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LOGARITHMIC AND OTHER MATHEMATICAL TABLE



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IN ALGEBRA  
AND TRIGONOMETRY  
FOR THE USE OF  
SCHOOL AND COLLEGE STUDENTS  
AND PRACTICING ENGINEERS  
BY  
SIMON NEWCOMB  
ASSISTANT  
TO THE  
ASTRONOMICAL  
DEPARTMENT  
OF THE  
U.S. NAVY  
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# LOGARITHMIC AND OTHER MATHEMATICAL TABLES

WITH EXAMPLES OF THEIR USE AND HINTS ON THE ART OF  
COMPUTATION

BY

SIMON NEWCOMB

*Professor of Mathematics, in the Johns Hopkins University.*



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## PREFACE.

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IN the present work an attempt is made to present to computers and students a set of logarithmic and trigonometric tables which shall have all the conveniences familiar to those who use German tables. The five-figure tables of F. G. GAUSS, of which fifteen editions have been issued, have, after long experience with them, been taken as the basis of the present ones, but modifications have been introduced wherever any improvement could be made.

Five places of decimals have been adopted as an advantageous mean. The results obtained by them, being nearly always reliable to the 10,000th part, are amply accurate for most computations, while the time of the student who uses them is not wasted in unnecessary calculation.

The Introduction is intended to serve not only as an explanation of the tables, but as a little treatise on the art of computation, and the methods by which the labor of computation may be abridged.

To avoid fostering the growing evil of nearsightedness among students, the author and publishers have spared neither pains nor expense in securing clearness of typography.



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TABLE I.  
LOGARITHMS OF NUMBERS.

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**1. Introductory Definitions.**

**Natural numbers** are numbers used to represent quantities.

The numbers used in arithmetic and in the daily transactions of life are natural numbers.

To every natural number may be assigned a certain other number, called its **logarithm**.

The **logarithm** of a natural number is the exponent of the power to which some assumed number must be raised to produce the first number. The assumed number is called the **base**. *E.g.*, the logarithm of 100 with the base 10 is 2, because  $10^2 = 100$ ; with the base 2, the logarithm of 64 would be 6, because  $2^6 = 64$ .

A **system of logarithms** means the logarithms of all positive numbers to a given base.

Although there may be any number of systems of logarithms, only two are used in practice, namely:

1. The natural or Napierian system, base =  $e = 2.718\ 282$ .
2. The common system, base = 10.

The natural system is used for purely algebraic purposes.

The common system is used to facilitate numerical calculations and is the only one employed in this book.

If the natural number is represented by  $n$ , its logarithm is called  
 $\log n$ .

A logarithm usually consists of an integer number and a decimal part.

The integer is called the **characteristic** of the logarithm.

The decimal part is called the **mantissa** of the logarithm.

A **table of logarithms** is a table by which the logarithm of any given number, or the number corresponding to any given logarithm, may be found.

The most simple form of table is that on the first page of Table I., which gives the logarithms of all entire numbers from 1 to 150; each logarithm being found alongside its number. The student may begin his exercises with this table.

Mathematical tables in general enable us, when one of two related quantities is given, to find the other.

In such tables the quantity supposed to be given is called the **argument**.

The argument is usually printed on the top, bottom, or side of the table.

The quantities to be found are called **functions** of the argument, and are found in the same columns or lines as the argument, but in the body of the table.

In a table of logarithms the natural number is the argument, and the logarithm is the function.

## 2. The Use of Logarithms.

The following properties of logarithms are demonstrated in treatises on algebra.

I. *The logarithm of a product is equal to the sum of the logarithms of its factors.*

II. *The logarithm of a quotient is found by subtracting the logarithm of the divisor from that of the dividend.*

III. *The logarithm of any power of a number is equal to the logarithm of the number multiplied by the exponent of the power.*

IV. *The logarithm of the root of a number is equal to the logarithm of the number divided by the index of the root.*

We thus derive the following rules:

To find the product of several factors by logarithms.

RULE. *Add the logarithms of the several factors. Enter the table with the sum as a new logarithm, and find the number corresponding to it.*

*This number is the product required.*

Example 1. To multiply  $7 \times 8$ .

We find from the first page of Table I.

$$\begin{array}{r} \log 7 = 0.845\ 10 \\ \text{“}\ 8 = 0.903\ 09 \end{array}$$

---

Sum of logs = 1.748 19 = log of product.

Having added the logarithms, we look in column log for a num-

ber corresponding to  $1.788\overline{1}9$  and find it to be 56, which is the product required.

*Ex. 2.* To find the continued product  $2 \times 6 \times 8$ .

$$\log 2, 0.301\,03$$

$$\text{“} 6, 0.778\,15$$

$$\text{“} 8, 0.903\,09$$

$$\text{Sum of logs, } 1.982\,27 = \log \text{product.}$$

The number corresponding to this logarithm is found to be 96, which is the product required.

*Ex. 3.* To find the quotient of  $147 \div 21$ .

$$\log 147, 2.167\,32$$

$$\text{“} 21, 1.322\,22$$

$$\text{Difference, } 0.845\,10$$

We find this difference to be the logarithm of 7, which is the required quotient.

*Ex. 4.* To find the quotient arising from dividing the continued product  $98 \times 102 \times 148$  by the continued product  $21 \times 37 \times 68$ .

$$\log 21, 1.322\,22 \qquad \log 98, 1.991\,23$$

$$\text{“} 37, 1.568\,20 \qquad \text{“} 102, 2.008\,60$$

$$\text{“} 68, 1.832\,51 \qquad \text{“} 148, 2.170\,26$$

$$\text{Sum} = \log \text{divisor, } 4.722\,93 \quad \text{Sum} = \log \text{dividend, } 6.170\,09$$

$$\log \text{divisor, } 4.722\,93$$

$$\text{Difference} = \log \text{quotient, } 1.447\,16$$

Looking into the table, we find the number corresponding to this logarithm to be 28, which is the required quotient.

NOTE. The student will notice that we have found this quotient without actually determining either the divisor or dividend, having used only their logarithms. If he will solve the problem arithmetically, he will see how much shorter is the logarithmic process.

*Ex. 5.* To find the seventh power of 2.

We have  $\log 2 = 0.301\,03$

7

$$\overline{2.107\,21} = \log 128$$

Hence 128 is the required power.

*Ex. 6.* To find the cube root of 125.

$$\begin{array}{r} 3 | 2.096\,91 \\ \hline 0.698\,97 \end{array}$$

The index of the root being 3, we divide the logarithm of 125 by it. Looking in the tables, we find the number to be 5, which is the root required.

## EXERCISES.

Compute the following products, quotients, powers, and roots by logarithms.

$$1. 11 \cdot 13. \text{ Ans. } 143.$$

$$5. \frac{22 \cdot 8^2}{\sqrt[4]{121}}. \text{ Ans. } 128.$$

$$2. 12^2. \text{ Ans. } 144.$$

$$6. \frac{51 \cdot 98 \sqrt[4]{81}}{34 \cdot 63}. \text{ Ans. } 21.$$

$$3. \frac{12^2}{6^2}. \text{ Ans. } 48.$$

$$7. \frac{2^7 \cdot 3^5}{6^3}. \text{ Ans. } 144.$$

$$4. \frac{2 \cdot 9^2 \cdot 91 \cdot 78}{13^2 \cdot 21 \cdot 3}. \text{ Ans. } 108.$$

$$8. \frac{54 \cdot 48}{8 \cdot 9}. \text{ Ans. } 36.$$

## 3. Arrangement of the Table of Logarithms.

A table giving every logarithm alongside its number, as on the first page of Table I., would be of inconvenient bulk. For numbers larger than 150 the succeeding parts of Table I. are therefore used. Here the first three figures of the natural number are given in the left-hand column of the table. The first figure must be understood where it is not printed. The fourth figure is to be sought in the horizontal line at the top or bottom. The mantissa of the logarithm is then found in the same line with the first three digits, and in the column having the fourth digit at the top.

To save space the logarithm is not given in the column, but only its last three figures. The first two figures are found in the first column, and are commonly the same for all the logarithms in any one line.

*Example* 1. To find the logarithm of 2090.

We find the number 209, the figure 2 being omitted in printing, in the left-hand column of the table, and look in the column having the fourth figure, 0, at its top or bottom. In this column we find 320 15, which is the mantissa of the logarithm required.

*Ex.* 2. To find the logarithm of 2092.

Entering the table with 209 in the left-hand column, and choosing the column with 2 at the top, we find the figures 056. To these we prefix the figures 32 in column 0, making the total logarithm 320 56. Therefore

$$\text{Mantissa of } \log 2092 = .320\ 56.$$

## EXERCISES.

Find in the same way the mantissæ of the logarithms of the following numbers:

2240;	5133;
2242;	5256;
2249;	5504;
2895;	8925;
3644;	9557;
4688;	9780.

When the first two figures of the mantissa are not found in the same line in which the number is sought, they are to be found in the first line above which contains them.

*Example.* The first two figures of log 6250 are 79, which belongs to all the logarithms below as far as 6309. Therefore mantissa of log 6250 = .795 88.

## EXERCISES.

Find the mantissæ of the logarithms of

6300;	answer, .799 34.
6309;	" .799 96.
6434;	
6653;	
6755;	
6918;	
7868.	

*Exception.* There are some cases in which the first two figures change in the course of the line. In this case the first two figures are to be sought in the line above before the change and in the line next below after the change.

*Example.* The mantissa of log 6760 is .829 95. But the mantissa of log 6761 is .830 01. In this case the figures 83 are to be found in the next line below. To apprise the computer of these cases, each of the logarithms in which the two first figures are found in the line below is indicated by an asterisk.

## EXERCISES.

Find the mantissa of

log 1022;	answer, .009 45.
log 1024;	" .010 30.

1231;	1999;
1387;	3988;
1419;	4675;
1621;	4798;
1622;	5377;
1862;	8512;
1863;	1009.

#### 4. Characteristics of Logarithms.

The part of the table here described gives only the *mantissa* of each logarithm. The characteristic must be found by the general theory of logarithms.

The following propositions are explained in treatises on algebra:

The logarithm of	1	is	0.
" " "	10	"	1.
" " "	100	"	2.
" " "	1000	"	3.
" " "	$10^n$	"	$n$ .

Since any number of one digit is between 0 and 10, its logarithm is between 0 and 1; that is, it is 0 *plus* some fraction. In the same way, the logarithm of a number of two digits is 1 + a fraction. And in general,

*The characteristic of the logarithm of any number greater than 1 is less by unity than the number of its digits preceding the decimal point.*

*Example.* The characteristic of the logarithm of any number between 1 and 10 is 0; between 10 and 100 it is 1; between 100 and 1000 it is 2, etc.

Characteristic of log	1646	is	3.
" " "	164.6	"	2.
" " "	16.46	"	1.
" " "	1.646	"	0.

It is also shown in algebra that if a number be divided by 10 we diminish its logarithm by unity.

Logarithms of numbers less than unity are most conveniently expressed by making the characteristic alone negative.

For example:

$$\begin{aligned}\log 0.2 &= \log 2 - 1 = -1 + .30103; \\ " 0.02 &= \log 2 - 2 = -2 + .30103.\end{aligned}$$

Hence: *The mantissæ of the logarithms of all numbers which differ only in the position of the decimal point are the same.*

Hence, also, in seeking a logarithm from the table we find the mantissa without any reference to the decimal point. Afterward we affix the characteristic according to the position of the decimal point.

For convenience, when a negative characteristic is written the minus sign is put above it to indicate that it extends only to the characteristic below it and not to the mantissa. Thus we write

$$\log .02 = \bar{2}.301\ 03.$$

In practice, however, it is more common to avoid the use of negative characteristics by increasing them by 10. We then write

$$\log .02 = 8.301\ 03 - 10.$$

If we omitted to write - 10 after the logarithm, the latter would, in strictness, be the log of  $2 \times 10^9$ . But numbers so great as this product occur so rarely in practice that it is not generally necessary to write - 10 after the logarithm. This may be understood.

A convenient rule for remembering what characteristic belongs to the logarithm of a decimal fraction is:

*The characteristic is equal to 9, minus the number of zeros after the decimal point and before the first significant figure.*

Examples.	log 34060	= 4.532 24
"	340.60	= 2.532 24
"	3.4060	= 0.532 24
"	.034 06	= 8.532 24 - 10
"	.000 340 6	= 6.532 24 - 10

It will be seen that we can find the logarithms of numbers from 1 to 150 without using the first page of the table at all, since all the mantissæ on this page are found on the following pages as logarithms of larger numbers.

### EXERCISES.

Find the logarithms of the following numbers:

1.515	.003 899
.01 702	0.4276
18.62	464 700
.03 735	98.030

Find the numbers corresponding to the following logarithms:

3.241 80;	8.750 35 - 10;	9.999 91 - 10;
1.191 45;	7.411 28 - 10;	5.999 96;
5.653 21;	6.889 97 - 10;	2.960 28;
6.748 27;	ans. 5 601 000	0.886 27;
7.560 03;	ans. 36 310 000	0.000 87.

*Always write - 10 & no doubt  
ever arises of correctness of work*

### 5. Interpolation of Logarithms.

In all that precedes we have used only logarithms of numbers containing not more than 4 significant digits. But in practice numbers of more than four figures have to be used. To find the logarithms of such numbers the process of interpolation is necessary. This process is one of simple proportion, which can be seen from the following example.

To find log. 1167.23.

The table gives the logarithms of 1167 and of 1168, which we find to be as follows:

$$\begin{aligned}\log 1167 &= 3.067\ 07 \\ “ 1168 &= 3.067\ 44\end{aligned}$$

$$\text{Difference of logarithms} = .000\ 37$$

Now the number of which we wish to find the logarithm being between these numbers, its logarithm is between these logarithms; that is, it is equal to 3.067 07 plus a fraction less than .000 37.

Since the difference 37 corresponds to the difference of unity in the two numbers, we assume that the quantity to be added to the logarithm bears the same proportion to .23 that 37 does to unity. We therefore state the proportion

$$1 : .23 :: 37 : \text{increase required.}$$

The solution of this proportion gives  $.23 \times 37 = 8.51$ , which is the quantity to be added to  $\log 1167$  to produce the logarithm required.\* The result is 3.067 155 1.

But our logarithms extend only to five places of decimals, while the result we have written has seven. We therefore take only five places of decimals. If we write the mantissa 3.067 15, the result will be too small by .51. If we write 3.067 16, it will be too great by .49. Since the last result is nearer than the first, we give it the preference, and write for the required logarithm

$$\log 1167.23 = 3.067\ 16.$$

We thus have the following rule for interpolating:

*Take from the table the logarithm corresponding to the first four significant digits of the number.*

*Considering the following digits as a decimal fraction, multiply the difference between the logarithm and the next one following by such decimal fraction.*

\* In this multiplication we have used a decimal point to mark on the fifth order of decimals. This is a convenient process in all such computations.

*This product being added to the logarithm of the table will give the logarithm required.*

The whole operation by which we have found  $\log 1167.23$  would then be as follows:

$$\begin{array}{r}
 \log 1167 = 3.067\ 07 \\
 37 \times 0.2 \qquad \qquad \qquad 7.4 \\
 \times 0.03 \qquad \qquad \qquad 1.11 \\
 \hline
 \log 1167.23 = 3.067\ 16
 \end{array}$$

The products for interpolation, 7.4 and 1.11, may be found by multiplying by the fifth and sixth figures of the number separately.

To facilitate this multiplication, tables of proportional parts are given in the margin. Each difference between two logarithms will be readily found in heavy type not far from that part of the table which is entered, and under it is given its product by .1, .2, etc., . . . .9. We therefore enter this little table with the fifth figure, and take out the corresponding number to be added to the logarithm. Then if there is a sixth figure, we enter with that also and move the decimal one place to the left. We then add the two sums to the logarithm.

## 6. Labor-saving Devices.

In using a table of logarithms, the student should accustom himself to certain devices by which the work may be greatly facilitated.

In the first place it is not necessary to take the whole difference between two consecutive logarithms. He has only to subtract the last figure of the preceding logarithm from the last one of the following, increased by 10 if necessary, and thus find the last figure of the difference.

The nearest difference in the margin of the table having this same last figure will always be the difference required.

*Example.* If the first four figures of the number are 1494, instead of subtracting 435 from 464 we say 5 from 14 leaves 9, and look for the nearest difference which has 9 for its last figure. This we readily find to be 29, at the top of the next page.

**NOTE.** In nearly all cases the difference will be found on the same page with the logarithm. The only exception is at the bottom of the first page, where, owing to the number of differences, they cannot all be printed.

In the preceding examples we have written down the numbers in full, which it is well that the beginner should do for himself. But after a little practice it will be unnecessary to write down anything

but the logarithm finally taken out. The student should accustom himself to take the proportional parts mentally, adding them to the logarithm of the table and writing down the sum at sight. The habit of doing this easily and correctly can be readily acquired by practice.

*Exercises.* Find the logarithms of

792 638;	0.99997;
1000.77;	949.916;
1000.07;	20.8962;
100 007;	660 652;
181 982;	77.642;
281.936;	8.8953.

As a precaution in taking out logarithms, the computer should always, after he has got his result, look into the table and see that it does really fall between two consecutive logarithms in the table.

If the fraction to be interpolated is nearly unity, especially if it is equal to or greater than 9, it will generally be more convenient to multiply the difference of the logarithms by the complement\* of the fraction and subtract the product from the logarithm next succeeding. The following are examples of the two methods, which may always be applied whether the fraction be large or small:

*Example 1.*  $\log 1004.28 = \log (1005 - .72)$ .

log 1004,	.001 73	log 1005,	.002 17
pr. pt. for	.2,	8.8	pr. pt. for
" " "	.08,	3.5	" " "
<hr/>			<hr/>
log, 3.001 85			log, 3.001 85

*Ex. 2.*  $\log 154\ 993 = 155\ 000 - .7$ .

log 1549,	.190 05	log 1550,	.190 33
pr. pt. for	.9,	25.2	pr. pt. for
" " "	.03,	0.8	" " "
<hr/>			<hr/>
log, 5.190 31			log, 5.190 31

\* By the *complement* or *arithmetical complement* of a decimal fraction is here meant the remainder found by subtracting it from unity or from a unit of the next order higher than itself. Thus:

$$\text{co. } .723 = .277$$

$$\text{co. } .1796 = .8204$$

$$\text{co. } .9982 = .0068.$$

### 7. To find the Number corresponding to a given Logarithm.

The reverse process of finding the number corresponding to a given logarithm will be seen by the following example:

To find the number of which the logarithm is 2.027 90.

Entering the table, we find that this logarithm does not exactly occur in the table. We therefore take the next smaller logarithm, which we find to be as follows:

$$\log 1066 = 2.02776.$$

Subtracting this from the given logarithm we find the latter to be greater by 14, while the difference between the two logarithms of the table is 40. We therefore state the proportion

$$40 : 14 :: 1 \text{ to the required fraction.}$$

The result is obtained by dividing 14 by 40, giving a quotient .35. The required number is therefore 106.635. It will be remarked that we take no account of the characteristic and position of the decimal until we write down the final result, when we place the decimal in the proper position.

The table of proportional parts is used to find the fifth and sixth figures of the number by the following rule:

If the given logarithm is not found in the table, note the excess of the given logarithm above the next smaller one in the table, which call  $\Delta$ .

Take the difference of the two tabular logarithms, and find it among the large figures which head the proportional parts.

That proportional part next smaller than  $\Delta$  will ~~be~~ correspond to the fifth figure of the required number.

Take the excess of  $\Delta$  above this proportional part; imagine its decimal point removed one place to the right, and find the nearest number of the table.

This number will be the sixth figure of the required number.

*Example.* To find the number of which the logarithm is 2.193 59.

Entering the table, we find the next smaller logarithm to be .193 40. Therefore  $\Delta = 19$ .

Also its tabular difference = 28.

Entering the table of proportional parts under 28, we find 16.8 opposite 6 to be the number next smaller than 19 the value of  $\Delta$ . Therefore the fifth figure of the number is 6.

The excess of 19 above 16.8 is 2.2. Looking in the same table for the number 22, we find the nearest to be opposite 8.

Therefore the fifth and sixth figures of the required number are 68. Now looking at the log .193 40 and taking the corresponding number, we find the whole required number to be

156 168.

