Evidence for decay of spin waves above the pseudogap of underdoped YBa$_2$Cu$_3$O$_{6.35}$


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The magnetic spectrum at high energies in heavily underdoped YBa$_2$Cu$_3$O$_{6.35}$ ($T_c=18$ K) has been determined throughout the Brillouin zone. At low energy, the scattering forms a cone of spin excitations emanating from the antiferromagnetic (0.5,0.5) wave vector with an acoustic velocity similar to that of insulating cuprates. At high-energy transfers, below the maximum energy of 270 meV at (0.5,0), we observe zone-boundary dispersion much larger and spectral weight loss more extensive than in insulating antiferromagnets. Moreover, we report phenomena not found in insulators, an overall lowering of the zone-boundary energies and a large damping of ~100 meV of the spin excitations at high energies. The energy above which the damping occurs coincides approximately with the gap determined from transport measurements. We propose that as the energy is raised, the spin excitations encounter an extra channel of decay into particle-hole pairs of a continuum that we associate with the pseudogap.

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In high-temperature superconductors, there is a close relationship between the carrier density, the magnetic ordering and excitations, and the unusual $d$-wave pairing.\cite{1-4} The superconducting phase first appears when the concentration of carriers is about 5.5% and this small concentration of defects is also able to destroy the long-range antiferromagnetic order. One of the most surprising results in the underdoped region of the phase diagram is the occurrence of a marked decrease in the charge scattering rate of the optical conductivity below the surmised pseudogap energy.\cite{5} The pseudogap energy decreases with increasing doping and its origin is controversial with many models and theories proposed.\cite{6-10} Understanding underdoped high-temperature superconductors clearly requires an understanding of this pseudogap, and more generally, of how the antiferromagnetic Mott insulator becomes a superconductor for such small doping.

YBa$_2$Cu$_3$O$_{6.35}$ (YBCO$_{6.35}$ with $x=0.35$) is a superconductor ($T_c=18$ K) with a planar hole doping of about 6%. Low-energy neutron scattering has shown that at this doping, there is strong quasielastic scattering, showing the existence of commensurate antiferromagnetic short-range order, and that there is no well-defined resonant mode.\cite{11} In contrast, in YBCO$_{6.5}$ and for similar hole doping, with $T_c=59$ K and a doping of 9%, the commensurate quasielastic peak is replaced by incommensurate excitations for energies less than a resonance at 33 meV, where the excitations become commensurate at the antiferromagnetic zone center (0.5,0.5) in units of $2\pi/a$.\cite{12-17} Since both these materials are superconducting, it follows that none of these low-energy properties of the magnetism are essential for the occurrence of superconductivity. This Brief Report represents an observation by a direct spectroscopic probe of the destruction of spins by the pseudogap states and reveals an energy range where this onset occurs. Based on a comparison to cuprates in the over-doped region of the phase diagram, we propose that this decay of spin excitations is a common feature in all cuprate high-temperature superconductors.

To date, there are very few measurements of the spin excitations at energies comparable to the zone-boundary excitations at about 2$J$ in the parent antiferromagnetic insulators and none exists for the heavily underdoped superconducting materials.\cite{18-20} We report neutron-scattering measurements in this region for YBCO$_{6.35}$. We compare the results with those obtained for insulating two-dimensional antiferromagnets and show that the low-energy magnetic excitations are very similar. The high-energy excitations are very different and exhibit strong damping and reduced spectral weight near the magnetic zone boundary. These properties are characteristic of the dispersion curve entering a continuum of excitations as found in magnetic metals and low dimensional materials. We suggest that the continuum is associated with the pseudogap states and the large damping occurs when the energy of the magnetic excitations is larger than the pseudogap.

The sample consisted of seven twinned crystals with a total volume of ~7 cm$^3$ aligned with a combined rocking curve width of ~2° and such that Bragg reflections (HHL) lie within the horizontal plane. The orthorhombic lattice parameters of the crystals were $a=3.843$ Å, $b=3.871$ Å, and $c=11.788$ Å. The measurements were performed at high energies using the MAPS time-of-flight spectrometer at the ISIS facility. A Fermi chopper was spun at 400 Hz and monochromated the incident beam with energies of 150, 310, and 450 meV. The effective resolution was selected by combining pixels and time channels using the MSLICE program.\cite{21} Typically, the energy integration was chosen to be 10–30 meV (full width at half maximum) while the integration in wave-vector transfer was between 0.025 and 0.1 reciprocal lattice units in the two-dimensional plane.
In Fig. 1, we show constant energy slices through the intensity distribution of magnetic neutron scattering for incident energies of 310 and 450 meV. The colored contour plots show how the scattering depends on wave-vector transfer in the two-dimensional CuO₂ plane. In Fig. 1, the incident neutron beam was parallel to the c axis and the results have been symmetrized to take into account the intensity arising at equivalent wave-vector transfers. At low energies, the scattering is confined to a small circular disk centered on the antiferromagnetic Brillouin zone center, $H_{\text{BZC}} = (0.5, 0.5)$. With increasing energy, the size of the circle increases and the center is depleted so as to form a ring whose diameter increases linearly with energy. Above $E_i = 200$ meV, the pattern becomes more complicated with the scattering intensity displaced towards the zone boundaries. In Fig. 2, we show a series of cuts through the data either to give constant energy scans or to give constant wave-vector scans through the data so as to obtain the dispersion from the antiferromagnetic peak position at $(0.5, 0.5)$, as shown in Fig. 4.

