45 45 46 30 30 31 45 46 30 31 46 46 31 46 46 46 46 46 46 46 46 46 46 46 46 46	25 17 21 18 21 29 24 21 27 23 27 20 19 16 20 16 23 24 27	235 211 114 188 233 223 233 199 235 247 247 247 247 247 247 247 247 247 247	26 28 21 22 32 32 26 23 36 25 25 19 25 117 14 22 22 23 22 25 25 25 25 25 25 25 25 25 25 25 25	25 20 26 18 19 22 28 26 22 23 26 40 30 24 40 14 17 34 25 25 22 23 26 22 23 26 26 27 28 28 28 28 28 28 28 28 28 28 28 28 28	24 24 24 22 24 28 26 27 27 24 31 29 28 23 25 23 25 23 25 23 25 25 25 25 25 25 25 25 25 25 25 25 25	277 281 285 282 280 287 287 288 297 311 238 238 239 231 231 231 231 232 232 233 233 242 262 277	21 29 19 21 31 38 29 28 27 32 40 29 30 24 20 22 22 23 21 31 24 25	30 223 27 22 23 28 26 25 30 26 31 30 30 30 28 22 21 24 24 25 25 25 25 25 25 26 26 27 28 28 28 28 28 28 28 28 28 28 28 28 28

				Apper	ıdix					85
HANDW	RITING:	Origin	al scor	es ma	le in 4	minut	es by 8	8 child	iren.	
Ind.	2/19		2/23		2/24		2/25		2/26	71
1 2 3 4 5 6 6 7 7 8 9 9 100 111 123 145 187 189 222 223 224 225 226 227 228 229 229 229 229 229 229 229 229 229	63 87 83 86 86 86 88 88 88 88 88 88 88	70 80 81 81 81 81 81 81 81 81 81 81 81 82 83 84 85 86 87 87 87 87 87 87 87 87 87 87 87 87 87	62 80 78 88 79 77 79 56 62 160 88 81 54 65 76 60 77 72 74 63 75 75 75 75 75 75 75 75 75 75 75 75 75	56 771 65 65 67 67 68 67 68 68 68 68 68 68 68 68 68 68 68 68 68	63 72 77 77 65 65 65 78 65 65 65 65 65 65 65 65 65 65 65 65 65	59 72 86 67 67 72 55 38 67 47 47 64 66 65 59 59 59 59 59 59 59 59 59 59 59 59 59	78 92 72 72 75 75 75 75 75 75 75 75 75 75 75 75 75	71 888 80 67 61 61 61 80 80 72 80 80 80 80 80 80 80 80 80 80 80 80 80	055 751 605 655 655 655 655 655 655 655 655 655	75
34 35 36 37 38 39	70 101 78 51 68	61 89 96 46 74	70 75 70 54 58	61 69 63 43 56	72 73 73 50 53	68 72 61 48 57	74 65 70 51 53	78 69 72 48 66	76 75 54 52 68	76 75 61 50 71
331 332 333 344 355 367 369 401 414 424 434 434 434 434 434 434 43	83 101 73 69 92 79 69 85 69 71 69 80 71 81 93 93 93 94 95 95 95 95 95 95 95 95 95 95 95 95 95	81 86 81 75 86 75 54 75 89 87 85 85 85 85 85 85 85 85 85 85 85 85 85	81 79 68 92 84 85 78 90 60 65 75 66 51 74 61 75 79 98 82	75 60 68 76 61 61 61 61 61 61 61 61 61 61 61 61 61	775 69 88 777 76 94 60 60 60 60 60 60 60 60 60 60 60 60 60	42 77 78 75 75 75 80 80 84 86 85 75 66 87 88 84 86 85 84 86 86 86 86 86 86 86 86 86 86 86 86 86	75 67 95 83 87 95 87 97 93 86 89 84 82 83 75 62 71 76 83 75	83 86 76 97 67 60 84 71 75 102 47 70 67 67 67 88 89 99 99	89 88 71 80 61 64 65 80 45 70 74 70 74 75 74	98877 977 8 6 6 77 8 8 6 6 77 8 8 8 6 6 77 8 8 8 8
68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84	82 66 68 75 84 74 85 98 72 68 84 95 95 89 80 —	75 67 68 75 79 74 79 104 66 65 83 93 100 73 —	70 87 64 76 69 78 89 70 56 75 79 98 84 71 78	64 64 68 68 68 65 66 92 60 62 82 82 76 63 72	73 58 70 74 53 80 87 72 54 68 69 95 71	59 58 68 72 45 72 82 73 51 77 70 98 75 69	79 68 73 72 73 76 74 64 48 78 88 104 83 69 51	76 69 83 80 81 95 93 75 69 79 93 100 79 82 80	72 48 66 69 72 80 101 61 61 75 90 79 63	1