The characteristic being 2, the number should have three figures before the decimal point. Therefore we insert the decimal point at the proper place, giving as the final result 156.168.

### 8. Number of Decimals necessary.

In the preceding examples we have shown how with these tables the numbers may be taken out to six figures. In reality, however, it will seldom be worth while to write down more than five figures. That is, we may be satisfied by adding only one figure to the four found from the table. In this case, when we enter the table of proportional parts, we take only the number corresponding to the nearest proportional part.

To return to the last preceding example, where we find the number corresponding to 2.193 59. We find under the difference 28 that the number nearest 19 is 19.6, which is opposite 7.

Therefore the number to be written down would be 156.17.

In the following exercises it would be well for the student to write six figures when the number is found on one of the first two pages of the table and only five when on one of the following pages. The reason of this will be shown subsequently.

### EXAMPLES AND EXERCISES.

1. To find the square root of  $\frac{3}{2}$ .

We have

$$\log 3. \quad 0.477 \ 12$$

$$\quad \quad \quad " \quad 2. \quad 0.301 \ 03$$

$$\log \frac{3}{2}. \quad 0.176 \ 09$$

$$\div 2, \log \sqrt{\frac{3}{2}}. \quad 0.088 \ 04$$

Here we have a case in which the half of an odd number is required. We might have written the last logarithm 0.088 045, but we should then have had six decimals, whereas, as our tables only give five decimals, we drop the sixth. If we write 4 for the fifth figure it will be too small by half a unit, and if we write 5 it will be too large by half a unit. It is therefore indifferent which figure we write, so far as mere accuracy is concerned.

A good rule to adopt in such a case is to *write the nearest even number*. For example,

for the half of .261 81 we write .130 90;

"	"	.261 83	"	.130 92;
"	"	.261 85	"	.130 92;
"	"	.261 87	"	.130 94;
"	"	.261 89	"	.130 94;
"	"	.261 97	"	.130 98;
"	"	.261 99	"	.131 00.

Returning to our example, we find, by taking the number corresponding to 0.088 04,

$$\sqrt{\frac{2}{3}} = 1.224\ 72.$$

2. To find the square root of  $\frac{2}{3}$ .

$$\log 2, 0.301\ 03$$

$$\quad \quad " 3, 0.477\ 12$$

$$\log \frac{2}{3}, 9.823\ 91 - 10$$

$$\frac{1}{2} \log \frac{2}{3}, 4.911\ 96 - 5 = \log \sqrt{\frac{2}{3}}.$$

The last logarithm is the same as

$$9.911\ 96 - 10,$$

which is the form in which it is to be written in order to apply the rule of characteristics. The corresponding number is 0.816 50.

We have here a case in ~~which~~, had we neglected considering the surplus - 10 as we ~~had~~ do, the characteristic of the answer would have been 4 instead of 9 or - 1. The easiest way to treat such cases is this:

*When we have to divide a logarithm in order to extract a root, instead of increasing the characteristic by 10, increase it by  $10 \times$  index of root.*

Thus we write  $\log \frac{2}{3} = 19.823\ 91 - 20$ .

Dividing by 2,  $\log \sqrt{\frac{2}{3}} = 9.911\ 96 - 10$ ,  
which is in the usual form.

3. To find the cube root of  $\frac{1}{2}$ .

$$\log 1, 0.000\ 00$$

$$\quad " 2, 0.301\ 03$$

$$\log \frac{1}{2}, 9.698\ 97 - 10,$$

which we write in the form

$$\log \frac{1}{2} = 29.698\ 97 - 30.$$

Dividing this by 3,

$$\frac{1}{3} \log \frac{1}{2} = \log \sqrt[3]{\frac{1}{2}} = 9.899\ 66 - 10.$$

This logarithm is in the usual form, and gives

$$\sqrt[3]{\frac{1}{2}} = 0.793\ 70.$$

The affix — 30, or  $-10 \times$  divisor, can be left to be understood in these cases as in others. All that is necessary to attend to is that instead of supposing the characteristic to be one or more units less than 10, as in the usual run of cases, we suppose it to be one or more units less than  $10 \times$  divisor.

*Omit*

Find:

4. The square root of  $\frac{1}{2}$ ;
5. The cube root of 2;
6. The fourth root of  $\frac{3}{4}$ ;
7. The fifth root of 20;
8. The tenth root of 10;
9. The tenth root of  $\frac{1}{10}$ .

### 9. The Arithmetical Complement.

When a logarithm is subtracted from zero, the remainder is called its *arithmetical complement*.

If  $L$  be any logarithm, its arithmetical complement will be  $-L$ . Hence if

$$L = \log n,$$

then

$$\text{arith. comp.} = -L = \log \frac{1}{n};$$

that is,

*The arithmetical complement of a given logarithm is the logarithm of the reciprocal of the number corresponding to the given logarithm.*

*Notation.* The arithmetical complement of a logarithm is written co-log. It is therefore defined by the form

$$\text{co-log } n = \log \frac{1}{n}.$$

*Finding the arithmetical complement.* To find the arithmetical complement of  $\log 2 = 0.301\ 03$ , we may proceed thus:

$$\begin{array}{r} 0.000\ 00 \\ \log 2, \ 0.301\ 03 \\ \hline \end{array}$$

$$\text{co-log } 2, \ 9.698\ 97 - 10.$$

We subtract from zero in the usual way; but when we come to the characteristic, we subtract it from 10. This makes the remainder too large by 10, so we write  $-10$  after it, thus getting a quantity which we see to be  $\log 0.5$ .

~~We may leave the 10 to be understood, as already explained.~~

The arithmetical complement may be formed by the following rule:

*Subtract each figure of the logarithm from 9, except the last significant one, which subtract from 10. The remainders will form the arithmetical complement.*

For example, having, as above, the logarithm 0.301 03, we form, mentally,  $9 - 0 = 9$ ;  $9 - 3 = 6$ ;  $9 - 0 = 9$ ;  $9 - 1 = 8$ ;  $9 - 0 = 9$ ;  $10 - 3 = 7$ ; and so write

$$\begin{array}{r} 9.698\ 97 \\ \hline \end{array}$$

as the arithmetical complement.

To form the arithmetical complement of 3.284 00 we have  $9 - 3 = 6$ ;  $9 - 2 = 7$ ;  $9 - 8 = 1$ ;  $10 - 4 = 6$ . The complement is therefore

$$\begin{array}{r} 6.716\ 00 \\ \hline \end{array}$$

The computer should be able to form and write down the arithmetical complement without first writing the tabular logarithm, the subtraction of each figure being performed mentally.

*Use of the arithmetical complement.* The co-log is used to substitute addition for subtraction in certain cases, on the principle: *To add the co-logarithm is the same as to subtract the logarithm.*

*Example.* We may form the logarithm of  $\frac{3}{2}$  in this way by addition:

$$\begin{array}{r} \log 3, \ 0.477\ 12 \\ \text{co-log } 2, \ 9.698\ 97 \quad \underline{-10} \\ \hline \log \frac{3}{2}, \ 0.176\ 09 \end{array}$$

Here there is really no advantage in using the co-log. But there is an advantage in the following example:

To find the value of  $P = \frac{2763 \times 419.24}{99}$ . We add to the logarithms of the numerator the co-log of the denominator, thus:

$$\begin{array}{r} \log 2763, \quad 3.441\ 38 \\ \log 419.24, \quad 2.622\ 46 \\ \text{co-log } 99, \quad 8.004\ 36 \quad \underline{-10} \\ \hline \log P, \quad 4.068\ 20 \\ \therefore P = 11\ 700. \end{array}$$

The use of the arithmetical complement is most convenient when the divisor is a little less than some power of 10.

## EXERCISES.

Form by arithmetical complements the values of:

$$1. \quad \frac{109 \times 216.26}{0.99316}$$

$$2. \quad \frac{8263 \times 9162.7}{92 \times 99.618}$$

$$3. \quad \frac{4 \times 6 \times 8219}{9 \times 992}$$

### 10. Practical Hints on the Art of Computation.

The student who desires to be really expert in computation should learn to reduce his written work to the lowest limit, and to perform as many of the operations as possible mentally. We have already described the process of taking a logarithm from the table without written computation, and now present some exercises which will facilitate this process.

1. *Adding and subtracting from left to right.* If one has but two numbers to add it will be found, after practice, more easy and natural to write the sum from the left than from the right. The method is as follows:

In adding each figure, notice, before writing the sum, whether the sum of the figures following is less or greater than 9, or equal to it.

If the sum is less than 9, write down the sum found, or its last figure without change.

If greater than 9, increase the figure by 1 before writing it down.

If equal to 9, the increase should be made or not made according as the first sum following which differs from 9 is greater or less than 9.

If the first sum which differs from 9 exceeds it, not only must we increase the number by 1, but must write zeros under all the places where the 9's occur. If the first sum different from 9 is less than 9, write down the 9's without change.

The following example illustrates the process:

$$\begin{array}{r}
 7\ 5\ 0\ 2\ 7\ 6\ 8\ 3\ 5\ 7\ 8\ 5\ 8\ 8\ 9\ 2\ 8\ 3\ 7 \\
 8\ 2\ 3\ 9\ 1\ 7\ 1\ 6\ 4\ 5\ 0\ 4\ 1\ 1\ 0\ 2\ 5\ 9\ 8 \\
 \hline
 1\ 5\ 7\ 4\ 1\ 9\ 4\ 0\ 0\ 0\ 2\ 8\ 9\ 9\ 9\ 5\ 4\ 3\ 5
 \end{array}$$

Here 7 and 8 are 15. 5 + 2 being less than 9, we write 15 without change. 8 + 0 being less than 9, we write 7 without change. 9 + 2 being greater than 9, we increase the sum 3 + 0 by 1 and write down 4. 7 + 1 being

less than 9, we write the last figure of  $9 + 2$ , or 1, without change.  $6 + 7$  being greater than 9, we increase  $7 + 1$  by 1 and write down 9. Under  $6 + 7$  we write down 3 or 4. To find which,  $8 + 1 = 9$ ;  $3 + 6 = 9$ ;  $5 + 4 = 9$ ;  $7 + 5 = 12$ . This first sum which is different from 9 being greater than 9, we write 4 under  $6 + 7$ , and 0's in the three following places where the sums are 9.  $7 + 5 = 12$ . Since  $8 + 0 < 9$ , we write down 2. Before deciding whether to put 8 or 9 under  $8 + 0$ , we add  $5 + 4 = 9$ ;  $8 + 1 = 9$ ;  $8 + 1 = 9$ ;  $9 + 0 = 9$ ;  $2 + 2 = 4$ . This being less than 9, we write 8 under  $8 + 0$ , and 9's in the four following places. Since  $5 + 8 = 13 > 9$ , we write 5 under  $2 + 2$ . Since  $9 + 3 = 12 > 9$ , we write 4 under  $5 + 8$ . Since  $8 + 7 = 15 > 9$ , we write 3 under  $9 + 3$ . Finally, under  $8 + 7$  we write 5.

This process cannot be advantageously applied when more than two numbers are to be added.

#### EXERCISES.

Let the student practise adding each consecutive pair of the following lines, which are spaced so that he can place the upper margin of a sheet of paper under the lines he is adding and write the sum upon it.

2	5	0	9	1	7	2	8	5	3	1	6	9	8	1	2	0	8
2	5	1	2	3	5	9	6	4	6	9	2	1	8	4	3	6	8
7	9	1	6	1	5	8	3	2	3	1	6	6	4	6	8	9	1
2	0	8	5	3	2	1	6	4	3	7	9	1	0	2	9	0	9
8	6	8	5	8	8	9	6	4	3	4	2	9	4	4	8	2	5
9	8	7	6	5	4	3	2	1	0	1	2	3	4	5	6	7	4

*Subtracting.* We subtract each figure of the subtrahend from the corresponding one of the minuend (the latter increased by 10 if necessary), as in arithmetic.

Before writing down the difference, we note whether the following figure of the subtrahend is greater, less, or equal to the corresponding figure of the minuend.

If greater, we diminish the remainder by 1 and write it down.\*

If less, we write the remainder without change.

If equal, we note whether the subtrahend is greater or less than the minuend in the first following figure in which they differ.

If greater, we diminish the remainder by 1, as before, and write 9's under the equal figures.

\* If the student is accustomed to carrying 1 to the figures of the minuend when he has increased the figure of his subtrahend by 10, he may find it easier to defer each subtraction until he sees whether the remainder is or is not to be diminished by 1, and, in the latter case, to increase the minuend by 1 before subtracting.

If less, write the remainder unchanged, putting 0's under the equal figures.

*Example.*

7	2	2	9	3	5	1	6	2	1	4	3	9	4
2	4	2	6	8	5	1	8	0	1	4	1	9	8
4	8	0	2	4	9	9	8	2	0	0	1	9	6

Here  $7 - 2 = 5$ ; because  $4 > 2$ , we write 4.  $12 - 4 = 8$ ; because  $2 = 2$  and  $6 < 9$ , we write 8; and write 0 in the following place.  $9 - 6 = 3$ ; because  $8 > 3$ , we write 2.  $13 - 8 = 5$ ;  $5 = 5$ ;  $1 = 1$ ;  $8 > 6$ ; so under  $13 - 8$  we write 4, with 9's in the two next places.  $16 - 8 = 8$ ; because  $0 < 2$ , we write 8.  $2 - 0 = 2$ ;  $1 = 1$ ;  $4 = 4$ ;  $1 < 3$ ; so under  $2 - 0$  we write 2, followed by 0's.  $3 - 1 = 2$ ; because  $9 = 9$ ,  $8 > 4$ , we write 1, with 9 in the next place.  $14 - 8 = 6$ , which we write as the last figure.

### EXERCISES.

The preceding exercises in addition will serve as exercises in subtraction by subtracting each line from that above or below it. The student should be able to subtract with equal facility whether the minuend is written above or below the subtrahend.

*Mental addition and subtraction.* When an expert computer has to add or subtract two logarithms, as in forming a product or quotient of two quantities, he does not necessarily write both of them, but prefers to write the first and, taking the other mentally, add (or subtract) each figure in order from left to right, and write down the sum (or difference). He thus saves the time spent in writing one number, and, sometimes, the inconvenience of writing it where there is not sufficient room for it.

This process of inverted addition is most useful in adding the proportional part in taking a logarithm from the table. It is then absolutely necessary to save the computer the trouble of copying both logarithm and proportional part.

Expert computers can add seven-figure logarithms in this way without trouble. But with those who do not desire to become experts it will be sufficient to learn to add two or three figures, so as to be able to take a five-figure or seven-figure logarithm from the table without writing anything but the result.

### 11. Imperfections of Logarithmic Calculations.

Nearly all practical computations with logarithms are affected by certain sources of error, arising from the omission of decimals. It is important that these errors should be understood in

order not only to avoid them so far as possible, but to avoid spending labor in aiming at a degree of accuracy beyond that of which the numbers admit.

Mathematical results may in general be divided into two classes: (1) those which are absolutely exact, and (2) those which are only to a greater or less degree approximate.

As an example of the former case, we have all operations upon entire numbers which involve only multiplication and division. For example, the equations

$$16^2 = 256$$

$$\frac{8^2}{6^2} = \frac{16}{9}$$

are absolutely exact.

But if we express the fraction  $\frac{1}{9}$  as a decimal fraction, we have

$$\frac{1}{9} = .142\ 857.\dots, \text{etc., ad infinitum.}$$

Hence the representation of  $\frac{1}{9}$  as a decimal fraction can never be absolutely exact. The amount of the error will depend upon how many decimals we include. If we use only two decimals we shall certainly be within one hundredth; if three, within one thousandth, etc. Hence the degree of accuracy to which we attain depends upon the number of decimals employed. By increasing the number of decimals we can attain to any degree of accuracy. As an example, it is shown in geometry that if the ratio of the circumference of a circle to its diameter be written to 35 places of decimals, the result will give the whole circumference of the visible universe without an error as great as the minutest length visible in the most powerful microscope.

There are no numbers, except the entire powers of 10, of which the logarithms can be exactly expressed in decimals. We must therefore omit all figures of the decimal beyond a certain limit. The number of decimals to be used in any case depends upon the degree of accuracy which is required. The large tables of logarithms contain seven decimal places, and therefore give results correct to the ten-millionth part of the unit. This is sufficiently near the truth in nearly all the applications of logarithms.

With five places of decimals our numbers will be correct to the hundred-thousandth part of a unit. This is sufficiently near for most practical applications.

*Accumulation of errors.* When a long computation is to be made, the small errors are liable to accumulate so that we cannot rely upon this degree of accuracy in the final result. The manner

in which the tables are arranged so as to reduce the error to a minimum may be shown as follows:

We have to seven places of decimals

$$\begin{aligned}\log 17 &= 1.230\ 448\ 9 \\ “\ 18 &= 1.255\ 272\ 5\end{aligned}$$

When the tables give only five places of decimals the two last figures must be omitted. If the tables gave  $\log 17 = .230\ 44$ , the logarithm would be too small by 89 units in the seventh place. It is therefore increased by a unit in the fifth place, and given .230 45. This quantity is then too large by 11, and is therefore nearer the truth than the other. The nearest number being always given, we have the result:

*Every logarithm in the table differs from the truth by not more than one half a unit of the last place of decimals.*

Since the error may range anywhere from zero to half a unit, and is as likely to have one value as another between those limits, we conclude:

*The average error of the logarithms in the tables is one fourth of a unit of the last place of decimals.*

*Errors in interpolation.* When we interpolate the logarithm we add to the tabular logarithm another quantity, the proportional part, which may also be in error by half a unit, but of which the average error will only be one fourth of a unit.

As most logarithms have to be interpolated, the general result will be:

*An interpolated logarithm may possibly be in error by a unit in the last place of decimals.*

The sum of the average errors will, however, be only half a unit. But these errors may cancel each other, one being too large and the other too small. The theory of probabilities shows that, in consequence of this probable cancellation of errors, the average error only increases as the square root of the number of erroneous units added.

The square root of 2 is 1.41.

If, therefore, we add two quantities each affected with a probable error  $\pm .25$ , the result will be, for the probable error of the sum,

$$1.41 \times .25 = 0.35.$$

We therefore conclude:

*The average error of a logarithm derived from the table by interpolation is 0.35 of a unit of the last place.*

Applying the above rule of the square root to the case in which

several logarithms are added or subtracted to form a quotient, we find the results of the following table:

No. of logs added or subtracted.	Average error.
1.....	0.35
2.....	0.50
3.....	0.63
4.....	0.72
5.....	0.81
6.....	0.88
7.....	0.95
8.....	1.02
9.....	1.08
10.....	1.14

From this table we see that if we form the continued product of eight factors, by adding their logarithms the average error of the sum of the logarithms will be more than a unit in the last place.

As an example of the accumulation of errors, let us form the product 11 · 13.

We have from the table

$$\begin{array}{r} \log 11 = 1.041\ 39 \\ " \ 13 = 1.113\ 94 \\ \hline \text{log product, } 2.155\ 33 \end{array}$$

We see that this is less than the given logarithm of the product 143 by a unit of the fifth order. But if we use seven decimals we have

$$\begin{array}{r} \log 11, 1.041\ 392\ 7 \\ " \ 13, 1.113\ 943\ 4 \\ \hline 2.155\ 336\ 1 \end{array}$$

Comparing this with the computation to five places, we see the source of the error.

If the numbers with which we enter the tables are affected by errors, these errors will of course increase the possible errors of the logarithms.

In determining to what degree of accuracy to carry our results, we have the following practical rule :

*It is never worth while to carry our decimals beyond the limit of precision given by the tables, which limit may be a considerable fraction of the unit in the last figure of the tables.*

Let us have a logarithm to five places of decimals, 1.929 49, of which we require the corresponding number. Entering the table, we

perceive that the corresponding number is between 85.01 and 85.02. If this logarithm is the result of adding a number of logarithms, each of which may be in error in the way pointed out, we may suppose it probably affected by an error of half a unit in the last figure and possibly by an error of a whole unit or more. That is, its true value may be anywhere between 92 948 and 92 950.

The number corresponding to the former value is 85.012, and that corresponding to the latter 85.016. Since the numbers may fall anywhere between these limits, we assign to it a mean value of 85.014, which value, however, may be in error by two units in the last place. It is not, therefore, worth while to carry the interpolation further and to write more than five digits.