To extract the energy dependence of the acoustic and the optic spectral weight, we varied the angle $\phi$, defined as the angle between the incident beam and the [001] axis, with the rotation axis along [110]. With the incident energy fixed at 150 meV and angles of $\phi=0$, 20, and 30, the variation in the intensity with $L$ enables the optic and acoustic components to be separated by Fourier analysis knowing the bilayer spacing $d/c=0.28$. This is the same analysis and method applied previously to the YBCO$_{6.5}$ superconductor.\(^{16}\) As shown in Fig. 3(c), at low energies below 40 meV, all the scattering occurs in the acoustic channel. At higher energies, the optic mode intensity increases, and at 75 meV, it is larger than the acoustic mode intensity, as shown by the reversal of the maxima and minima compared with the results at $E_i = 35$ meV. At larger energies, the dispersion energies and intensities of both optic and acoustic modes are within error, similar to the insulating antiferromagnet.

For energy transfers below 200 meV, the momentum integral of the scattered intensity is shown in Fig. 3 as a function of the two-dimensional wave vector. The dashed line is the linear spin-wave theory with a constant renormalization factor, $Z_\chi=0.51$.\(^{26}\) The intensity loss at high energies, while subject to uncertainties in the absolute normalization and in the estimation of the background, is likely a forerunner of the large zone-boundary loss discussed below. For energy transfers below $\sim 200$ meV, the magnetic excitation energies and intensities resemble those of the insulating antiferromagnet YBCO$_{6.15}$ and the acoustic and optic intensities are similar to those of the insulator. In particular, the slope of the dispersion curve gives a spin-wave velocity of $592\pm30$ meV Å, which is in agreement with the velocity of $600$ meV Å measured for insulating YBCO$_{6.15}$.\(^{22}\) There are, however, considerable differences from spin-wave behavior at high-energy transfers above the range of $\hbar \omega \sim 150$–200 meV.

First, the energy widths of the excitations, shown in the constant-Q plots in Fig. 2, are about 100 meV, which are much larger than the experimental resolution (horizontal bar) of about 10 meV. Therefore, the zone-boundary excitations have acquired strong damping.

Second, we observe an overall lowering of the zone-boundary energies that is inconsistent with that of a simple antiferromagnet with a coupling between local spins. The
that in the layered Sr$_2$Cu$_3$O$_4$Cl$_2$ and Cu the same sign as that observed in La$_2$CuO$_4$ and opposite to CFTD.24,25

curs only near the point that in the square lattice CFTD, the spectral weight loss occur-
surements in superconducting La$_{1.86}$Sr$_{0.14}$CuO$_4$.20 We note
the difference decreases on approaching the magnetic zone
and suppressed spectral weight suggest that the magnetic ex-

![Image](78x499 to 270x734)

**FIG. 3.** (a) The momentum integrated intensity is plotted as a function of energy transfer. (b) The energy integrated intensity as a function of wave vector relative to (0.5,0.5) around the zone bound-
aries. (c) The intensity as a function of $L$ used to extract the acoustic and optic intensities.

dashed line in Fig. 4 shows that a nearest-neighbor model $J=130$ meV can fit the velocity at low energies but fails to
describe the dispersion at high energies above $\sim 150$–200 meV. The dotted curve shows that the La$_2$CuO$_4$ nearest and next-nearest interactions of 112 and $-11$ meV respectively, also overestimate the frequencies of the zone-
boundary excitations. The solid line represents an attempt to
reproduce the zone-boundary energies (with nearest and
next-nearest-neighbor interactions of 96 and $-10$ meV, re-
spectively) and it shows that the data cannot be described consistently with only near-neighbor interactions. All calculations
include a renormalization factor calculated to be $Z_c$
=1.18.26 We also observe anisotropic behavior at the zone
boundary almost twice as large as that found in the insulator
La$_2$CuO$_4$. The zone-boundary dispersion in YBCO$_{6.35}$ carries
the same sign as that observed in La$_2$CuO$_4$ and opposite to
that in the layered Sr$_2$Cu$_3$O$_4$Cl$_2$ and Cu(DCOO)$_3$·4D$_2$O
CFTD.24,25