T. J. sational Management

86	Corre	latio	n of P		logical				Meası	iremei	its
					WRITING					1010	
Ir		2)	19	2/2	23	2/	24	2/2	25	59	
8888	3	86 73 58	85 78 54	72 76 65	76 80 48	73 76 56	61 64 51	70 42 64	72 70 54	65 50 59	67 72 57 70 89 79 89
888888888888888888888888888888888888888		70 91 84 79	58 89 80 71	84 75 75 78	76 73 76 63	84 64 78 79	75 66 78 72	63 86 85 75	57 83 79 80	81 74 89	89 79 89
I	ad.		/1		/2	3/		3,		3,	
	1233453773990122345567899012234556789901223	69 637 64 559 59 64 66 66 66 66 66 66 66 66 66 66 66 66	63 65 62 61 59 68 51 43 56 77 83 62 63 63 63 63 63 63 63 63 63 63 63 63 63	59 72 96 64 83 55 73 58 64 10 41 65 65 66 63 65 66 67 70 64 68 67 70 64 68 67 70 64 68 67 70 64 68 67 70 70 70 70 70 70 70 70 70 70 70 70 70	64 777 78 66 66 67 77 85 66 66 67 77 67 67 67 67 67 68 69 69 69 69 69 69 69 69 69 69 69 69 69	66 — 621 69 — 65 48 74 59 55 77 59 62 49 68 69 58 58 22 — 77 77 71 64 95 55	64 - 06 00 70 - 1710 675 585 68 79 17 1810 675 68 00 77 77 77 70 675 68 77 77 70 50 77 78 51 1 - 0976 55 44 59 - 1575 58 56 55 56 56 56 56 56 57 77 68 57 77 77 78 51 77 78 51 77 78 51 77 78 51 78 78 78 78 78 78 78 78 78 78 78 78 78	61 73 58 68 59 44 45 55 56 57 56 58 57 56 58 57 58 58 58 58 58 58 58 58 58 58 58 58 58	575 577 584 586 581 585 586 586 587 586 587 587 587 587 587 587 587 587 587 587	59 57 75 97 75 56 56 52 57 57 57 56 52 54 55 55 57 56 56 56 56 57 56 56 56 56 56 56 56 56 56 56 56 56 56	69 65 68 68 68 68 68 68 68 68 68 68 68 68 68
3333333	5	75 81 55 49 69	74 78 62 45 71	72 70 64 48 57	78 85 80 50 70	77 77 61 49 55	90 78 65 44 59	68 82 64 51 61	59 74 72 46 56	67 85 73 54 56	69 79 87 57 64
444455555555556666666666666666666666666	2	775 7270 7280 555 557 558 558 558 613 627 688 613 757 757	75577688962576876896251787768996277687768996277687768996277687768996277689962776899776997709977699776997769977699776997769977699776997769977699776997700000000	78 67 40 79 53 55 49 66 54 10 22 68 68 68 68 68 68 68 68 68 68 68 68 68	78 84 39 75 76 56 87 74 55 100 50 53 83 83 65 51 77 77 58 83 83 83 83 83 83 84 85 85 86 86 86 87 87 87 87 87 87 87 87 87 87 87 87 87	62 445 4173 818 55 55 61 62 94 41 70 63 65 55 61 62 63 65 65 66 65 66 66 66 66 66 66 66 66 66	67 55 56 95 69 60 65 71 55 100 71 63 65 47 77 71	75 66 74 74 74 43 50 62 67 59 104 45 69 84 71 50 84 71 50 84 72 87 87 87 87 87 87 87 87 87 87 87 87 87	69 68 71 69 93 64 46 59 67 49 90 39 62 65 56 57 2 48 72 48 72 48 72 48 72 48 72 72 72 72 72 72 72 72 72 72 72 72 72	55 62 68 62 65 65 67 71 61 63 33 67 50 50 50 50 50 50 50 50 50 50 50 50 50	69 79 87 64 60 76 76 69 69 73 73 74 73 73 74 75 77 75 77 77 78 78 78 78 78 78 78 78 78 78 78

3/2

3/1

3/3 80 91

3/4

87

3/5



VITA

WILLIAM ANDERSON McCall. Born, Wellsville, Tennessee, 1801.

Educational Record: Cumberland College, Williamsburg, Kentucky, 1907-11, B.S. 1911. Part-time student, Lincoln Memorial University, Harrogate, Tennessee, 1911-13, A.B. 1913. Teachers College, Columbia University, 1913-16; Research Scholar in Education, 1914-15; A.M. and Master's Diploma in Education, 1914.

Professional Record: Instructor in Psychology, Lincoln Memorial University, 1911-13. Psychological Investigator for the New York State Commission on Ventilation, 1914-16. Lecture in Educational Psychology, Columbia University, 1915.

Previous Publications: A monograph: "Ventilation in Relation to Mental Work," Columbia University Contributions to Education, Teachers College Series, written in collaboration with Dr. J. C. Chapman and Dr. E. L. Thorndike.

"The Effects of Outside Air and Recirculated Air upon the Intellectual Achievement and Improvement," School and Society, Vol. III, No. 71; with E. L. Thorndike and G. J. Ruger.