Next suppose the logarithm to be 2.021 70. Entering the table, we find in the same way that the number probably lies between the limits 105.121 and 105.126. There is therefore an uncertainty of five units in the sixth place, or half a unit in the fifth place. If the greatest precision is desired, we should write 105.124. But our last figure being doubtful by two or three units, the question might arise whether it were worth while to write it at all. As a general rule, if the sixth figure is required to be exact, we must use a six- or seven-place table of logarithms.

Still, near the beginning of the table, the probable error will be diminished by writing the sixth figure.

Now knowing that at the beginning of the table a difference of one unit in the number makes a change ten times as great in the logarithm as at the end of the table, we reach the conclusions :

*In taking out a number in the first part of the table, it can never be worth while to write more than six significant figures, and very little is added to the precision by writing more than five.*

*In the latter part of the table it is never worth while to write more than five significant figures.*

Sometimes no greater accuracy is required than can be gained by using four-figure logarithms. There is then no need of writing the last figure. If, however the printed logarithm is used without change, the fourth figure must be increased by unity whenever the fifth figure exceeds 5. When the fifth figure is exactly 5, the increase should or should not be made according as the 5 is too small or too great. To show how the case should be decided, a stroke is printed above the 5 when it is too great. In these cases the fourth figure should be used as it stands, but, when there is no stroke, it should be increased by unity.

## 12. Applications of Logarithms to the Computation of Annuities and Accumulations of Funds at Compound Interest.

One of the most useful applications of logarithms is to fiscal calculations, in which the value of moneys accumulating for long periods at compound interest is required.

Compound interest is gained by any fund on which the interest is collected at stated intervals and put out at interest.

As an example, suppose that \$10 000 is put out at 6 per cent interest, and the interest collected semi-annually and put out at the same rate. The principal will then grow as follows:

Principal at starting.....	\$10 000.00
Six months' interest = 3 per cent.....	<u>300.00</u>
Amount at end of 6 months.....	\$10 300.00
Interest on this amount = 3 per cent..	<u>309.00</u>
Amount at end of 1 year.....	\$10 609.00
Interest on this amount = 3 per cent..	<u>318.27</u>
Amount at end of $1\frac{1}{2}$ years.....	\$10 927.27
Interest on this amount for 6 months..	<u>327.82</u>
Amount at end of 2 years.....	\$11 255.09

Although in business practice interest is commonly payable semi-annually, it is in calculations of this kind commonly supposed to be collected and re-invested only at the end of each year. This makes the computation more simple, and gives results nearer to those obtained in practice, because a company cannot generally invest its income immediately. If it had to wait three months to invest each semi-annual instalment of interest collected, the general result would be about the same as if it collected interest only once a year and invested it immediately.

If  $r$  be the rate per cent per annum, the annual rate of increase will be  $\frac{r}{100}$ . Let us put

$$\rho, \text{ the annual rate of increase} = \frac{r}{100};$$

$p$ , the amount at interest at the beginning of the time, or the principal;

$a$ , the amount at the end of one or more years.

Then, at the beginning of first year, principal.....  $\rho$   
 Interest during the year.....  $\rho p$

Amount at end of year.....  $p(1 + \rho)$

Interest on this amount during second year.....  $\rho p(1 + \rho)$

Amount at end of second year,  $(1 + \rho)p(1 + \rho) = p(1 + \rho)^2$

Continuing the process, we see that at the end of  $n$  years the amount will be

$$a = p(1 + \rho)^n. \quad (1)$$

To compute by logarithms, let us take the logarithms of both members. We then have

$$\log a = \log p + n \log (1 + \rho). \quad (2)$$

*Example.* Find the amount of \$1250 for 30 years at 6 per cent per annum.

Here  $\rho = .06$

$$1 + \rho = 1.06$$

$$\log (1 + \rho) = 0.025\ 306 \text{ (end of Table I.)}$$

30

$$n \log (1 + \rho), \quad \overline{0.759\ 18}$$

$$\log p, \quad \overline{3.096\ 91}$$

$$\log a, \quad \overline{3.856\ 09}$$

a, \$7179.50 = required amount.

#### EXERCISES.

1. Find the amount of \$100 for 100 years at 5 per cent compound interest.

2. A man bequeathed the sum of \$500 to accumulate at 4 per cent interest for 80 years after his death. After that time the annual interest was to be applied to the support of a student in Harvard College. What would be the income from the scholarship?

3. If the sum of one cent had been put out at 3 per cent per annum at the Christian era, and accumulated until the year 1800, what would then have been the amount, and the annual interest on this amount?

It is only requisite to give three significant figures, followed by the necessary number of zeros.

4. Solve by logarithms the problem of the horseshoeing, in which a man agrees to pay 1 cent for the first nail, 2 for the second, and so on, doubling the amount for every nail for 32 nails in all.

NOTE. It is only necessary to compute the amount for the 32d nail, because it is easy to see that the amount paid for each nail is 1 cent more than for all the preceding ones.

5. A man lays aside \$1000 as a marriage-portion for his new-born daughter, and invests it so as to accumulate at 8 per cent compound interest. The daughter is married at the age of 25. What does the portion amount to?

6. A man of 30 pays \$2000 in full for a \$5000 policy of insurance on his life. Dying at the age of 80, his heirs receive \$7000, policy and dividends. If the money was worth 4 per cent to him, how much have the heirs gained or lost by the investment?

7. What would have been the answer to the previous question, had the man died at the age of 40, and the amount paid been \$6000?

*Other applications of the formulæ.* By means of the equations (1) and (2) we may obtain any one of the four quantities  $a$ ,  $p$ ,  $\rho$ , and  $n$  when the other three are given.

CASE I. Given the *principal*, *rate of interest*, and *time*, to find the *amount*.

This case is that just solved.

CASE II. Given the *amount*, *time*, and *rate per cent*, to find the *principal*.

*Solution.* Equation (1) gives

$$p = \frac{a}{(1 + \rho)^n}.$$

Taking the logarithms,

$$\log p = \log a - n \log (1 + \rho),$$

by which the computation may be made.

CASE III. Given the *principal*, *amount*, and *time*, to find the *rate*.

*Solution.* Equation (2) gives

$$\log (1 + \rho) = \frac{\log a - \log p}{n} = \frac{1}{n} \log \frac{a}{p}.$$

*Example.* A man wants a principal of \$600 to amount to \$1000 in 10 years. At what rate of interest must he invest it?

*Solution.*

$$\log a = 3.000\ 00$$

$$\log p = 3.990\ 00$$

$$\log \frac{a}{p} = 0.009\ 99$$

$$\frac{1}{10} \log \frac{a}{p} = 0.009\ 99 = \log (1 + \rho).$$

Hence, from last page of logarithms,

$$1 + \rho = 1.052\ 41;$$

and                          rate = 5.241,

or 5½ per cent, nearly.

## EXERCISES.

1. At what rate of interest will money double itself every ten years? Ans. 7.17%.
2. At what rate will it treble itself every 15 years? Ans. 7.59%.
3. A man having invested \$1000, with all the interest it yielded him, for 25 years, finds that it amounts to \$3386. What was the rate of interest? Ans. 5 per cent.
4. A life company issued to a man of 20 a paid-up policy for \$10,000, the single premium charged being \$3150. If he dies at the age of 60, at what rate must the company invest its money to make itself good? Ans. 2.93 per cent.
5. A man who can gain 4 per cent interest wants to invest such a sum that it shall amount to \$5000 when his daughter, now 5 years old, attains the age of 20. How much must he invest? Ans. \$2776.62.
6. How much must a man leave in order that it may amount to \$1,000,000 in 500 years at  $2\frac{1}{2}$  per cent interest? Ans. \$4.36 $\frac{1}{2}$
7. How much if the time is 1000 years, the rate being still  $2\frac{1}{2}$  per cent, and the amount \$1,000,000? Ans. 0.0019 of a cent.
8. A man finds that his investment has increased fivefold in 25 years. What is the average rate of interest he has gained? Ans. 6.65.
9. An endowment of \$7500 is payable to a man when he attains the age of 65. What is its value when he is 45, supposing the rate of interest to be 4 per cent? Ans. \$3423.

**13. Accumulation of an Annuity.**

It is often necessary to ascertain the present or future value of a series of equal annual payments. Thus it is very common to pay a constant annual premium for a policy of life insurance. The value of such a series of payments at any epoch is found by reducing the value of each one to the epoch, allowing for interest, and taking the sum. Supposing the epoch to be the present time, the problem may be stated as follows:

*A man agrees to pay  $p$  dollars a year for  $n$  years, the first payment being due in one year, and the total number of payments  $n$ . What is the present value of all  $n$  payments?*

Putting, as before,  $\rho = \frac{\text{rate of interest}}{100}$ , the present value of  $p$  dollars payable after  $y$  years will, by § 12, Case II., be

$$\frac{p}{(1 + \rho)^y}.$$

Putting in succession,  $y = 1, y = 2, \dots, y = n$ , the sum of the present values is

$$\frac{p}{1+\rho} + \frac{p}{(1+\rho)^2} + \frac{p}{(1+\rho)^3} + \dots + \frac{p}{(1+\rho)^n}.$$

This is a geometrical progression in which

$$\text{First term} = \frac{p}{1+\rho};$$

$$\text{Common ratio} = \frac{1}{1+\rho};$$

$$\text{Number of terms} = n.$$

By *College Algebra*, § 212, the sum of this progression will be

$$\begin{aligned}\Sigma_1 &= \frac{p}{1+\rho} \cdot \frac{1 - \left(\frac{1}{1+\rho}\right)^n}{1 - \frac{1}{1+\rho}} = p \frac{(1+\rho)^n - 1}{(1+\rho)^{n+1} - (1+\rho)^n} \\ &= \frac{p}{(1+\rho)^n} \cdot \frac{(1+\rho)^n - 1}{\rho}.\end{aligned}\quad (1)$$

If the first payment is to be made immediately, instead of at the end of a year, the last or  $n$ th payment will be due in  $n - 1$  years, and the progression will be

$$p + \frac{p}{1+\rho} + \frac{p}{(1+\rho)^2} + \dots + \frac{p}{(1+\rho)^{n-1}}.$$

We find the sum of the geometric progression to be

$$\Sigma_2 = p \frac{(1+\rho)^n - 1}{(1+\rho)^n - (1+\rho)^{n-1}}.\quad (2)$$

### EXERCISES.

1. What is the present value of 15 annual payments of \$85 each, of which the first is due in one year, the rate being 5 per cent?

We find by substitution

$$\begin{aligned}\text{Present value} &= 85 \frac{1.05^{15} - 1}{1.05^{16} - 1.05^{15}} = \frac{85}{1.05^{15}} \cdot \frac{1.05^{15} - 1}{.05} \\ &= \frac{1700 (1.05^{15} - 1)}{(1.05)^{15}}.\end{aligned}$$

$$\log 1.05, \quad 0.021\ 189$$

$$\overline{15}$$

$$1.05^{15}, \quad 2.078\ 95$$

$$1.05^{16} - 1, \quad 1.078\ 95$$

$$\log 1.05^{15}, \quad \overline{0.317\ 84}$$

$$\log, \quad \overline{0.033\ 00}$$

$$\text{co-log } 1.05^{16}, \quad \overline{9.682\ 16}$$

$$\log 1700, \quad \overline{3.230\ 45}$$

$$\text{Value, } \$882.28$$

$$\log \text{value, } \overline{2.945\ 61}$$

2. The same thing being supposed, what would be the present value if the rate of interest were 4 per cent? Ans. \$945.80

3. What is the present value of 25 annual payments of \$1000 each, the first due immediately, if the rate of interest is 3 per cent? Ans. \$17,935

4. A debtor owing \$10,000 wishes to pay it in 10 equal annual instalments, the first being payable immediately. If the rate of interest is 6 per cent, how much should each payment be?

Ans. \$1281.76.

**NOTE.** This problem is the reverse of the given one, since, in the equation (2), we have given  $\Sigma_2 = 10\,000$ ,  $\rho = 0.06$ , and  $n = 10$ , to find  $p$ .

5. The same thing being supposed, what should be the annual payment in case the payments should begin in a year?

Ans. \$1358.69.

*Perpetual annuities.* If the rate of interest were zero, the present value of an infinity of future payments would be infinite. But with any rate of interest, however small, it will be finite. For if, in the first equation (1), we suppose  $n$  infinite,  $\left(\frac{1}{1+\rho}\right)^n$  will converge toward zero, and we shall have

$$\Sigma = \frac{p}{(1+\rho)\left(1 - \frac{1}{1+\rho}\right)} = \frac{p}{\rho}. \quad (3)$$

This result admits of being put into a concise form, thus:

Since  $\Sigma$  is the present value of the perpetual annuity  $p$ , the annual interest on this value will be  $\rho\Sigma$ . But the equation (3) gives  $\rho\Sigma = p$ .

Hence:

*The present value of a perpetual annuity is the sum of which the annuity is the annual interest.*

*Example.* If the rate of interest were  $3\frac{1}{2}$  per cent, the present value of a perpetual annuity of \$70 would be \$2000.

#### EXERCISES.

1. A government owing a perpetual annuity of \$1000 wishes to pay it off by 10 equal annual payments. If the rate of interest is  $\frac{1}{4}$  per cent, what should be the amount of each payment?

Ans. \$3082.30.

2. A government bond of \$100 is due in 15 years with interest at 6 per cent. The market rate of interest having meanwhile fallen to  $3\frac{1}{2}$  per cent, what should be the value of the bond?

**NOTE.** We find, separately, the present value of the 15 annual instalments of interest, and of the principal.

**TABLE II.**  
**MATHEMATICAL CONSTANTS.**

---

**14.** In this table is given a collection of constant quantities which frequently occur in computation, with their logarithms.

The logarithms are given to more than five decimals, in order to be useful when greater accuracy is required. When used in five-place computations, the figures following the fifth decimal are to be dropped, and the fifth decimal is to be increased by unity in case the figure next following is 5 or any greater one.

## TABLES III. AND IV.

### LOGARITHMS OF TRIGONOMETRIC FUNCTIONS.

---

**15.** By means of these tables the logarithms of the six trigonometric functions of any angle may be found.

The logarithm of the function instead of the function itself is given, because the latter is nearly always used as a factor.

We begin by explaining Table IV., because Table III. is used only in some special cases where Table IV. is not convenient.

I. *Angles less than 45°.* If the angle of which a function is sought is less than 45°, we seek the number of degrees at the top of the table and the minutes in the left-hand column. Then in the line opposite these minutes we find successively the sine, the tangent, the cotangent, and the cosine of the angle, as given at the heading of the page.

*Example.*

$\log \sin 31^\circ 27' = 9.717\ 47;$
$\log \tan 31^\circ 27' = 9.786\ 47;$
$\log \cotan 31^\circ 27' = 0.213\ 53;$
$\cos 31^\circ 27' = 9.931\ 00.$

The sine, tangent, and cosine of this angle being all less than unity, the true mantissae of the logarithm are negative; they are therefore increased by 10, on the system already explained.

If the secant or cosecant of an angle is required, it can be found by taking the arithmetical complement of the cosine or sine. It is shown in trigonometry that

$$\text{secant} = \frac{1}{\text{cosine}},$$

and

$$\text{cosecant} = \frac{1}{\text{sine}}.$$

Therefore  $\log \text{secant} = 0 - \log \text{cosine} = \text{co-log cosine};$   
 $\log \text{cosec} = 0 - \log \text{sine} = \text{co-log sine}.$

We thus find       $\log \sec 31^\circ 27' = 0.069\ 00;$   
 $\log \text{cosec } 31^\circ 27' = 0.282\ 53.$

After each column, upon intermediate lines, is given the differ-

ence between every two consecutive logarithms, in order to facilitate interpolation.

In the case of tangent and cotangent, only one column of differences is necessary for both functions. *since  $\tan = \frac{\text{opp}}{\text{adj}} = \frac{\text{opp}}{\text{adj}^2}$*

If we use no fractional parts of minutes, no interpolation is necessary; but if decimals of a minute are employed, we can interpolate precisely as in taking out the logarithms of numbers.

Where the differences are very small they are sometimes omitted.

Tables of proportional parts are given in the margin, the use of which is similar to those given with the logarithms of numbers.

*Example 1.* To find the log sin of  $31^\circ 27' .7$ .

We have from the tables,  $\log \sin 31^\circ 27' = 9.717\ 47$

Under diff. 20, P.P. for 7,                                    14

$$\log \sin 31^\circ 27'.7 = 9.717\ 61$$

*Ex. 2.* To find  $\log \cot 15^\circ 44'.34$ .

The tables give  $\log \cot 15^\circ 44' = 0.550\ 19$

Under diff. 48, opposite 0.3, P.P.,                            - 14.4

"                         "                          $0.4 \div 10$ ,                                    - 1.9

$$\log \cot 15^\circ 44'.34,                                    0.550\ 03$$

Since the tabular quantity diminishes as the angle increases, the proportional parts are subtractive.

### EXERCISES.

Find from the tables:

1.  $\log \cot 43^\circ 29'.3$ ;
2.  $\log \tan 43^\circ 29'.3$ ;
3.  $\log \cos 27^\circ 10'.6$ ;
4.  $\log \sin 27^\circ 10'.6$ ;
5.  $\log \tan 12^\circ 9'.43$ ;
6.  $\log \cot 12^\circ 9'.43$ .

In the case of sines and tangents of small angles the differences vary so rapidly that in most cases the exact difference will not be found in the table of proportional parts. In this case, if the proportional parts are made use of, a double interpolation will generally be necessary to find the fraction of a minute corresponding to a given sine or tangent. If only tenths of minutes are used, an expert computer will find it as easy to multiply or divide mentally as to refer to the table.

II. *Angles between  $45^\circ$  and  $90^\circ$ .* It is shown in trigonometry that if we compute the values of the trigonometric functions for the

first  $45^\circ$ , we have those for the whole circle by properly exchanging them in the different parts of the circle. First, if we have

$$\alpha + \beta = 90^\circ,$$

then  $\alpha$  and  $\beta$  are complementary functions, and

$$\sin \beta = \cos \alpha;$$

$$\tan \beta = \cotan \alpha.$$

Therefore if our angle is between  $45^\circ$  and  $90^\circ$ , we may find its complement. Entering the table with this complement, the complementary function will then be the required function of the angle.

*Example.* To find the sine of  $67^\circ 23'$ , we may enter the table with  $22^\circ 37'$  ( $= 90^\circ - 67^\circ 23'$ ) and take out the cosine of  $22^\circ 37'$ , which is the required sine of  $67^\circ 23$ .

To save the trouble of doing this, the complementary angles and the complementary denominations of the functions are given at the bottom of the page.

The minutes corresponding to the degrees at the bottom are given on the right hand. Therefore:

*To find the trigonometric functions corresponding to an angle between  $45^\circ$  and  $90^\circ$ , we take the degrees at the bottom of the page and the minutes in the right-hand column. The values of the four functions log sine, log tangent, log cotangent, and log cosine, as read at the bottom of the page, are then found in the same line as the minutes.*

*Example 1.* For  $52^\circ 59'$  we find

$$\log \sin = 9.90225;$$

$$\log \tan = 0.12262;$$

$$\log \cot = 9.87738;$$

$$\log \cos = 9.77963.$$

*Ex. 2.* To find the trigonometric functions of  $77^\circ 17'.28$ .

	sin.	tan.	cot.	cos.
$77^\circ 17'$	9.98921	0.64653	9.35347	9.34268
P.P. for 0.2	+ 0.6	+ 11.8	- 11.8	- 11.2
" 0.08	+ 0.2	+ 4.7	- 4.7	- 4.5
	9.98922	0.64670	9.35330	9.34252

Then  $\log \sec = \text{co-log cos} = 0.65748$ ;

$\log \text{cosec} = \text{co-log sin} = 0.01078$ .

### EXERCISES.

Find the logarithms of the six functions of the following angles:

1.  $45^\circ 50'.74$ ;

3.  $74^\circ 0'.68$ ;

2.  $48^\circ 49'.37$ ;

4.  $83^\circ 59'.62$ .