A third difference between our results and linear spin-
wave theory is shown in Fig. 3(b), which plots the integral
over all energies taken from constant-$Q$ cuts above
150 meV. The zone-boundary intensity is about a factor of 2
less than predicted by linear spin-wave theory with a renor-
malization factor ($Z_c=0.51$).19,26 Figure 3(b) also shows that the difference decreases on approaching the magnetic zone
center. A decrease in the zone-boundary magnetic neutron-
scattering intensity has also been suggested based on meas-
urements in superconducting La$_{1.86}$Sr$_{0.14}$CuO$_4$.20 We note
that in the square lattice CFTD, the spectral weight loss oc-
curs only near the point (0.5,0) whereas we observe a loss of
spectral weight across a broader range in momentum.25

The large energy widths, reduced zone-boundary energy,
and suppressed spectral weight suggest that the magnetic ex-

![Image](78x499 to 270x734)

**FIG. 4.** The momentum dispersion is compared with the insulator YBCO$_{6.15}$ (Ref. 18) and YBCO$_{6.5}$ (Ref. 16). $\xi$ is measured from the zone center, (0.5,0.5).
citations interact with other high-energy excitations that do
not scatter neutrons strongly. The magnetic excitations could
decay into two spin waves but we find that it is not possible
to conserve wave vector and energy with the creation of pairs
of uncoupled magnetic excitations having the dispersion of
Fig. 4.23 We note, however, that if the single-magnon line-
width is increased, then the kinematic constraints are relaxed
and the decay into a pair of magnons may be possible. It is
also possible that in an $S=1/2$ system, there are two spin-
wave states that are coupled and that lie below the two spin-
wave continuum. The interaction between these states and
the magnetic excitations might give rise to the damping.

The fact that the unusual high-energy dispersion cannot
be made consistent with the spin-wave models that describe
the low-energy velocity and intensity (and also the entire
spin-wave dispersion in the insulators) points to the need for
an energy-dependent decay process. It is likely that the
damping arises from the decay into electronic particle-hole
pairs since the most energetic spin excitations lie above es-

timates for the pseudogap. One suggestion from thermal con-
ductivity measurements is that the quasiparticle gap for
heavily underdoped YBCO is $\sim 160$ meV, which is compa-

able to the energy where the magnetic excitations show
strong damping.27 The energy is also comparable to the ex-
pected pseudogap energy measured by nuclear magnetic
resonance and optical absorption.5 Hence, for energy trans-
fers greater than the pseudogap, the decay of a magnon into
a particle-hole pair is allowed.

In ferromagnetic metallic systems characterized by a con-
tinuum of particle-hole excitations (for example, in Fe, Ni, or
MnSi), spin waves become strongly damped when both $q$
and $\omega$ match those of the particle-hole pairs.29,30 This has
been suggested to account for the anomalous decrease in

intensity in YBCO$_{6.85}$ for energies $\sim 55$ meV.28 A similar
decay process may account for strong damping of the high-
energy excitations in YBCO$_{6.35}$. It therefore appears that
the large damping of the spin excitations at high energies maybe
a common trait among all high-temperature superconductors
across the entire phase diagram unlike the resonance and
incommensurate scattering which have not been observed in
all superconductors. It would be interesting to model this effect; however, the $t$-$J$ model has been applied to heavily doped superconductors, but to our knowledge, predictions for the lightly doped superconductor have not been made, possibly because of uncertainty in the Fermi surface.31–36

Near the onset of superconductivity, the low-energy spin response is strong and gives the appearance of spin waves, while at high energy, we have shown that the spin excitations enter a region where the decay, decrease in energy, and intensity do not fit into a spin-wave description. The evidence points to the presence of a particle-hole continuum as a possible explanation of the results. On this basis, we consider that the pseudogap is identified to be in the range 150–200 meV for $T_c = 0.35$, $T_c = 18$ K. The damping observed for $x = 0.85$, $T_c = 85$ K also suggests that the spin excitations decay near 55 meV and if this has the same origin, it implies that the pseudogap has decreased with increasing doping. In contrast, the low-energy results between $x = 0.35$ and $x = 0.5$ (Fig. 4) show the presence or absence of quasielastic scattering, commensurate or incommensurate excitations, and the presence or absence of a resonance, suggesting that these features are not present in all superconductors. We therefore suggest that the existence of the high-energy continuum seems to be the feature which is common to all superconductors at least up to optimal doping, whereas the low-energy features seem less universal.

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