To find &  $< 90^\circ$  which corresp to a given  $\log f\ell$   
 The method of int. of Ex 2. above is reversed.  
 Find &  $< 90^\circ$  corresp to  $\log \sin = 9.90243$ ,  
 $\log \cos = 9.90243$ ,  $\log \tan = 0.02481$ ,  $\log \cot = 9.87743$ ,  
 $\log \sec = 0.65748$ ,  $\log \cosec = 0.01078$ .

Sines ✓

III. When the angle exceeds  $90^\circ$ .

**RULE.** Subtract from the angle the greatest multiple of  $90^\circ$  which it contains.

If this multiple is  $180^\circ$ , enter the table with the excess of the angle over  $180^\circ$  and take out the functions required, as if this excess were itself the angle.

If the multiple is  $90^\circ$  or  $270^\circ$ , take out the complementary function to that required.

By then assigning the proper algebraic sign, as shown in trigonometry, the complete values of the function will be obtained.

The computer should be able to assign the proper algebraic sign according to the quadrant, without burdening his memory with the special rules necessary in each case. This he can do by carrying in his mind's eye the following scheme. He should have at command the arrangement of the four quadrants as usually represented in trigonometry, so as to know, when an angle is stated, where it will fall relatively to the horizontal and vertical lines through the centre of the circle. Then, in the case of—

*Sine or cosecant.* If the angle is above the horizontal line (which it is between  $0^\circ$  and  $180^\circ$ ), the sine is positive; if below, negative.

*Cosine or secant.* If the angle is to the right of the vertical central line (as it is in the first and fourth quadrants), the cosine and secant are positive; if to the left (as in the second and third quadrants), negative.

*Tangent or cotangent.* Through the opposite first and third quadrants, positive; through the opposite second and fourth quadrants, negative. *Don't forget to take note.*

*Example 1.* To find the tangent and cosine of  $122^\circ 44'$ . Subtracting  $90^\circ$ , we enter the table with  $32^\circ 44'$  and find

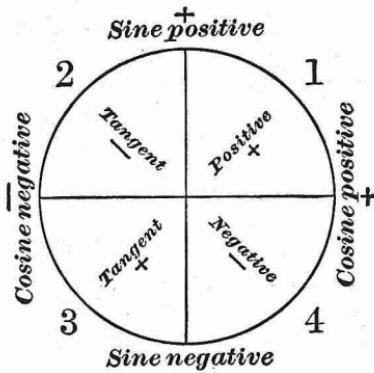
$$\log \cot 32^\circ 44' = 0.19192;$$

$$\log \sin 32^\circ 44' = 9.73298.$$

'Therefore, writing the algebraic sign before the logarithm, we have

$$\log \tan 122^\circ 44' = + 0.19192;$$

$$\log \cos 122^\circ 44' = + 9.73298.$$



*Ex. 2.* To find the sine and cotangent of  $322^\circ 58'$ .

Entering the table with  $52^\circ 58' = 322^\circ 58' - 270^\circ$ , and taking out the complementary functions, we find

$$\log \sin 322^\circ 58' = + 9.779\ 80; \sim$$

$$\log \cot 322^\circ 58' = + 0.122\ 36. \sim$$

*Ex. 3.* To find the sine and tangent of  $253^\circ 5'$ .

Entering with  $73^\circ 5'$ , we take out the sine and tangent, finding

$$\log \sin 253^\circ 5' = + 9.880\ 79; \sim$$

$$\log \tan 253^\circ 5' = + 0.516\ 93.$$

*Ex. 4.* To find the six trigonometric functions of  $152^\circ 38'$ . We have

$$\log \sin 152^\circ 38' = \log \cos 62^\circ 38' \text{ pos.} = + 9.662\ 46;$$

$$\log \cos 152^\circ 38' = \log \sin 62^\circ 38' \text{ neg.} = + 9.948\ 45; \sim$$

$$\log \tan 152^\circ 38' = \log \cot 62^\circ 38' \text{ neg.} = + 9.714\ 01; \sim$$

$$\log \cot 152^\circ 38' = \log \tan 62^\circ 38' \text{ neg.} = + 0.285\ 99; \sim$$

$$\log \sec = \text{co-log cos} = + 0.051\ 55; \sim$$

$$\log \cosec = \text{co-log sin} = + 0.337\ 54.$$

### EXERCISES.

Find the six trigonometric functions of the following angles:

$$276^\circ 29'.3;$$

$$66^\circ 0'.5;$$

$$96^\circ 59'.8;$$

$$252^\circ 20'.3;$$

$$318^\circ 10'.7;$$

$$- 25^\circ 22'.2;$$

$$- 155^\circ 30'.7.$$

### 16. Method of Writing the Algebraic Signs.

As logarithms are used in computation, they may always be considered positive. It is true that the logarithms of numbers less than unity are in reality negative, but, for convenience in calculation, we increase them by 10, so as to make them positive.

The number corresponding to a given logarithm may, in computation, be positive or negative. (There are two ways of distinguishing the algebraic sign of the number, between which the computer may choose for himself.

I. Write the algebraic sign of the number before the logarithm.

As usually interpreted, the algebraic sign written thus would apply to the logarithm, which it does not. It is therefore necessary for the

computer to bear in mind that the sign belongs, not to the logarithm, as written, but to the number.

II. Write the letter  $n$  after the logarithm when the number is negative. This plan is theoretically the best, but, should the computer accidentally omit the letter, the number will be treated as positive, and a mistake will be made. It therefore requires vigilance on his part. An improvement would be to write a letter not likely to be mistaken for  $n$ ,  $s$  for instance, after all positive logarithms.

### 17. To Find the Angle Corresponding to a Given Trigonometric Function.

Disregarding algebraic signs, there will always be four angles corresponding to each function, one in each quadrant. These angles will be:

- The smallest angle, as found in the table;
- This angle increased by  $180^\circ$ ;
- The complementary angle increased by  $90^\circ$ ;
- The complementary angle increased by  $270^\circ$ .

For instance, for the angle of which  $\log \tan$  is 0.611 92, we find  $76^\circ 16'$ . But we should get this same tangent for  $103^\circ 44'$ ,  $256^\circ 16'$ , and  $283^\circ 44'$ .

Of the four functions corresponding to the four angles, two will always be positive and two negative; so that, in reality, there will only be two angles corresponding to a function of which both the sign and the absolute value are given. These values are found by selecting from the four possible ones the two for which the functions have the given algebraic sign. After selecting them, they may be checked by the following theorems, which are easily deduced from the relations between the values of each function as given in trigonometry:

*The sum of the two angles corresponding to the same sine is  $180^\circ$  or  $540^\circ$ .*

*The sum of the two angles corresponding to the same cosine is  $360^\circ$ .*

*The difference of the two angles corresponding to the same tangent is  $180^\circ$ .*

Which of the two possible angles is to be chosen depends upon the conditions of the problem or the nature of the figure to which the angle belongs. If neither the conditions nor the figure decide the question, the problem is essentially ambiguous, and either both angles are to be taken.

## EXERCISES.

Find the pairs of values of the angle  $\alpha$  from the following values of the trigonometric functions:

- |                                       |                                       |
|---------------------------------------|---------------------------------------|
| 1. $\log \sin \alpha = + 9.902\ 43;$  | 12. $\log \sec \alpha = + 0.221\ 06;$ |
| 2. $\log \sin \alpha = - 9.902\ 43;$  | 13. $\log \sec \alpha = - 0.221\ 06;$ |
| 3. $\log \cos \alpha = + 9.902\ 43;$  | 14. $\log \sec \alpha = - 0.099\ 20;$ |
| 4. $\log \cos \alpha = - 9.902\ 43;$  | 15. $\log \sec \alpha = + 0.123\ 46;$ |
| 5. $\log \tan \alpha = + 0.143\ 16;$  | 16. $\log \sin \alpha = + 8.990\ 30;$ |
| 6. $\log \tan \alpha = - 0.143\ 16;$  | 17. $\log \sin \alpha = - 8.990\ 30;$ |
| 7. $\log \cot \alpha = + 0.143\ 16;$  | 18. $\log \cos \alpha = + 9.218\ 67;$ |
| 8. $\log \cot \alpha = - 0.143\ 16;$  | 19. $\log \cos \alpha = - 9.218\ 67;$ |
| 9. $\log \tan \alpha = - 9.024\ 81;$  | 20. $\log \tan \alpha = - 9.136\ 90;$ |
| 10. $\log \tan \alpha = - 0.975\ 19;$ | 21. $\log \tan \alpha = + 9.136\ 90;$ |
| 11. $\log \tan \alpha = + 0.975\ 19;$ | 22. $\log \cot \alpha = + 9.136\ 90.$ |

### 18. Cases when the Function is very Small or Great.

When the angle of which we are to find the functions approaches to zero, the logarithms of the sine, tangent, and cotangent vary so rapidly that their values to five figures cannot be readily interpolated. The same remark applies to the cosine, cotangent, and tangent of angles near  $90^\circ$  or  $270^\circ$ . The mode of proceeding in these cases will depend upon circumstances.

In the use of five-place logarithms, there is little advantage in carrying the computations beyond tenths of minutes, though the hundredths may be found when the tangent or cotangent is given. Where greater accuracy than this is required, six- or seven-place tables must be used.

If the angles are only carried to tenths of minutes, there is no necessity for taking out the sine, tangent, or cotangent to more than four decimals when the angle is less than  $3^\circ$ , and three decimals suffice for angles less than  $30'$ . The reason is that this number of decimals then suffice to distinguish each tenth of minute.

When the decimals are thus curtailed, an expert computer will be able to perform the multiplication and division for the tenths of minutes mentally. If, however, this is inconvenient, the following rule may be applied.

To find the log sine or log tangent of an angle less than  $3^\circ$  to four places of decimals:

**RULE.** Enter the table of logarithms of numbers with the value

of the angle expressed in minutes and tenths, and take out the logarithm.

To this logarithm add the quantity 6.4637.

The sum will be the log sine, and the log tangent may be assumed to have the same value.

*Example 1.* To find  $\log \sin 1^\circ 22'.6$ .

$$1^\circ 22'.6 = 82'.6$$

$$\log 82'.6 = 1.9170$$

$$\text{constant, } 6.4637$$

$$\log \sin 1^\circ 22'.6, \quad \underline{\quad 8.3807}$$

This rule is founded on the theorem that the sines and tangents of very small arcs may be regarded as equal to the arcs themselves. Since, in using the trigonometric functions, the radius of the circle is taken as unity, an arc must be expressed in terms of the unit radius when it is to be used in place of its sine or tangent. Now, it is shown in trigonometry that the unit radius is equal to  $57^\circ.2958$  or  $3437'.747$  or  $206264''.8$ . Hence we must divide the number of angular units in the angle by the corresponding one of these coefficients to obtain the length of the corresponding arcs in unit radius. Now,

$$\log 3437.747 = 3.5363$$

$$\text{co-log.} \dots \dots \dots \quad 6.4637$$

which may be added instead of subtracting the logarithm.

To find the cosine of an angle very near  $90^\circ$ , we find the sine of its complement, which will then be a very small angle, positive or negative.

#### EXERCISES.

Find to four places of decimals:

1.  $\log \sin 22'.73;$
2.  $\log \sin 1^\circ 1'.12;$
3.  $\log \cos 90^\circ 0'.78;$
4.  $\log \tan 88^\circ 59'.35;$
5.  $\log \cot 90^\circ 28'.76;$
6.  $\log \cos 89^\circ 22'.23;$
7.  $\log \sin 0^\circ 0'.25.$

If an angle corresponding to a given sine or tangent is required, the rule is:

*From the given log sine or tangent subtract 6.4637 or add 3.5363. The result is the logarithm of the number of minutes.*

Of course this rule applies only to angles less than  $2^\circ$ , in the value of which only tenths of minutes are required.

## EXERCISES.

Find  $\alpha$  from:

- |                                 |                                  |
|---------------------------------|----------------------------------|
| 1. $\log \sin \alpha = 7.2243;$ | 3. $\log \tan \alpha = -2.8816;$ |
| 2. $\log \cot \alpha = 2.8816;$ | 4. $\log \cos \alpha = 6.9218.$  |

When the small angle is given in seconds. Although the computer may take out his angles to tenths of minutes, cases often arise in which a small angle is given in seconds, or degrees, minutes, and seconds, and in which the trigonometric function is required to five decimals. In this case the preceding method may not always give accurate results, because the arc and its sine or tangent may differ by a greater amount than the error we can admit in the computation.

Table III. is framed to meet this case. The following are the quantities given:

*In the second column:* The argument, in degrees and minutes, as already explained for Table IV.

*In the first column:* This argument reduced to seconds. From this column the number of seconds in an arc of less than  $2^\circ$ , given in degrees, minutes, and seconds, may be found at sight.

*Example.* How many seconds in  $1^\circ 28' 39''$ ? In the table, before  $1^\circ 28'$ , we find  $5280''$ , which being increased by  $39''$  gives  $5319''$ , the number required.

*Col. 3.* The logarithm of the sine of the angle. This is the same as in Table IV.

*Col. 4.* The value of  $\log \text{sine} - \log \text{arc}$ ; that is, the difference between the logarithm of the sine and the logarithm of the number of seconds in the angle.

*Col. 5.* The same quantity for the tangent.

*Cols. 6 and 7.* The complements of the preceding logarithms, distinguished by accents.

The use of the tables is as follows.

To find the sine or tangent of an angle less than  $2^\circ$ :

*Express the angle in seconds by the first two columns of the table.*

*Write down the logarithm in column S or column T, according as the sine or a tangent is required.*

*Find from Table I. the logarithm of the number of seconds.*

*Adding this logarithm to S or T, the sum will be the log sine or log tangent.*

*Example.* Find  $\log \sin 1^\circ 2' 47''.9$ .

S, 4.685 55

$$1^\circ 2' 47''.9 = 3767''.9; \log, 3.576\ 10$$

$$\log \sin 1^\circ 2' 47''.9, \underline{8.261\ 65}$$

To find the arc corresponding to a given sine or tangent:

Find in the column  $L. \sin$ . the quantity next greater or next smaller than the given logarithm.

Take the corresponding value of  $S'$  or  $T'$  according as the given \*\* function is a sine or tangent, and add it to the given function.

The sum is the logarithm of the number of seconds in the required angle.

Example. Given  $\log \tan x = 8.40125$ , to find  $x$ .

$$\begin{array}{r} \log \tan x, 8.40125 \\ T', 5.31433 \\ \hline \log x, 3.71558 \\ x = 5194''.9 = 1^\circ 26' 34''.9, \text{ from col. 2.} \end{array}$$

### EXERCISES.

Find:

1.  $\log \sin 0^\circ 20' 20''.25$ ;
2.  $\log \tan 0^\circ 0' 1''.2273$ ;
3.  $\log \sin 1^\circ 59' 22''.7$ ;
4.  $\log \tan 1^\circ 0' 59''.7$ .

Find  $x$  from:

1.  $\log \tan x = 8.42796$ ;
2.  $\log \tan x = 7.42796$ ;
3.  $\log \tan x = 6.42796$ ;
4.  $\log \sin x = 5.35435$ ;
5.  $\log \sin x = 4.22619$ ;
6.  $\log \sin x = 8.54078$ .

When the cosine or cotangent of an angle near  $90^\circ$  or  $270^\circ$  is required, we take its difference from  $90^\circ$  or  $270^\circ$ , and find the complementary function by the above rules.

Remark. The use of the logarithms of the trigonometric functions is so much more extensive than that of the functions themselves that the prefix "log" is generally omitted before the designation of the logarithmic function, where no ambiguity will result from the omission.

\* The radian measure of the small  $t''$  is  $\frac{t''}{206265}$

$\log \sin \frac{t''}{206265} = x$  (almost unity)

$x$  can be computed for small  $t''$  say between 0 and  $2^\circ$   
 $\therefore \log \sin t'' = t'' \frac{x}{206265} \therefore \log \sin t'' = \log t'' + \log \frac{x}{206265}$

where  $s = \log \frac{x}{206265}$

Coll. 2 Table 2 contains values of  $s$  for each minute of arc bet 0 and  $2^\circ$

$\therefore s = \log \sin t'' - \log t''$

$t'' = \log \tan t'' - \log t''$

Hence the values in Table 2 are increased by 10

TABLE V.  
NATURAL SINES AND COSINES.

---

**19.** This table gives the actual numerical values of the sine and cosine for each minute of the quadrant.

To find the sine or cosine corresponding to a given angle less than  $45^\circ$ , we find the degrees at the top of a pair of columns and the minutes on the left.

In the two columns under the degrees and in the line of minutes we find first the sine and then the cosine, as shown at the head of the column.

A decimal point precedes the first printed figure in all cases, except where the printed value of the function is unity.

If the given angle is between  $45^\circ$  and  $90^\circ$ , find the degrees at the bottom and the minutes at the right.

Of the two numbers above the degrees, the right-hand one is the sine and the left-hand one the cosine.

For angles greater than  $90^\circ$  the functions are to be found according to the precepts given in the case of the logarithms of the sines and tangents.

TABLE VI.  
ADDITION AND SUBTRACTION LOGARITHMS.

---

**20.** Addition and subtraction logarithms are used to solve the problem: *Having given the logarithms of two numbers, to find the logarithm of the sum or difference of the numbers.*

The problem can of course be solved by finding the numbers corresponding to the logarithms, adding or subtracting them, and taking out the logarithm of their sum or difference. The table under consideration enables the result to be obtained by an abbreviated process.

I. *Use in addition.* The principle on which the table is constructed may be seen by the following reasonings. Let us put

$$S = a + b,$$

$a$  and  $b$  being two numbers of which the logarithms are given. We shall have

$$S = a \left(1 + \frac{b}{a}\right) = a(1 + x);$$

putting, for clearness,  $x = \frac{b}{a}$ .

We then have

$$\log S = \log a + \log(1 + x).$$

Since  $\log a$  and  $\log b$  are both given, we can find  $\log x$  from the equation

$$\log x = \log b - \log a,$$

which is therefore a known quantity.

Now, for every value of  $\log x$  there will be one definite value of each of the quantities  $x$ ,  $1 + x$ , and  $\log(1 + x)$ . Therefore a table may be constructed showing, for every value of  $\log x$ , the corresponding value of  $\log(1 + x)$ .

Such a table is Table VI.

The argument, in column *A*, being  $\log x$ , the quantity *B* in the table is  $\log(1 + x)$ .

*Example.*  $\log 0.25 = 0.39794$ .

Entering the table with  $A = 0.39794$ , we find

$$B = 0.09691,$$

which is the logarithm of 1.25.

Therefore, entering the table with  $\log x$  as the argument, we take out  $\log(1+x)$ , which added to  $\log a$  will give  $\log S$ .

We have therefore the following precept for using the table in addition:

*Take the difference of the two given logarithms.*

*Enter the table with this difference as the argument A, and take out the quantity B.*

*Adding B to the subtracted logarithm, the sum will be the required logarithm of the sum.*

It is indifferent which logarithm is subtracted, but convenience in interpolating will be gained by subtracting the greater logarithm from the lesser increased by 10. The number  $B$  will then be added to the greater logarithm.

*Example.* Given  $\log m = 1.629\ 74$ ,  $\log n = 2.203\ 86$ ; find  $\log(m+n)$ .

The required logarithm is found in either of the following two ways:

$$\log m, 1.629\ 74 \quad (1) \qquad \log B, 0.676\ 76 \quad (4)$$

$$\log n, 2.203\ 86 \quad (2) \qquad \log m, 1.629\ 74 \quad (1)$$

$$B, 0.102\ 64 \quad (4) \qquad \log n, 2.203\ 86 \quad (2)$$

$$A = \log m \div n, 9.425\ 88 \quad (3) \qquad \log n \div m, 0.574\ 12 \quad (3)$$

$$\log(m+n), 2.306\ 50 \quad (5) \qquad \log(m+n), 2.306\ 50 \quad (5)$$

The figures in parentheses show the order in which the numbers are written.

#### EXERCISES.

Log  $a$  and log  $b$  having the following values, find  $\log(a+b)$ .

$$1. \log a = 1.700\ 37; \log b = 0.921\ 69.$$

$$2. \log a = 0.624\ 60; \log b = 9.881\ 26.$$

$$3. \log a = 9.791\ 86; \log b = 9.322\ 09.$$

$$4. \log a = 1.601\ 62; \log b = 1.306\ 06.$$

$$5. \log a = 0.792\ 90; \log b = 9.221\ 27.$$

$$6. \log a = 0.601\ 32; \log b = 9.001\ 68.$$

$$7. \log a = 4.796\ 43; \log b = 3.981\ 86.$$

II. *Use in subtraction.* The problem is, having given  $\log a$  and  $\log b$ , to find the logarithm of

$$D = a - b.$$

We have

$$D = b \left( \frac{a}{b} - 1 \right);$$

whence

$$\log D = \log b + \log \left( \frac{a}{b} - 1 \right).$$

Since  $\log \frac{a}{b}$  is found by subtracting  $\log b$  from  $\log a$ , if we can find  $\log \left( \frac{a}{b} - 1 \right)$  from  $\log \frac{a}{b}$ , the problem will be solved.

From the construction of the table already explained, if we have

$$B = \log \frac{a}{b},$$

we must have

$$A = \log \left( \frac{a}{b} - 1 \right).$$

We now have the following precept for subtraction:

*Subtract the lesser of the given logarithms from the greater.*

*Enter the table so as to find the difference of the logarithms in the numbers B of the table.*

*Add the corresponding value of A to the lesser of the given logarithms. The sum will be the logarithm of the difference.*

*Example.* Find  $\log(n - m)$  in the example of the preceding section.

$$\log n, 2.203\ 86 \quad (1)$$

$$\log m, 1.629\ 74 \quad (2)$$

$$\underline{A, 0.439\ 45 \quad (4)}$$

$$\log \frac{n}{m} = B, 0.574\ 12 \quad (3)$$

$$\log(n - m), \underline{\quad \quad \quad} \quad (5)$$

### EXERCISES.

Find the logarithms of the differences of the quantities  $a$  and  $b$  in the preceding section.

*Remark.* In the use of addition and subtraction logarithms, the precepts apply to *numerical* sums and differences, without respect to the algebraic signs of the quantities. For example, the algebraic difference between + 1473 and - 29 462 is to be found by addition, and the algebraic sum of a positive and negative quantity by subtraction.

*Case where the quotient is large.* Near the end of the table,  $A$  and  $B$  become nearly equal; the structure of the table is therefore changed so as to simplify its use. It is evident that if  $b$  is very small compared with  $a$ , the logarithms of  $a + b$  and  $a - b$  will not differ much from the logarithm of  $a$  itself. Hence, in this case, we shall have smaller numbers to use if we can find the quantity which must be added to  $\log a$  to give  $\log(a + b)$ , or subtracted from

$\log a$  to give  $\log(a - b)$ . Now, the equations already written give, when  $a > b$ ,

$$\log a = \log b + A,$$

$$\log(a + b) = \log b + B;$$

whence, by subtraction,

$$\log(a + b) - \log a = B - A,$$

or  $\log(a + b) = \log a + B - A$ . (with Arg.  $A$ )

We find in the same way,

$$\log(a - b) = \log a - (B - A). \quad (\text{with Arg. } B)$$

Now, whenever  $\log a - \log b$  is greater than 1.65, we shall find it more convenient to take out  $B - A$  from the table than either  $A$  or  $B$ . We notice that the last two figures of  $B$  in this part of the table vary slowly, and we need only attend to them in interpolating. For instance, in the horizontal line corresponding to  $A = 1.66$  we find:

for $A = 1.660\ 00$ ;	$B = 1.669\ 40$ ;	$B - A = .009\ 40$ ;
.661\ 00;	.670\ 38;	.009\ 38;
.662\ 00;	.671\ 36;	.009\ 36;
.663\ 00;	.672\ 33;	.009\ 33;
.664\ 00;	.673\ 31;	.009\ 31;
.665\ 00;	.674\ 29;	.009\ 29;
etc.	etc.	etc.

The interpolation of  $B - A$  is now very easy whether the quantity given is  $A$  or  $B$ . We note that  $B - A$  has but three significant figures, of which the first is found in column zero, and the other two are the last two figures of  $B$  as printed.

As an example, let us find  $\log(a + b)$  from

$$\log a = 2.791\ 63$$

$$\log b = 1.128\ 19$$

$$A = 1.663\ 44$$

Entering the table with this value of  $A$ , we find by column 0 that  $B - A$  falls between .009 40 and .009 19. Following the horizontal line  $A = 1.66$  to column 3 and interpolating the last two figures between 33 and 31 for .44, with the difference — 2, we find

$$B - A = .009\ 32$$

Then

$$\log a = 2.791\ 63$$

$$\log(a + b) = 2.800\ 95$$

Next, if  $\log(a - b)$  is required, we have to find the difference 1.663 44 in the part  $B$  of the table. We find in the table:

$$\text{for } B = 1.662\ 55; \quad B - A = .009\ 55;$$

$$\text{for } B = 1.663\ 53; \quad B - A = .009\ 53.$$

Therefore

$$\text{for } B = 1.663\ 44; \quad B - A = .009\ 53.$$

Subtracting this from  $\log a$ , we have

$$\log(a - b) = 2.782\ 10.$$

#### EXERCISES.

Find  $\log(a + b)$  and  $\log(a - b)$  from:

$$8. \quad \log a = 0.367\ 02; \quad \log b = 8.462\ 83.$$

$$9. \quad \log a = 0.001\ 26; \quad \log b = 8.329\ 07.$$

$$10. \quad \log a = 2.069\ 23; \quad \log b = 0.110\ 85.$$

$$11. \quad \log a = 5.807\ 35; \quad \log b = 3.838\ 09.$$

For values of  $A$  and  $B$  greater than 2.00, the table is so arranged that no interpolation at all is necessary. The computer has only to find what value of  $A$  or  $B$  given in the table comes *nearest* his value of  $\log a - \log b$  and take the corresponding value of  $B - A$ . He must remember that column  $A$  is to be entered for addition, and  $B$  for subtraction.

In this part of the table  $A$  and  $B$  are given to fewer than five decimals; because five decimals are not necessary to give  $B - A$  with accuracy. The nearer the end of the table is approached, the fewer the decimals necessary in taking the difference.

*Example.* Find  $\log(a + b)$  and  $\log(a - b)$  from

$$\log a = 1.265\ 32$$

$$\log b = 9.222\ 30$$

$$\log a - \log b, \underline{\hspace{2cm}} 2.043\ 02$$

Entering column  $A$  with this difference, we find the nearest tabular value of  $A$  to be 2.0425, to which corresponds  $B - A = .003\ 92$ . Hence

$$\log(a + b) = 1.265\ 32 + .003\ 92 = 1.269\ 24.$$

Entering column  $B$  with the same difference, we find  $B - A = .003\ 95$ ; whence

$$\log(a - b) = 1.265\ 32 - .003\ 95 = 1.261\ 37.$$

#### EXERCISES.

Find  $\log(a + b)$  and  $\log(a - b)$  from:

$$1. \quad \log a = 4.069\ 05; \quad \log b = 2.001\ 32.$$

$$2. \quad \log a = 3.926\ 93; \quad \log b = 1.201\ 59.$$

$$3. \quad \log a = 3.061\ 64; \quad \log b = 0.126\ 15.$$

$$4. \quad \log a = 1.220\ 68; \quad \log b = 7.321\ 56.$$

$$5. \quad \log a = 0.693\ 17; \quad \log b = 6.010\ 23.$$

$$6. \quad \log a = 2.306\ 20; \quad \log b = 7.023\ 01.$$

*Case of nearly equal numbers.* Near the beginning of the table the reverse is true: it is not possible to find  $A$  with accuracy to five places of decimals. But here the value of  $A$  taken from the tables, though it be found to only two, three, or four places of decimals, will give as accurate a result as the computation of  $a$  and  $b$  to five places will admit of. Let us suppose, for example, that we have to find  $\log(a - b)$  from

$$\log a = 9.883\ 15$$

$$\log b = 9.882\ 96$$

$$B = \overline{0.000\ 19}$$

We find

$$A = 6.64 - 10;$$

whence

$$\log(a - b) = 6.52 - 10.$$

We note that the value of  $A$  may be 6.63 or 6.65 as well as 6.64, so that the result cannot be carried beyond two decimals. To show that these two are as accurate as the work admits of, we find the natural numbers  $a$  and  $b$  from Table I.

$$a = 0.764\ 10$$

$$b = 0.763\ 77$$

$$a - b = \overline{0.000\ 33}$$

Since  $a - b$  has but two significant figures, and the first of these is less than 5, two figures in the logarithm are all that can be accurate.

TABLE VII.  
SQUARES OF NUMBERS.

---

**21.** By means of this table the square of any number less than 1000 may be found at sight, and that of any number less than 10 000 by a simple and easy interpolation.

The first page gives the squares of the first 100 numbers, which it is often convenient to have by themselves.

On the second and third pages (98 and 99) the hundreds of the number to be squared are found at the tops of the several columns, and the tens and units in the left-hand column. The first three or four figures of the square are in the column under the hundreds, and opposite the tens and units, and the last two figures on the right of the page after the column 9 ♦♦♦

*Examples.* The square of 634 is 401 956;

$$\begin{array}{lll} “ & “ & 329 “ 108 241; \end{array}$$

$$\begin{array}{lll} “ & “ & 265 “ 70 225; \end{array}$$

$$\begin{array}{lll} “ & “ & 153 “ 23 409; \end{array}$$

$$\begin{array}{lll} “ & “ & 999 “ 998 001. \end{array}$$

The same table may be used for any number of three significant figures by attention to the position of the decimal-point. Thus:

$$51100^2 = 2611210\,000;$$

$$511^2 = 261\,121;$$

$$51.1^2 = 2611.21;$$

$$5.11^2 = 26.1121;$$

$$0.511^2 = 0.261121.$$

When there are four significant figures, an interpolation may be executed in several ways. If  $n$  be the nearest number the square of which is found in the table, and  $h$  the excess of the given number over this, so that  $n + h$  is the number whose square is required, we shall have

$$\begin{aligned} (n+h)^2 &= n^2 + 2nh + h^2 = n^2 + h(2n+h) \\ &= n^2 + h(N+n); \end{aligned}$$

where  $N = n + h$ , the given number.

We may therefore find the square of 257.4 in the following way:

$$\begin{array}{r} 257^2 = 66\,049 \\ 514.4 \times .4 = \underline{\quad 205.76} \\ (257.4)^2 = \underline{\quad 66\,254.76} \end{array}$$

To find the square of 9037 we proceed thus:

$$\begin{array}{r} 9037 \\ 9030^2 = 81\,540\,900 \\ \hline 18067 \times 7 = \underline{\quad 126\,469} \\ 9037^2 = \underline{\quad 81\,667\,369} \end{array}$$

In many cases only one more figure will be required in the square than in the given number. The square can then be interpolated with all required accuracy by the differences, the last two figures of which are found in the last column of the table, while the remaining figures are found by taking the difference between two consecutive numbers in the principal column.

To return to the last example, we find the difference between  $257^2$  and  $258^2$  to be 515, the first figure being the difference between 660 and 665, and the last two, 15, in the last column. Then

$$\begin{array}{r} 257^2 = 66\,049 \\ 515 \times 0.4 = \underline{\quad 206} \\ (257.4)^2 = \underline{\quad 66\,255} \end{array}$$

—which is correct to the nearest unit.

It will be remarked that the two methods are substantially the same when only five figures are sought in the result. The substantial identity rests upon the general theorem that

*The difference of the squares of two consecutive numbers is equal to the sum of the numbers.*

We prove this theorem thus:

$$(n+1)^2 - n^2 = 2n + 1 = n + (n+1).$$

When the tabular difference is taken in the way already described, it will often happen that the difference between the numbers in the columns of hundreds is to be diminished by unity. Thus, although  $4173 - 4160 = 13$ , the difference between  $645^2$  and  $646^2$  is not 1391, but 1291. These cases are noted by the asterisk after the number in the last column.

The squares of numbers of more than four figures may be found in the same way, but in such cases it will generally be easier to use logarithms than the table of squares.

## TABLE VIII.

**TO CONVERT HOURS, MINUTES, AND SECONDS  
INTO DECIMALS OF A DAY, AND *VICE VERSA*.**

---

**22.** The familiar method of solving this problem is to convert the seconds into decimals of a minute, and the minutes into decimals of an hour, by dividing by 60, and then the hours into decimals of a day by dividing by 24. The reverse problem is solved by multiplying by 24, 60, and 60.

Table VIII. enables us to perform these operations without division. Column *D* gives each hundredth of a day, but its numbers may also be regarded as ten thousandths or millionths of a day, according to which of the following three columns is used. In column *H.M.S.* are found the hours, minutes, and seconds corresponding to these hundredths. In the next column is one hundredth of column *H.M.S.*, or the minutes and seconds in the number of ten thousandths of a day in column *D*. Finally, column  $\frac{H.M.S.}{100^2}$  shows the number of seconds in the number of millionths of a day found in column *D*.

*Example.* To convert  $0^d.532\ 946$  into hours, minutes, and seconds.

$$\begin{array}{rcl}
 0^d.53 & = & 12^h\ 43^m\ 12^s \\
 .002\ 9 & = & 4^m\ 10^s.56 \\
 .000\ 046 & = & 3^s.97 \\
 \hline
 0^d.532\ 946 & = & 12^h\ 47^m\ 26^s.53
 \end{array}$$

It will be seen that we divide the figures of the given decimal of a day into pairs, and enter the three columns of time with these three pairs in succession.

If seven decimals are given, we may interpolate the last number, as in taking out a logarithm.

*Example.* Convert  $0^d.050\ 762\ 7$ .

$$\begin{array}{rcl}
 0^d.05 & = & 1^h\ 12^m\ 0^s \\
 .000\ 7 & = & 1^m\ 0^s.48 \\
 .000\ 062 & = & 5^s.36 \\
 .000\ 000\ 7 = .7 \times .08 = & & 0^s.06 \\
 \hline
 & & 1^h\ 13^m\ 5^s.90
 \end{array}$$

In practice the computer will perform the interpolation mentally, adding  $.7 \times .08 = .06$  to the number 5.36 of the table in his head, and writing down 5<sup>o</sup>.42 as the last quantity to be added.

### EXERCISES.

Convert into hours, minutes, and seconds:

1. 0<sup>d</sup>.203 079 2;
2. 0<sup>d</sup>.783 605 8;
3. 0<sup>d</sup>.010 203 4;
4. 0<sup>d</sup>.990 990 9.

To use the table for the reverse operation, we proceed as in the following example:

It is required to convert 17<sup>h</sup> 29<sup>m</sup> 30<sup>s</sup>.93 into decimals of a day. Looking in the table, we find that the required decimal is between 0.72 and 0.73. Hence the first two figures are 0.72, the equivalent of 17<sup>h</sup> 16<sup>m</sup> 48<sup>s</sup>. Subtracting the latter from the given number, we have a remainder 12<sup>m</sup> 42<sup>s</sup>.93, to be sought for in column  $\frac{H.M.S.}{100}$ . This gives 88 as the next two figures. Subtracting the equivalent of .0088 or 12<sup>m</sup> 40<sup>s</sup>.32, we have left 2<sup>s</sup>.61, which we are to seek in column  $\frac{H.M.S.}{100^2}$ . We find the corresponding number of column D to be 302. Hence

$$17^h 29^m 30^s.93 = 0^d.728\ 830\ 2.$$

In solving this problem the computer should be able, after a little practice, to perform the subtractions and carry the remainders mentally, thus saving himself the trouble of writing down the numbers.

### EXERCISES.

Take the answers obtained from the four preceding exercises, subtract each result from 24<sup>h</sup> 0<sup>m</sup> 0<sup>s</sup>, change the remainder to decimals of a day, and see if when added to the decimals of the preceding exercises the sum is 1<sup>d</sup>.000 000 0, as it should be.

## TABLE IX.

TO CONVERT TIME INTO ARC, AND *VICE VERSA.*

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**23.** In astronomy the right ascensions of the heavenly bodies are commonly given in hours, minutes, and seconds, the circumference being divided into 24 hours, each hour into 60 minutes, and each minute into 60 seconds.

Since  $360^\circ$  = one circumference,  
we have  $1^h = 15^\circ$ ;  
 $1^m = 15'$ ;  
 $1^s = 15''$ ;

the signs  $^h$ ,  $^m$ , and  $^s$  indicating hours, minutes, and seconds of time.

Hence we may change time into arc by multiplying by 15, and arc into time by dividing by 15, the denominations being changed in each case. Table IX. enables us to do this by simple addition and subtraction by a process similar to that employed in changing hours, minutes, and seconds into decimals of a day.

To turn time into arc, we find in the table the whole number of degrees contained in the time denomination next smaller than the given one, and subtract the former time denomination from the latter.

Next we find the minutes of arc corresponding to the given time next smaller than the remainder, and again subtract.

Lastly we interpolate the seconds corresponding to the second remainder.

*Example.* Change  $15^h 29^m 46.^s.24$  to arc.

Given time,  $15^h 29^m 46.^s.24$

The table gives  $232^\circ = 15^h 28^m$

Remainder,	<hr/>	$1^m 46.^s.24$
------------	-------	----------------

The table gives	$26' =$	<hr/>	$1^m 44^s$
-----------------	---------	-------	------------

Remainder,	<hr/>	$2.^s.24 = 33''.6$
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Hence

$$15^h 29^m 46.^s.24 = 232^\circ 26' 33''.6.$$

The computer should be able to go through this operation without writing down anything but the result.

The operation of changing arc into time is too simple to require description, but it is more necessary to write down the work.

#### EXERCISES.

Change the following times to arc, and then check the results by changing the arcs into time and seeing whether the original times are reproduced:

1.  $7^{\text{h}} 29^{\text{m}} 17^{\text{s}}.86$ ;
2.  $0^{\text{h}} 4^{\text{m}} 0^{\text{s}}.25$ ;
3.  $12^{\text{h}} 4^{\text{m}} 0^{\text{s}}.25$ ;
4.  $13^{\text{h}} 48^{\text{m}} 16^{\text{s}}.40$ ;
5.  $19^{\text{h}} 7^{\text{m}} 59^{\text{s}}.92$ .

## TABLE X.

### TO CONVERT MEAN TIME INTO SIDEREAL TIME, AND SIDEREAL INTO MEAN TIME.

---

**24.** Since  $365\frac{1}{4}$  solar days =  $366\frac{1}{4}$  sidereal days (very nearly), any period expressed in mean time may be changed to sidereal time by increasing it by its  $\frac{1}{365.25}$  part, and an interval of sidereal time may be changed to mean time by diminishing it by its  $\frac{1}{366.25}$  part.

The first part of the table gives, for each 10 minutes of the argument, its  $\frac{1}{365.25}$  part, by which it is to be increased. The second part of the table gives the  $\frac{1}{366.25}$  part of the argument.

The small table in the margin shows the change for periods of less than 10 minutes.

*Example 1.* To change  $17^{\text{h}} 48^{\text{m}} 36\text{s}.7$  of mean time to sidereal time.

Given mean time,	$17^{\text{h}} 48^{\text{m}} 36\text{s}.70$
Corr. for $17^{\text{h}} 40^{\text{m}}$ ,	$2^{\text{m}} 54\text{s}.13$
Corr. for $8^{\text{m}} 37\text{s}$ ,	$1\text{s}.41$
Sidereal time,	$17^{\text{h}} 51^{\text{m}} 32\text{s}.24$

*Ex. 2.* To change this interval of sidereal time back to mean time.

Corr. for $17^{\text{h}} 50^{\text{m}}$ ,	$- 2^{\text{m}} 55\text{s}.29$
Corr. for $1^{\text{m}} 32\text{s}$ ,	$- 0\text{s}.25$
	$- 2^{\text{m}} 55\text{s}.54$
Sidereal time,	$17^{\text{h}} 51^{\text{m}} 32\text{s}.24$
Mean time,	$17^{\text{h}} 48^{\text{m}} 36\text{s}.70$

#### EXERCISES.

Change to sidereal time:

- |   |  |
|---|--|
| 1. $3^{\text{h}} 42^{\text{m}} 36\text{s}.5$ m. t.; | 3. $22^{\text{h}} 3^{\text{m}} 5\text{s}.61$ m. t. |
| 2. $18^{\text{h}} 46^{\text{m}} 29\text{s}.82$ "    | 4. $0^{\text{h}} 1^{\text{m}} 12\text{s}.55$ "     |

Change to mean time:

- |  |
|--|
| 5. $0^{\text{h}} 7^{\text{m}} 16\text{s}.3$ sidereal time; |
| 6. $22^{\text{h}} 17^{\text{m}} 29\text{s}.65$ "           |

## OF DIFFERENCES AND INTERPOLATION.\*

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### 25. General Principles.

We call to mind that the object of a mathematical table is to enable one to find the value of a function corresponding to any value whatever of the variable argument. Since it is impossible to tabulate the function for all values of the argument, we have to construct the table for certain special values only, which values are generally equidistant. For example, in the tables of sines and cosines in the present work the values of the functions are given for values of the argument differing from each other by one minute.

The process of finding the values of functions corresponding to values of the argument intermediate between those given is called *interpolation*.

We have already had numerous examples of interpolation in its most simple form; we have now to consider the subject in a more general and extended way.

In the first place, we remark that, in strictness, no process of interpolation can be applicable to all cases whatever. From the mere facts that

To the number 2 corresponds the logarithm 0.301 03,

" " " 3 " " " 0.477 12,

we are not justified in drawing any conclusion whatever respecting the logarithms of numbers between 2 and 3. Hence some one or more hypotheses are always necessary as the base of any system of interpolation. The hypotheses always adopted are these two:

1. *That, supposing the argument to vary uniformly, the function varies according to some regular law.*

2. *That this law may be learned from the values of the function given in the table.*

These hypotheses are applied in the process of *differencing*, the

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\* The study of this subject will be facilitated by first mastering so much of it as is contained in the author's College Algebra, §§ 299-302.

It is also recommended to the beginner in the subject that, before going over the algebraic developments, he practise the methods of computation according to the rules and formulæ, so as to have a clear practical understanding of the notation. He can then more readily work out the developments.

nature of which will be seen by the following example, where it is applied to the logarithms of the numbers from 30 to 37:

	Function.	$\Delta'$	$\Delta''$	$\Delta'''$	$\Delta^{(4)}$
log 30.	1.477 12	+ 1424	- 45	+ 2	
" 31.	1.491 36	+ 1379	- 43	+ 4	+ 2
" 32.	1.505 15	+ 1336	- 39	+ 1	- 3
" 33.	1.518 51	+ 1297	- 38	+ 2	+ 1
" 34.	1.531 48	+ 1259	- 36	+ 3	+ 1
" 35.	1.544 07	+ 1223	- 33		
" 36.	1.556 30	+ 1190			
" 37.	1.568 20				

The column  $\Delta'$  gives each difference between two consecutive values of the function, formed by subtracting each number from that next following. These differences are called *first differences*.

The column  $\Delta''$  gives the difference between each two consecutive first differences. These are called *second differences*.

In like manner the numbers in the succeeding columns, when written, are called *third differences*, *fourth differences*, etc.

Now if, in continuing the successive orders of differences, we find them to continually become smaller and smaller, or to converge toward zero, this fact shows that the values of the functions follow a regular law, and the first hypothesis is therefore applicable.

In order to apply interpolation we must then assume that the intermediate values of the function follow the same law. The truth of this assumption must be established in some way before we can interpolate with mathematical rigor, but in practice we may suppose it true in the absence of any reason to the contrary.

**26. Effect of errors in the values of the functions.** In the preceding example it will be noticed that if we continue the orders of differences beyond the fourth, they will begin to increase and become irregular. This arises from the imperfections of the logarithms, owing to the omission of decimals beyond the fifth, already described in § 11.

When we find the differences to become thus irregular, we must be able to judge whether this irregularity arises from actual errors in the original numbers, which ought to be corrected, or from the small errors necessarily arising from the omission of decimals.

The great advantage of differencing is that any error, however small, in the quantities differenced, unless it follows a regular law, will be detected by the differences. To show the reason of this, we investigate what effect errors in the given functions will have upon the successive orders of differences.

**THEOREM.** *The differences of the sum of two quantities are equal to the sums of their differences.*

*General proof.* Let

$f_1, f_2, f_3, \dots$ , etc., be one set of functions;  
 $f'_1, f'_2, f'_3, \dots$ , etc., another set.

$f_1 + f'_1, f_2 + f'_2, f_3 + f'_3, \dots$ , etc., will then be their sums.

In the first of the following columns we place the first differences of  $f$ , in the second those of  $f'$ , and in the third those of  $f + f'$ , each formed according to the rule:

$$\begin{array}{lll} f_2 - f_1 & f'_2 - f'_1 & f_2 + f'_2 - (f_1 + f'_1) \\ f_3 - f_2 & f'_3 - f'_2 & f_3 + f'_3 - (f_2 + f'_2) \\ \text{etc.} & \text{etc.} & \text{etc.} \end{array}$$

It will be seen that the quantities in the third column are the sums of those in the first two.

#### NUMERICAL EXAMPLE.

$f$	$\Delta'$	$f'$	$\Delta'$	$f+f'$	$\Delta'$
14		1		15	
+ 25		+ 2		+ 27	
39		3		42	
+ 11		+ 3		+ 14	
50		6		56	
- 51		+ 4		- 47	
- 1				9	

We see that the third set of values of  $\Delta'$  follow the theorem.

Because the second differences are the differences of the first, the third the differences of the second, etc., it follows that the theorem is true for differences of any order.

Now when we write a series of functions in which the decimals exceeding a certain order are omitted, we may conceive each written number to be composed of the algebraic sum of two quantities, namely:

1. The true mathematical value of the function.
2. The negative of the omitted decimals.

*Example.* In the preceding collection of logarithms, since the true value of  $\log 30$  is  $1.477\ 121\ 3\dots$ , we may conceive the quantity written to be

$$1.477\ 12 = \log 30 - .000\ 001\ 3\dots$$

Hence the differences actually written are the differences of the true logarithms minus the differences of the errors. Now suppose the errors to be alternately  $+ 0.5$  and  $- 0.5$  = the point marking off the last decimal. Their differences will then be as follows:

$$\begin{array}{llll} f' & \Delta' & \Delta'' & \Delta''' \\ - 0.5 & + 1 & + 2 & - 4 \\ + 0.5 & - 1 & - 2 & + 4 \\ - 0.5 & + 1 & + 2 & - 4 \\ + 0.5 & - 1 & - 2 & + 4 \\ \text{etc.} & \text{etc.} & \text{etc.} & \text{etc.} \end{array}$$

It is evident that the  $n$ th order of differences of the errors are equal to  $\pm 2^{n-1}$ . Hence, in this case, if the  $n$ th order of differences of the true values of the function were zero, still, in consequence of the omission of decimals, the actual differences of the  $n$ th order would be  $2^{n-1}$ .

This, however, is a very extreme case, since it is beyond all probability that the errors should alternate in this way. A more probable average example will be obtained by supposing a single number to have an error of 0.5, while the others are correct. We shall then have:

$f'$	$\Delta'$	$\Delta''$	$\Delta'''$	$\Delta^{iv}$	$\Delta^v$
0	0	0	+ 0.5	+ 0.5	- 2.5
0	0	+ 0.5	+ 0.5	- 2.0	- 2.5
0.5	+ 0.5	- 1.0	- 1.5	+ 3.0	+ 5.0
0	- 0.5	+ 0.5	+ 1.5	- 2.0	- 5.0
0	0	0	- 0.5	+ 0.5	+ 2.5

In this case the maximum value of the difference of the  $n$ th order is 1.5 in the differences of the third order, 3 in those of the fourth, 5 in those of the fifth, etc. Its general expression is

$$\frac{1}{2} \frac{n(n-1)(n-2)\dots(n-s+1)}{1.2.3\dots s},$$

where  $n$  is the order of differences, and

$$s = \frac{n}{2} \text{ or } \frac{n-1}{2}$$

according as  $n$  is even or odd. Thus:

$$\begin{aligned}\Delta' &= \frac{1}{2}; \\ \Delta'' &= \frac{1}{2} \cdot \frac{2}{1} = 1; \\ \Delta''' &= \frac{1}{2} \cdot \frac{3}{1} = 1.5; \\ \Delta^{iv} &= \frac{1}{2} \cdot \frac{4 \cdot 3}{1 \cdot 2} = 3; \\ \Delta^v &= \frac{1}{2} \cdot \frac{5 \cdot 4}{1 \cdot 2} = 5; \\ &\text{etc.} \quad \text{etc.}\end{aligned}$$

This being about the average case, in actual practice the differences may be two or three times as great without necessarily implying an error greater than 0.5 in the numbers written.

We have now the following general rule for judging whether a series of numbers do really follow a uniform law.

*Difference the series until we reach an order of differences in which the + and - signs either alternate or follow each other irregularly.*

If none of the differences of this order expressed in units of the last place of decimals exceed the limit

$$\frac{n(n-1)\dots(n-s+1)}{1\cdot 2\cdot 3\dots s}$$

—that is, the value of the largest binomial coefficient of the  $n$ th order—the given numbers may be assumed to follow a regular law, and therefore to be correct to a unit in the last figure.

If some differences exceed this limit, their quotient by the above binomial coefficient may be considered to show the maximum error with which the number opposite it is probably affected.

We can thus detect an isolated error in a series of numbers with great certainty. Suppose, for example, an error of 2 in some number of the series. Differencing the series 0, 0, 0, 2, 0, 0, 0, we shall find the four largest differences of the fifth order to be  $-10$ ,  $+20$ ,  $-20$ ,  $+10$ , which would enable us to hit at once upon the erroneous number and judge of the magnitude of its error.

An error near the beginning and end of the series of numbers of which the differences are taken cannot be detected by the differences unless it is considerable. If, for instance, the first or last number is in error by 1, the error of each order of differences will only be 1, as we may easily see by the following example:

$$\begin{array}{cccc} f' & \Delta' & \Delta'' & \Delta''' \\ \frac{1}{0} - \frac{1}{0} + \frac{1}{0} - 1 & \text{etc.} \end{array}$$

It is only in those differences which are on or near the same line as the numbers which are magnified in the way we have shown. But at the beginning and end of the series we cannot determine these differences.

Examining the various tables of differences, we see that  $n$  numbers have  $n-1$  first differences,  $n-2$  second differences, and so on, the number diminishing by 1 with each succeeding order. Hence, unless the number of given functions exceeds the index expressing the order of differences which we have to form, no certain conclusion can be drawn.

What is here said of the correctness of the numbers when the differences run properly must be understood as applicable to isolated errors only. If all the numbers were subject to an error following a regular law, this error would not be detected by the differences because, from the nature of the case, the latter only show deviations from some regular law.

## 27. Fundamental Formulae of Interpolation.

We suppose a series of numbers to be differenced in the way already shown, and the various differences to be designated as in the following scheme, which is supposed to be a selection from a series preceding and following it.

Function.	1st Diff.	2d Diff.	3d Diff.	4th Diff.	5th Diff.
$u_{-2}$	$\Delta'_{-2}$	$\Delta''_{-2}$	$\Delta'''_{-2}$	$\Delta^{iv}_{-2}$	$\Delta^v_{-2}$
$u_{-1}$	$\Delta'_{-1}$	$\Delta''_{-1}$	$\Delta'''_{-1}$	$\Delta^{iv}_{-1}$	$\Delta^v_{-1}$
$u_0$	$\Delta'_0$	$\Delta''_0$	$\Delta'''_0$	$\Delta^{iv}_0$	$\Delta^v_0$
$u_1$	$\Delta'_{\frac{1}{2}}$	$\Delta''_{\frac{1}{2}}$	$\Delta'''_{\frac{1}{2}}$	$\Delta^{iv}_{\frac{1}{2}}$	$\Delta^v_{\frac{1}{2}}$
$u_2$	$\Delta'_{\frac{3}{2}}$	$\Delta''_{\frac{3}{2}}$	$\Delta'''_{\frac{3}{2}}$	$\Delta^{iv}_{\frac{3}{2}}$	$\Delta^v_{\frac{3}{2}}$
$u_3$	$\Delta'_{\frac{5}{2}}$	$\Delta''_{\frac{5}{2}}$	$\Delta'''_{\frac{5}{2}}$	$\Delta^{iv}_{\frac{5}{2}}$	$\Delta^v_{\frac{5}{2}}$
$u_4$	$\Delta'_{\frac{7}{2}}$	$\Delta''_{\frac{7}{2}}$			
etc.	etc.	etc.	etc.	etc.	etc.

It will be seen that the lower indices are chosen so as to show on which line a difference of any order falls. Thus all quantities with index 2 are on one horizontal line, those with index  $\frac{5}{2} = 2\frac{1}{2}$  are half a line below, etc. This notation is a little different from that used in algebra, but the change need not cause any confusion.

It is shown in algebra that if  $n$  be any index, we have

$$u_n = u_0 + n\Delta'_{\frac{1}{2}} + \frac{n(n-1)}{1.2} \Delta''_{\frac{1}{2}} + \frac{n(n-1)(n-2)}{1.2.3} \Delta'''_{\frac{1}{2}} + \text{etc.}; \quad (a)$$

the notation being changed as in the preceding scheme.

Now the fundamental hypothesis of interpolation is that this formula, which can be demonstrated only for integral values of  $n$ , is true also for fractional values; that is, for values of the function  $u$  between those given in the table or in the above scheme. We therefore suppose this formula to express the value of the function  $u$  for any value of  $n$  between 0 and 1.

For values between  $+1$  and  $+2$  we have only to increase the indices of  $u$  and its differences by unity, thus:

$$u_{1+n} = u_1 + n\Delta'_{\frac{1}{2}} + \frac{n(n-1)}{1.2} \Delta''_{\frac{1}{2}} + \text{etc.},$$

and by supposing  $n$  to increase from 0 to 1 in this formula we shall have values of  $u$  from  $u_1$  to  $u_2$ .

Increasing the indices again—that is, applying our general formulae to a row of quantities one line lower—we shall have

$$u_{2+n} = u_2 + n\Delta'_{\frac{1}{2}} + \frac{n(n-1)}{1 \cdot 2} \Delta''_{\frac{1}{2}} + \text{etc.}$$

The equation (a) is known as *Newton's formula of interpolation*.

## 28. Transformations of the Formula of Interpolation.

In the equation (a) and those following it, the formula of interpolation is not in its most convenient form. We shall therefore transform it so that the differences employed shall be symmetrical with respect to the functions between which the interpolation is to be made.

In working these transformations we shall suppose the sixth and following orders of differences to be so small as not to affect the result. These differences being supposed zero, any two consecutive fifth differences may be supposed equal.

*First transformation.* Let us first find what the original formula (a) will become when, instead of using the series of differences

$$\Delta'_{\frac{1}{2}}, \Delta''_{\frac{1}{2}}, \Delta'''_{\frac{1}{2}}, \Delta^{IV}_{\frac{1}{2}}, \text{ etc.,}$$

we use

$$\Delta'_{\frac{1}{2}}, \Delta''_0, \Delta'''_{\frac{1}{2}}, \Delta^{IV}_0, \text{ etc.}$$

To effect the transformation we must find the values of the first series of differences in terms of the second, and substitute them in the formula (a).

We find, by the mode of forming the differences,

$$\Delta''_{\frac{1}{2}} = \Delta''_0 + \Delta'''_{\frac{1}{2}};$$

$$\Delta'''_{\frac{1}{2}} = \Delta'''_{\frac{1}{2}} + \Delta^{IV}_{\frac{1}{2}};$$

$$= \Delta'''_{\frac{1}{2}} + \Delta^{IV}_0 + \Delta^{IV}_{\frac{1}{2}};$$

$$\Delta^{IV}_{\frac{1}{2}} = \Delta^{IV}_0 + \Delta^{IV}_{\frac{1}{2}} + \Delta^{IV}_{\frac{1}{2}};$$

for which, because we suppose the values of  $\Delta^V$  to be equal, we may put

$$\Delta^{IV}_{\frac{1}{2}} = \Delta^{IV}_0 + 2\Delta^{IV}_{\frac{1}{2}};$$

$$\Delta^{IV}_{\frac{1}{2}} = \Delta^{IV}_{\frac{1}{2}}.$$

Making these substitutions in (a), we have

$$\begin{aligned} u_n = & u_0 + n\Delta'_{\frac{1}{2}} + \frac{n(n-1)}{1 \cdot 2} (\Delta''_0 + \Delta'''_{\frac{1}{2}}) \\ & + \frac{n(n-1)(n-2)}{1 \cdot 2 \cdot 3} (\Delta'''_{\frac{1}{2}} + \Delta^{IV}_0 + \Delta^{IV}_{\frac{1}{2}}) \\ & + \frac{n(n-1)(n-2)(n-3)}{1 \cdot 2 \cdot 3 \cdot 4} (\Delta^{IV}_0 + 2\Delta^{IV}_{\frac{1}{2}}) \\ & + \frac{n(n-1) \dots (n-4)}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5} \Delta^{IV}_{\frac{1}{2}}. \end{aligned}$$

Reducing by collecting the coefficients of equal differences, we find

$$\begin{aligned} u_n - u_0 &= n \Delta'_{\frac{1}{2}} + \frac{n(n-1)}{1.2} \Delta''_{\frac{1}{2}} + \frac{(n+1)n(n-1)}{1.2.3} \Delta'''_{\frac{1}{2}} \\ &\quad + \frac{(n+1)n(n-1)(n-2)}{1.2.3.4} \Delta^{IV}_0 \\ &\quad + \frac{(n+2)(n+1)n(n-1)(n-2)}{1.2.3.4.5} \Delta^V_{\frac{1}{2}}. \end{aligned} \quad (b)$$

*Second transformation.* Next, instead of the series of this last formula, (b),

$$\Delta'_{\frac{1}{2}}, \Delta''_0, \Delta'''_{\frac{1}{2}}, \Delta^{IV}_0, \text{ etc.,}$$

let us use

$$\Delta'_{-\frac{1}{2}}, \Delta''_0, \Delta'''_{-\frac{1}{2}}, \Delta^{IV}_0, \text{ etc.}$$

To effect this transformation we substitute in (b) for  $\Delta'_{\frac{1}{2}}$ ,  $\Delta''_{\frac{1}{2}}$ , etc.,

$$\Delta'_{\frac{1}{2}} = \Delta'_{-\frac{1}{2}} + \Delta''_0;$$

$$\Delta'''_{\frac{1}{2}} = \Delta'''_{-\frac{1}{2}} + \Delta^{IV}_0;$$

$$\Delta^V_{\frac{1}{2}} = \Delta^V_{-\frac{1}{2}}.$$

The series (b) then changes into

$$\begin{aligned} u_n - u_0 &= n \Delta'_{-\frac{1}{2}} + \frac{n(n+1)}{1.2} \Delta''_0 + \frac{(n+1)n(n-1)}{1.2.3} \Delta'''_{-\frac{1}{2}} \\ &\quad + \frac{(n+2)(n+1)n(n-1)}{1.2.3.4} \Delta^{IV}_0 \\ &\quad + \frac{(n+2)(n+1)n(n-1)(n-2)}{1.2.3.4.5} \Delta^V_{-\frac{1}{2}}. \end{aligned} \quad (c)$$

*Third transformation. Stirling's formula.* We effect a third transformation by taking the half sum of the equations (b) and (c), which gives us a formula perfectly symmetrical with respect to the lines of differences, namely,

$$\begin{aligned} u_n - u_0 &= n \frac{\Delta'_{-\frac{1}{2}} + \Delta'_{\frac{1}{2}}}{2} + \frac{n^2}{2} \Delta''_0 + \frac{n(n^2-1)}{1.2.3} \frac{\Delta'''_{-\frac{1}{2}} + \Delta'''_{\frac{1}{2}}}{2} \\ &\quad + \frac{n^2(n^2-1)}{1.2.3.4} \Delta^{IV}_0 + \frac{n(n^2-1)(n^2-4)}{1.2.3.4.5} \frac{\Delta^V_{-\frac{1}{2}} + \Delta^V_{\frac{1}{2}}}{2} + \text{etc.,} \end{aligned} \quad (d)$$

which is known as *Stirling's formula of interpolation*.

It will be seen that we have put

$$n^2 - 1 \text{ for } (n+1)(n-1),$$

$$n^2 - 4 \text{ for } (n+2)(n-2),$$

etc. etc.

*Fourth transformation.* In the equation (b), instead of the series of differences

$$\Delta'_{\frac{1}{2}}, \Delta''_0, \Delta'''_{\frac{1}{2}}, \Delta^{IV}_0, \text{ etc.,}$$

let us use

$$\Delta'_{\frac{1}{2}}, \Delta''_0, \Delta'''_{\frac{1}{2}}, \Delta^{IV}_0, \text{ etc.}$$

To effect this we put

$$\begin{aligned}\Delta''_0 &= \Delta''_1 - \Delta'''_{\frac{1}{2}}; \\ \Delta^{1v}_0 &= \Delta^{1v}_1 - \Delta^v_{\frac{1}{2}}.\end{aligned}$$

Making these substitutions in (b), it becomes

$$\begin{aligned}u_n - u_0 &= n\Delta'_{\frac{1}{2}} + \frac{n(n-1)}{1.2}\Delta''_1 + \frac{n(n-1)(n-2)}{1.2.3}\Delta'''_{\frac{1}{2}} \\ &\quad + \frac{(n+1)n(n-1)(n-2)}{1.2.3.4}\Delta^{1v}_1 \\ &\quad + \frac{(n+1)n(n-1)(n-2)(n-3)}{1.2.3.4.5}\Delta^v_{\frac{1}{2}}. \quad (e)\end{aligned}$$

*Fifth transformation. Bessel's formula.* Let us take half the sum of the equations (e) and (b). We then have

$$\begin{aligned}u_n - u_0 &= n\Delta'_{\frac{1}{2}} + \frac{n(n-1)}{1.2}\frac{\Delta''_0 + \Delta''_1}{2} + \frac{n(n-1)(n-\frac{1}{2})}{1.2.3}\Delta'''_{\frac{1}{2}} \\ &\quad + \frac{(n+1)n(n-1)(n-2)}{1.2.3.4}\frac{\Delta^{1v}_0 + \Delta^{1v}_1}{2} \\ &\quad + \frac{(n+1)n(n-1)(n-2)(n-\frac{1}{2})}{1.2.3.4.5}\Delta^v_{\frac{1}{2}}, \quad (f)\end{aligned}$$

which is commonly known as *Bessel's formula of interpolation*, and which is the one most convenient to use in practice.

In applying this formula to find a value of the function intermediate between two given values, we must always suppose the index 0 to apply to the given value next preceding that to be found, and the index 1 to apply to that next following. The quantity  $n$  will then be a positive proper fraction.

**29. Example of interpolation to halves.** If we increase the logarithms of 30, 31, etc., already given, by unity, we shall have the logarithms of 300, 310, 320, etc. It is required to find, by interpolation, the logarithms of the numbers half way between the given ones (omitting the first and last), namely, the logarithms of 315, 325, 335, etc.

Here, the required quantities depending upon arguments half way between the given ones, we have  $n = \frac{1}{2}$ , and the values of the Besselian coefficient, so far as wanted, are

$$\begin{aligned}\frac{n(n-1)}{2} &= -\frac{1}{8}; \\ \frac{n(n-1)(n-\frac{1}{2})}{6} &= 0.\end{aligned}$$

The subsequent terms are neglected, being insensible. So, if we put  $a_0$  and  $a_1$  for any consecutive two of the numbers 300, 310, etc., we have

$$\left. \begin{aligned} \log(a_0 + 5) &= \log a_0 + \left( \frac{1}{2} \Delta'_{\frac{1}{2}} - \frac{1}{8} \frac{\Delta''_0 + \Delta''_1}{2} \right) \\ \text{and} \quad \log(a_1 - 5) &= \log a_1 - \left( \frac{1}{2} \Delta'_{\frac{1}{2}} + \frac{1}{8} \frac{\Delta''_0 + \Delta''_1}{2} \right), \end{aligned} \right\} \quad (h)$$

where we put  $\Delta'_{\frac{1}{2}}$  for that first difference between  $a_0$  and  $a_1$ .

These two formulæ are two expressions for the same quantity because  $a_0 + 5 = a_1 - 5$ . They are both used in such a way as to provide a check upon the accuracy of the work. For this purpose we compute the two quantities

$$\left. \begin{aligned} \log(a_0 + 5) - \log a_0 &= \frac{1}{2} \Delta'_{\frac{1}{2}} - \frac{1}{8} \frac{\Delta''_0 + \Delta''_1}{2}, \\ \log a_1 - \log(a_0 + 5) &= \frac{1}{2} \Delta'_{\frac{1}{2}} + \frac{1}{8} \frac{\Delta''_0 + \Delta''_1}{2}. \end{aligned} \right\} \quad (k)$$

The most convenient and expeditious way of doing the work is shown in the accompanying table, where we give every figure which it is necessary to write, besides those found on p. 57. The following is the plan of computation:

No.	Log.	Diff.	$\frac{1}{2} \Delta'_{\frac{1}{2}}$	$\frac{1}{8} \frac{\Delta''_0 + \Delta''_1}{2}$	$\frac{\Delta''_0 + \Delta''_1}{2}$
310	2.491 36	695			
315	.498 31	684	+ 689.5	- 5.5	- 44
320	.505 15	673			
325	.511 88	663	668.0	- 5.1	- 41
330	.518 51	653			
335	.525 04	644	648.5	- 4.8	- 38
340	.531 48	634			
345	.537 82	625	629.5	- 4.6	- 37
350	.544 07	616			
355	.550 23	607	+ 611.5	- 4.3	- 34
360	2.556 30				

We compute the right-hand column by the formula

$$\frac{\Delta''_0 + \Delta''_1}{2} = \Delta''_0 + \frac{1}{2} \Delta'''_{\frac{1}{2}} = \Delta''_1 - \frac{1}{2} \Delta'''_{\frac{1}{2}},$$

using the values of  $\Delta$  given in the scheme, p. 57.

This mode of computing the half sum of two numbers which are nearly equal is easier than adding and dividing by 2.

In the next two columns to the left, the sixth place of decimals

is added in order that the errors may not accumulate by the addition of several quantities. This precaution should always be taken when the interpolated quantities are required to be as accurate as the given ones.

The fourth column from the right is formed by adding and subtracting the numbers of the second and third columns according to the formula (*k*). The additional figure is now dropped, because no longer necessary for accuracy. The numbers thus formed are the first differences of the series of logarithms found by inserting the interpolated logarithms between the given ones, as will be seen by equation (*k*).

We write the first logarithm of the series, namely,

$$\log 310 = 2.49136,$$

and then form the subsequent ones by continual addition of the differences, thus:

$$\begin{aligned}\log 315 &= \log 310 + 695; \\ \log 320 &= \log 315 + 684; \\ \log 325 &= \log 320 + 673; \\ &\text{etc.} \quad \text{etc.} \quad \text{etc.}\end{aligned}$$

If the work is correct, the alternate logarithms will agree with the given ones in the former table.

The continuance of the above process for a few more numbers, say up to 450, is recommended to the student as an exercise.

**30. Interpolation to thirds.** Let us suppose the value of a quantity to be given for every third day, and the value for every day to be required. By putting  $n = \frac{1}{3}$  and applying formula (*f*) to each successive given quantity, we shall have the value for each day following one of those given, and by putting  $n = \frac{2}{3}$  we shall have values for the second day following, which will complete the series. But the interpolation can be executed by a much more expeditious process, which consists in computing the middle difference of the interpolated quantities and finding the intermediate differences by a secondary interpolation.

Let us put

- $f_0, f_1, f_2, \dots$ , etc., the given series of quantities;
- $f_0, f_1, f_2, f_3, f_4, \dots$ , etc., the required interpolated series;
- $\Delta', \Delta'', \dots$ , etc., the first differences, second differences, etc., of the given series;
- $\delta', \delta'', \dots$ , etc., the first differences, second differences, etc., of the interpolated series.

We may then put

$$\left. \begin{aligned} f_2 - f_0 &= \Delta'_{\frac{1}{2}} && (\text{in the given series}); \\ f_1 - f_0 &= \delta'_{\frac{1}{2}} \\ f_2 - f_1 &= \delta'_{\frac{3}{2}} \\ f_3 - f_2 &= \delta'_{\frac{5}{2}} \end{aligned} \right\} (\text{in the interpolated series}).$$

We shall then have

$$\delta'_{\frac{1}{2}} + \delta'_{\frac{3}{2}} + \delta'_{\frac{5}{2}} = \Delta'_{\frac{1}{2}}.$$

The value of  $f_1 - f_0 = \delta'_{\frac{1}{2}}$  is given by putting  $n = \frac{1}{2}$  in the Bes-selian formula ( $f$ ). Thus we find

$$\begin{aligned} \delta'_{\frac{1}{2}} &= \frac{1}{3} \Delta'_{\frac{1}{2}} - \frac{1}{9} \frac{\Delta''_0 + \Delta''_1}{2} + \frac{1}{162} \Delta'''_{\frac{1}{2}} \\ &\quad + \frac{5}{243} \frac{\Delta^{1v}_0 + \Delta^{1v}_1}{2} - \frac{1}{1458} \Delta^v_{\frac{1}{2}}. \end{aligned}$$

Putting  $n = \frac{2}{3}$ , we have the value of  $f_2 - f_0$ , that is, of  $\delta'_{\frac{1}{2}} + \delta'_{\frac{3}{2}}$ . Thus we find

$$\begin{aligned} \delta'_{\frac{1}{2}} + \delta'_{\frac{3}{2}} &= \frac{2}{3} \Delta'_{\frac{1}{2}} - \frac{1}{9} \frac{\Delta''_0 + \Delta''_1}{2} - \frac{1}{162} \Delta'''_{\frac{1}{2}} \\ &\quad + \frac{5}{243} \frac{\Delta^{1v}_0 + \Delta^{1v}_1}{2} + \frac{1}{1458} \Delta^v_{\frac{1}{2}}. \end{aligned}$$

Subtracting these expressions, we have

$$\delta'_{\frac{3}{2}} = \frac{1}{3} \Delta'_{\frac{1}{2}} - \frac{1}{81} \Delta'''_{\frac{1}{2}} + \frac{1}{729} \Delta^v_{\frac{1}{2}},$$

which is most easily computed in the form

$$\delta'_{\frac{3}{2}} = \frac{1}{3} \left\{ \Delta'_{\frac{1}{2}} - \frac{1}{27} \left( \Delta'''_{\frac{1}{2}} - \frac{1}{9} \Delta^v_{\frac{1}{2}} \right) \right\}. \quad (m)$$

We see that the computation of  $\delta'_{\frac{3}{2}}$ , the middle difference of the interpolated quantities, is much simpler than that of  $\delta'_{\frac{1}{2}}$ . It will therefore facilitate the work to compute only these middle differences, and to find the others by interpolation.

This process is again facilitated, in case the second differences are considerable, by first computing the second differences of the interpolated series on the same plan. The formulæ for this purpose are derived as follows:

Let us put

$$\delta'_{\frac{3}{2}} = f_4 - f_2.$$

The second difference of which we desire the value is then

$$\delta''_{\frac{3}{2}} = \delta'_{\frac{3}{2}} - \delta'_{\frac{1}{2}}.$$

The value of  $\delta'_{\frac{3}{2}}$  is given by the equation

$$\delta'_{\frac{3}{2}} = \Delta'_{\frac{1}{2}} - (\delta'_{\frac{1}{2}} + \delta'_{\frac{3}{2}}),$$

and the value of  $\delta'_{\frac{1}{2}}$  is found from that of  $\delta'_{\frac{1}{3}}$  by simply increasing the indices of the differences by unity, because it belongs to the next lower line.

We thus find

$$\begin{aligned}\delta'_{\frac{1}{2}} &= \frac{1}{3} \Delta'_{\frac{1}{3}} - \frac{1}{9} \frac{\Delta''_0 + \Delta''_1}{2} + \frac{1}{162} \Delta'''_{\frac{1}{3}} \\ &\quad + \frac{5}{243} \frac{\Delta^{1v}_0 + \Delta^{1v}_1}{2} - \frac{1}{1458} \Delta^{v}_{\frac{1}{3}}; \\ \delta'_{\frac{1}{3}} &= \frac{1}{3} \Delta'_{\frac{1}{2}} + \frac{1}{9} \frac{\Delta''_0 + \Delta''_1}{2} + \frac{1}{162} \Delta'''_{\frac{1}{2}} \\ &\quad - \frac{5}{243} \frac{\Delta^{1v}_0 + \Delta^{1v}_1}{2} - \frac{1}{1458} \Delta^{v}_{\frac{1}{2}}.\end{aligned}$$

Then by subtraction,

$$\begin{aligned}\Delta''_{\frac{1}{2}} &= \frac{1}{3} (\Delta'_{\frac{1}{3}} - \Delta'_{\frac{1}{2}}) - \frac{1}{9} \frac{\Delta''_0 + 2\Delta''_1 + \Delta''_2}{2} + \frac{1}{162} (\Delta'''_{\frac{1}{3}} - \Delta'''_{\frac{1}{2}}) \\ &\quad + \frac{5}{243} \frac{\Delta^{1v}_0 + 2\Delta^{1v}_1 + \Delta^{1v}_2}{2} - \frac{1}{1458} (\Delta^v_{\frac{1}{3}} - \Delta^v_{\frac{1}{2}}).\end{aligned}$$

Reducing the first of these terms, we have

$$\Delta'_{\frac{1}{3}} - \Delta'_{\frac{1}{2}} = \Delta''_1.$$

For the second term,

$$\begin{aligned}\Delta''_0 &= \Delta''_1 - \Delta'''_{\frac{1}{3}}; \\ \Delta''_2 &= \Delta''_1 + \Delta'''_{\frac{1}{2}};\end{aligned}$$

whence

$$\Delta''_0 + \Delta''_2 = 2\Delta''_1 + \Delta'''_{\frac{1}{3}} - \Delta'''_{\frac{1}{2}} = 2\Delta''_1 + \Delta^{1v}_1,$$

and

$$\frac{\Delta''_0 + 2\Delta''_1 + \Delta''_2}{2} = 2\Delta''_1 + \frac{1}{2}\Delta^{1v}_1.$$

For the third term,

$$\Delta'''_{\frac{1}{3}} - \Delta'''_{\frac{1}{2}} = \Delta^{1v}_1.$$

For the fourth term, dropping the terms in  $\Delta^{1v}$  as too small in practice, we may put

$$\frac{\Delta^{1v}_0 + 2\Delta^{1v}_1 + \Delta^{1v}_2}{2} = 2\Delta^{1v}_1.$$

The difference of the fifth terms may also be dropped, because they contain only sixth differences.

Making these substitutions in the value of  $\Delta''_{\frac{1}{2}}$ , we find

$$\begin{aligned}\Delta''_{\frac{1}{2}} &= \frac{1}{3} \Delta''_1 - \frac{1}{9} \left( 2\Delta''_1 + \frac{1}{2} \Delta^{1v}_1 \right) + \frac{1}{162} \Delta^{1v}_1 + \frac{10}{243} \Delta^{1v}_1, \\ &= \frac{1}{9} \Delta''_1 - \frac{2}{243} \Delta^{1v}_1, \\ &= \frac{1}{9} \left( \Delta''_1 - \frac{2}{27} \Delta^{1v}_1 \right). \tag{n}\end{aligned}$$

By this formula we may compute every third value of  $\delta''$ , and then interpolate the intermediate values. By means of these values we find by addition the intermediate values of  $\delta'$ , of which every third value has been computed by formula (m). Then, by continually adding the values of  $\delta'$ , we find those of the function  $f$ .

As an example of the work, we give the following values of the sun's declination for every third day of part of July, 1886, for Greenwich mean noon:

Date. 1886.	$\odot$ 's Dec. ° / " "	$\Delta'$ "	$\Delta''$ "	$\Delta'''$ "
July 3.....	22 57 37.5	- 16 28.3		
6.....	22 41 9.2	- 20 0.7	- 212.4	+ 4.5
9.....	22 21 8.5	- 23 28.6	- 207.9	+ 4.5
12.....	21 57 39.9	- 26 52.0	- 203.4	+ 5.7
15.....	21 30 47.9	- 30 9.7	- 197.7	
18.....	21 0 38.2			

The values of  $\Delta^{iv}$  are too small to have any influence.

The whole work of interpolation is shown in the following table, where, as before, the right-hand column is that first computed, and gives the value of  $\Delta' - \frac{1}{27}\Delta'''$  according to formula (m):

Date. 1886.	$\odot$ 's Dec. ° / " "	$\delta'$ "	$\delta''$ "	$\Delta' - \frac{1}{27}\Delta'''$
July 6.....	22 41 9.2	- 6 16.86	- 23.60	
7.....	22 34 52.4	- 6 40.29	- 23.43	- 20 0.87
8.....	22 28 12.1	- 7 3.56	- 23.27	
9.....	22 21 8.5	- 7 26.66	- 23.10	
10.....	22 13 41.9	- 7 49.59	- 22.93	- 23 28.77
11.....	22 5 52.3	- 8 12.37	- 22.78	
12.....	21 57 39.9	- 8 34.98	- 22.61	
13.....	21 49 4.9	- 8 57.40	- 22.42	
14.....	21 40 7.5	- 9 19.59	- 22.19	- 26 52.21
15.....	21 30 47.9		- 21.97	

To make the process in the example clear, the computed differences, etc., are printed in heavier type than the interpolated ones.

It is also to be remarked that the sum of the three consecutive values of  $\delta''$ , formed of one computed value and the interpolated values next above and below it, should be equal to the difference between the corresponding computed first differences. For instance,

$$23''.27 + 23''.10 + 22''.93 = 7' 49''.59 - 6' 40''.29.$$

But in the first computation this condition will seldom be exactly fulfilled, owing to the errors arising from omitted decimals and other sources. If the given quantities are accurate, the errors should never

exceed half a unit of the last decimal in the given quantities, or five units in the additional decimal added on in dividing.

To correct these little imperfections after the interpolation of the second differences, but before that of the first differences, the sum of the last two figures in each triplet of second differences should be formed, and if it does not agree with the difference of the first differences, the last figures of the second difference should each be slightly altered, to make the sum exact.

The first differences can then be formed by addition.

In the same way, the sum of three consecutive first differences should be equal to the difference between the given quantities. If, as is generally the case, this condition is not exactly fulfilled, the differences should be altered accordingly. This alteration may, however, be made mentally while adding to form the required interpolated functions.

As an exercise for the student we give the continuance of the sun's declination for the remainder of the month, to be interpolated for the intermediate dates from July 15th onward:

	°   '   "
July 21.....	20 27 16.5
24.....	19 50 49.1
27.....	19 11 22.7
30.....	18 29 4.8
Aug. 2.....	17 44 3.1

As another exercise the logarithms of the intermediate numbers from 998 to 1014 may be interpolated by the following table:

Number.	Logarithm.
994.....	2.997 386 4
997.....	2.998 695 2
1000.....	3.000 000 0
1003.....	3.001 300 9
1006.....	3.002 598 0
1009.....	3.003 891 2
1012.....	3.005 180 5
1015.....	3.006 466 0
1018.....	3.007 747 8

**32. Interpolation to fifths.** Let us next investigate the formulæ when every fifth quantity is given and the intermediate ones are to be found by interpolation. By putting  $n = \frac{1}{5}$  in the Besselian formula, we shall have the value of the interpolation function second

following one of the given ones, and by putting  $n = \frac{3}{5}$  that third following. The difference will be the middle interpolated first difference of the interpolated series. Putting  $n = \frac{3}{5}$  in (f), we have

$$\begin{aligned} u_{\frac{3}{5}} = u_0 + \frac{2}{5} \Delta'_{\frac{1}{5}} - \frac{\frac{2.3}{2.5^2} \Delta''_0 + \Delta''_1}{2} + \frac{2.3.1}{2^2.3.5^2} \Delta'''_{\frac{1}{5}} \\ + \frac{2.3.7.8}{2.3.4.5^4} \frac{\Delta^{IV}_0 + \Delta^{IV}_1}{2} - \frac{2.3.7.8.1}{2^2.3.4.5.5^4} \Delta^{IV}_{\frac{1}{5}}. \end{aligned}$$

Putting  $n = \frac{3}{5}$ , we have

$$\begin{aligned} u_{\frac{3}{5}} = u_0 + \frac{3}{5} \Delta'_{\frac{1}{5}} - \frac{\frac{2.3}{2.5^2} \Delta''_0 + \Delta''_1}{2} - \frac{2.3.1}{2^2.3.5^2} \Delta'''_{\frac{1}{5}} \\ + \frac{2.3.7.8}{2.3.4.5^4} \frac{\Delta^{IV}_0 + \Delta^{IV}_1}{2} + \frac{8.3.2.7.1}{2^2.3.4.5.5^4} \Delta^{IV}_{\frac{1}{5}}. \end{aligned}$$

The difference of these expressions, being reduced, gives

$$\begin{aligned} u_{\frac{3}{5}} - u_{\frac{2}{5}} &= \frac{1}{5} \Delta'_{\frac{1}{5}} - \frac{1}{125} \Delta'''_{\frac{1}{5}} + \frac{14}{15625} \Delta^{IV}_{\frac{1}{5}} \\ &= \frac{1}{5} \left\{ \Delta'_{\frac{1}{5}} - \frac{1}{25} \left( \Delta'''_{\frac{1}{5}} - \frac{14}{125} \Delta^{IV}_{\frac{1}{5}} \right) \right\}. \end{aligned}$$

The term in  $\Delta^{IV}$  will not produce any effect unless the fifth differences are considerable, and then we may nearly always, in practice, put  $\frac{1}{25}$  instead of  $\frac{14}{125}$ .

The interpolated second differences opposite the given functions are most readily obtained by Stirling's formula, (d). Putting  $n = \frac{1}{5}$ , we have the following value of the interpolated first differences immediately following a given value of the function:

$$\begin{aligned} u_{\frac{1}{5}} - u_0 &= \frac{1}{5} \frac{\Delta'_{-\frac{1}{5}} + \Delta'_{\frac{1}{5}}}{2} + \frac{1}{50} \Delta''_0 - \frac{24}{6.5.25} \frac{\Delta'''_{-\frac{1}{5}} + \Delta'''_{\frac{1}{5}}}{2} \\ &\quad - \frac{24}{6.5.20.25} \Delta^{IV}_0 + \text{etc.} \end{aligned}$$

Again, putting  $n = -\frac{1}{5}$ , and changing the signs, we find for the first difference next preceding a given function

$$\begin{aligned} u_0 - u_{-\frac{1}{5}} &= \frac{1}{5} \frac{\Delta'_{-\frac{1}{5}} + \Delta'_{\frac{1}{5}}}{2} - \frac{1}{50} \Delta''_0 - \frac{24}{6.5.25} \frac{\Delta'''_{-\frac{1}{5}} + \Delta'''_{\frac{1}{5}}}{2} \\ &\quad + \frac{24}{6.5.20.25} \Delta^{IV}_0 - \text{etc.} \end{aligned}$$

The difference of these quantities gives the required second difference, which we find to be

$$\delta''_0 = \frac{1}{25} \Delta''_0 - \frac{2}{625} \Delta^{IV}_0 = \frac{1}{25} \left( \Delta''_0 - \frac{2}{25} \Delta^{IV}_0 \right).$$

As an example and exercise we show the interpolation of logarithms when every fifth logarithm is given:

Number.	Logarithm.	$\delta'$	$\delta''$	$\Delta'$	$\Delta''$
1000	3.000 000 0			+ 21 661	
<b>1005</b>	<b>3.002 166 1</b>	4319.2	- 4.32		- 108
1006	.002 598 0	4314.9	- 4.31		
1007	.003 029 5		- 4.30		
1008	.003 460 6	<b>4310.6</b>	- 4.30	+ 21 553	
1009	.003 891 2	4306.3	- 4.29		
<b>1010</b>	<b>3.004 321 4</b>	4302.0	- 4.28		- 107
1011	.004 751 2	4297.7	- 4.27		
1012	.005 180 5	4293.5	- 4.26		
1013	.005 609 4	<b>4289.2</b>	- 4.23	+ 21 446	
1014	.006 037 9	4285.0	- 4.20		
<b>1015</b>	<b>3.006 466 0</b>	4280.8	- 4.16	+ 21 342	- 104
1020	3.008 600 2				
1025	3.010 723 9				
1030	3.012 837 2				
1035	3.014 940 3				
1040	3.017 033 3				

# **FORMULÆ**

**FOR THE SOLUTION OF**

**PLANE AND SPHERICAL TRIANGLES.**

## REMARKS.

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1. It is better to determine an angle by its tangent than by its sine or cosine, because a small angle or an angle near  $180^\circ$  cannot be accurately determined by its cosine, nor one near either  $90^\circ$  or  $270^\circ$  by its sine.

Sometimes, however, the data of the problem are such that the angle can be determined only through its sine or cosine. Any uncertainty which may then arise from the source pointed out is then inherent in the problem; e.g., if the hypotenuse and one side of a right triangle are 0.39808 and 0.39806 respectively (sixth and following decimals being omitted), the value of the included angle may be anywhere between  $0^\circ 25'$  and  $0^\circ 42'$ , no matter what method of computation be adopted.

2. If the sine and cosine can be independently computed, their agreement as to the angle will generally serve as a check on the accuracy of the computation. If they agree, their quotient will give the tangent.

3. It is desirable, when possible, to have a check upon the accuracy of the computation; that is, to make a computation which must give a certain result if the work is right. But no check can give a positive assurance of accuracy: all it can do is to make it more or less improbable that a mistake exceeding a certain limit exists.

4. In the following list several formulæ are sometimes given as applicable to the same problem. In such cases, the most convenient for the special purpose must be chosen.

*Notation.*  $a$ ,  $b$ , and  $c$  are the three sides.

$A$ ,  $B$ , and  $C$  are the opposite angles.

## PLANE TRIANGLES.

<b>Given.</b> $a, b, c$ , the three sides.	<b>Required.</b> $A$ , one angle.	$s = \frac{1}{2}(a + b + c)$ . $\tan \frac{1}{2}A = \sqrt{\frac{(s - b)(s - c)}{s(s - a)}}$ . $H = \sqrt{\frac{(s - a)(s - b)(s - c)}{s}}$ ; $\tan \frac{1}{2}A = \frac{H}{s - a}$ ; $\tan \frac{1}{2}B = \frac{H}{s - b}$ ; $\tan \frac{1}{2}C = \frac{H}{s - c}$ . Checks: $A + B + C = 180^\circ$ ; $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$ $\tan \frac{1}{2}(B - C) = \frac{b - c}{b + c} \cot \frac{1}{2}A$ ; $\frac{1}{2}(B + C) = 90^\circ - \frac{1}{2}A$ ; $B = \frac{1}{2}(B + C) + \frac{1}{2}(B - C)$ ; $C = \frac{1}{2}(B + C) - \frac{1}{2}(B - C)$ . Check, as before. $a \sin \frac{1}{2}(B - C) = (b - c) \cos \frac{1}{2}A$ ; $a \cos \frac{1}{2}(B - C) = (b + c) \sin \frac{1}{2}A$ . Having found $a$ and $\frac{1}{2}(B - C)$ , proceed as in the last case.
<u><math>b, c, A</math>,</u> two sides and the included angle.	<u><math>B</math> and <math>C</math></u> , the other angles.	$a, B, C$ , the remaining parts.
<u><math>a, b, A</math>,</u> two sides and the angle oppo- site one of them.	<u><math>c, B, C</math></u> , the re- maining parts.	$\sin B = \frac{b}{a} \sin A$ ; (two values of $B$ .) $C = 180^\circ - (A + B)$ ; $c = \frac{b \sin C}{\sin B} = \frac{a \sin C}{\sin A}$ .

Given. $a, A, B,$ one side and any two angles.	Required. $b, c, C,$ the re- maining parts.	$C = 180^\circ - (A + B);$ $b = \frac{a \sin B}{\sin A};$ $c = \frac{a \sin C}{\sin A} = \frac{a \sin (A + B)}{\sin A}.$
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## RIGHT SPHERICAL TRIANGLES.

$a, b,$ the sides containing the right angle.	$A, B, \text{ or } c.$	$c$ is the hypotenuse. $\cot A = \cot a \sin b;$ $\cot B = \cot b \sin a;$ $\cos c = \cos a \cos b;$ $\sin c = \frac{\sin a}{\sin A}.$
	$A$ and $c.$	$\sin c \sin A = \sin a;$ $\sin c \cos A = \cos a \sin b;$ $\cos c = \cos a \cos b.$
	$B$ and $c$	$\sin c \sin B = \sin b;$ $\sin c \cos B = \sin a \cos b.$
$a, c,$ one side and the hy- pothenuse.	$A, B, \text{ or } b.$	$\sin A = \frac{\sin a}{\sin c};$ $\cos B = \tan a \cot c;$ $\cos b = \frac{\cos c}{\cos a}.$
$a, A,$ one side and the opposite angle.	$b, c, \text{ or } B.$	$\sin b = \tan a \cot A;$ $\sin c = \frac{\sin a}{\sin A};$ $\sin B = \frac{\cos A}{\cos a}.$
$a, B,$ one side and the adjacent angle.	$b, c, \text{ or } A.$	$\tan b = \sin a \tan B;$ $\tan c = \frac{\tan a}{\cos B};$ $\cos A = \cos a \sin B.$
	$c$ and $A.$	$\sin A \sin c = \sin a;$ $\sin A \cos c = \cos a \cos B;$ $\cos A = \cos a \sin B.$

Given.	Required.	
$a, B.$	$b$ and $A.$	$\sin A \sin b = \sin a \sin B;$ $\sin A \cos b = \cos B.$
$c, A,$ the hypo- thenuse and one angle.	$a, b$ , or $B.$	$\sin a = \sin c \sin A;$ $\tan b = \tan c \cos A;$ $\cot B = \cos c \tan A.$
	$a$ and $B.$	$\cos a \sin B = \cos A;$ $\cos a \cos B = \sin A \cos c;$ $\sin a = \sin A \sin c.$
	$a$ and $b.$	$\cos a \sin b = \cos A \sin c;$ $\cos a \cos b = \cos c.$
$A, B,$ the two angles.	$a, b$ , or $c.$	$\cos a = \frac{\cos A}{\sin B};$ $\cos b = \frac{\cos B}{\sin A};$ $\cos c = \cot A \cot B.$

## QUADRANTAL SPHERICAL TRIANGLES.

		$c$ is the omitted side equal to $90^\circ.$ $C$ is the angle opposite this side.
$a, b,$ the two sides.	$A, B$ , or $C,$ either angle.	$\cos A = \frac{\cos a}{\sin b};$ $\cos B = \frac{\cos b}{\sin a};$ $\cos C = -\cot a \cot b.$
$a, C,$ one side and the angle oppo- site the right side.	$A, B$ , or $b.$	$\sin A = \sin a \sin C;$ $\tan B = -\cos a \tan C;$ $\cot b = -\tan a \cos C.$
	$A$ and $b.$	$\cos A \sin b = \cos a;$ $\cos A \cos b = -\sin a \cos C.$ $\sin A = \sin a \sin C.$
	$A$ and $B.$	$\cos A \sin B = \cos a \sin C;$ $\cos A \cos B = -\cos C.$

Given.	Required.	
$a, b,$ one angle and the adjacent side.	$a, B,$ or $C.$	$\cos a = \cos A \sin b;$ $\tan B = \sin A \tan a;$ $\cot C = -\cot A \cos b.$
	$a$ and $B.$	$\sin a \sin B = \sin A \sin b;$ $\sin a \cos B = \cos b;$ $\cos a = \cos A \sin b.$
	$a$ and $C.$	$\sin a \sin C = \sin A;$ $\sin a \cos C = -\cos A \cos b.$
$a, A,$ one side and the opposite angle.	$b, B,$ or $C.$	$\sin b = \frac{\cos a}{\cos A};$ $\sin B = \cot a \tan A;$ $\sin C = \frac{\sin A}{\sin a}.$
$A, C,$ one angle and the angle oppo- site the right side.	$a, b,$ or $B.$	$\sin a = \frac{\sin A}{\sin C};$ $\cos b = -\tan A \cot C;$ $\cos B = -\frac{\cos C}{\cos A}.$
$A, B,$ two angles.	$a, b,$ or $C.$	$\cot a = \cot A \sin B;$ $\cot b = \sin A \cot C;$ $\cos C = -\cos A \cos B.$
	$a$ and $C.$	$\sin C \sin a = \sin A;$ $\sin C \cos a = \cos A \sin B;$ $\cos C = -\cos A \cos B.$
	$b$ and $C.$	$\sin C \sin b = \sin B;$ $\sin C \cos b = \sin A \cos B.$

## SPHERICAL TRIANGLES IN GENERAL.

Given. $a, b, c$ , the three sides.	Required. $A, B, C$ , the three angles.	$s = \frac{1}{2}(a + b + c);$ $H = \sqrt{\frac{\sin(s-a) \sin(s-b) \sin(s-c)}{\sin s}},$ $\tan \frac{1}{2}A = \frac{H}{\sin(s-a)};$ $\tan \frac{1}{2}B = \frac{H}{\sin(s-b)};$ $\tan \frac{1}{2}C = \frac{H}{\sin(s-c)}.$ Check: $\frac{\sin a}{\sin A} = \frac{\sin b}{\sin B} = \frac{\sin c}{\sin C}.$
$a, b, C$ , two sides and the included angle.	$A$ and $c$ , one angle and the remaining side.	$\sin c \sin A = \sin a \sin C;$ $\sin c \cos A = \cos a \sin b - \sin a \cos b \cos C;$ $\cos c = \cos a \cos b + \sin a \sin b \cos C.$
	$B$ and $c$ .	$\sin c \sin B = \sin b \sin C;$ $\sin c \cos B = \sin a \cos b - \cos a \sin b \cos C.$ If addition and subtraction logarithms are not available for this computation, we may compute $k$ and $K$ from $k \sin K = \sin a \cos C;$ $k \cos K = \cos a.$
	Then	$\sin c \cos A = k \sin(b - K);$ $\cos c = k \cos(b - K).$
	Also,	$h \sin H = \sin b \cos C;$ $h \cos H = \cos b.$
	Then	$\sin c \cos B = h \sin(a - H);$ $\cos c = h \cos(a - H).$
$A, B, c$ , all the remaining parts.		$\sin \frac{1}{2}c \sin \frac{1}{2}(A - B) = \cos \frac{1}{2}C \sin \frac{1}{2}(a - b);$ $\sin \frac{1}{2}c \cos \frac{1}{2}(A - B) = \sin \frac{1}{2}C \sin \frac{1}{2}(a + b);$ $\cos \frac{1}{2}c \sin \frac{1}{2}(A + B) = \cos \frac{1}{2}C \cos \frac{1}{2}(a - b);$ $\cos \frac{1}{2}c \cos \frac{1}{2}(A + B) = \sin \frac{1}{2}C \cos \frac{1}{2}(a + b).$

<p>Given.</p> <p><math>a, b, A</math>, two sides and an opposite angle.</p> <hr/> <p><math>A, B, c</math>, two angles and the included side.</p> <hr/> <p><math>a, b, C</math>, all the remaining parts.</p> <hr/> <p><math>A, B, a</math>, two angles and an opposite side.</p> <hr/> <p><math>A, B, C</math>, the three angles.</p>	<p>Required.</p> <p><math>B, C, c</math>, all the remaining parts.</p> <hr/> <p><math>a</math> and <math>C</math>, one side and the third angle.</p> <hr/> <p><math>b</math> and <math>C</math>.</p> <hr/> <p><math>b, c, C</math>, all the remaining parts.</p> <hr/> <p><math>a, b, c</math>, the three sides.</p>	$\sin B = \frac{\sin A \sin b}{\sin a}$ (two values of $B$ ); $\tan \frac{1}{2} C = \frac{\cos \frac{1}{2}(a - b) \cot \frac{1}{2}(A + B)}{\cos \frac{1}{2}(a + b)}$ ; $\tan \frac{1}{2} c = \frac{\cos \frac{1}{2}(A + B) \tan \frac{1}{2}(a + b)}{\cos \frac{1}{2}(A - B)}$
		$\sin C \sin a = \sin A \sin c$ ; $\sin C \cos a = \cos A \sin B + \sin A \cos B \cos c$ ; $\cos C = -\cos A \cos B + \sin A \sin B \cos c$ .
		$\sin C \sin b = \sin B \sin c$ ; $\sin C \cos b = \sin A \cos B + \cos A \sin B \cos c$ . If we compute $k$ and $K$ from $k \sin K = \cos A$ , $k \cos K = \sin A \cos c$ , then $\sin C \cos a = k \cos(B - K)$ ; $\cos C = k \sin(B - K)$ .
		If we compute $h$ and $H$ from $h \sin H = \cos B$ , $h \cos H = \sin B \cos c$ , then $\sin C \cos b = h \cos(A - H)$ ; $\cos C = h \sin(A - H)$ . $\sin \frac{1}{2} C \sin \frac{1}{2}(a + b) = \sin \frac{1}{2} c \cos \frac{1}{2}(A - B)$ ; $\sin \frac{1}{2} C \cos \frac{1}{2}(a + b) = \cos \frac{1}{2} c \cos \frac{1}{2}(A + B)$ ; $\cos \frac{1}{2} C \sin \frac{1}{2}(a - b) = \sin \frac{1}{2} c \sin \frac{1}{2}(A - B)$ ; $\cos \frac{1}{2} C \cos \frac{1}{2}(a - b) = \cos \frac{1}{2} c \sin \frac{1}{2}(A + B)$ .
		$\sin b = \frac{\sin a \sin B}{\sin A}$ (two values of $b$ ); $\tan \frac{1}{2} c = \frac{\cos \frac{1}{2}(A + B) \tan \frac{1}{2}(a + b)}{\cos \frac{1}{2}(A - B)}$ ; $\tan \frac{1}{2} C = \frac{\cos \frac{1}{2}(a - b) \cot \frac{1}{2}(A + B)}{\cos \frac{1}{2}(a + b)}$ .
		$S = \frac{1}{2}(A + B + C)$ ; $P = \sqrt{\frac{-\cos S}{\cos(S - A) \cos(S - B) \cos(S - C)}}$ ; $\tan \frac{1}{2} a = P \cos(S - A)$ ; $\tan \frac{1}{2} b = P \cos(S - B)$ ; $\tan \frac{1}{2} c = P \cos(S - C)$ .

## TABLES.



T A B L E I.

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COMMON LOGARITHMS  
O F N U M B E R S.

N.	Log.	N.	Log.	N.	Log.	N.	Log.	N.	Log.
0	—Infinity.	30	1.47 712	60	1.77 815	90	1.95 424	120	2.07 918
1	0.00 000	31	1.49 136	61	1.78 533	91	1.95 904	121	2.08 279
2	0.30 103	32	1.50 515	62	1.79 239	92	1.96 379	122	2.08 636
3	0.47 712	33	1.51 851	63	1.79 934	93	1.96 848	123	2.08 991
4	0.60 206	34	1.53 148	64	1.80 618	94	1.97 313	124	2.09 342
5	0.69 897	35	1.54 407	65	1.81 291	95	1.97 772	125	2.09 691
6	0.77 815	36	1.55 630	66	1.81 954	96	1.98 227	126	2.10 037
7	0.84 510	37	1.56 820	67	1.82 607	97	1.98 677	127	2.10 380
8	0.90 309	38	1.57 978	68	1.83 251	98	1.99 123	128	2.10 721
9	0.95 424	39	1.59 106	69	1.83 885	99	1.99 564	129	2.11 059
10	1.00 000	40	1.60 206	70	1.84 510	100	2.00 000	130	2.11 394
11	1.04 139	41	1.61 278	71	1.85 126	101	2.00 432	131	2.11 727
12	1.07 918	42	1.62 325	72	1.85 733	102	2.00 860	132	2.12 057
13	1.11 394	43	1.63 347	73	1.86 332	103	2.01 284	133	2.12 385
14	1.14 613	44	1.64 345	74	1.86 923	104	2.01 703	134	2.12 710
15	1.17 609	45	1.65 321	75	1.87 506	105	2.02 119	135	2.13 033
16	1.20 412	46	1.66 276	76	1.88 081	106	2.02 531	136	2.13 354
17	1.23 045	47	1.67 210	77	1.88 649	107	2.02 938	137	2.13 672
18	1.25 527	48	1.68 124	78	1.89 209	108	2.03 342	138	2.13 988
19	1.27 875	49	1.69 020	79	1.89 763	109	2.03 743	139	2.14 301
20	1.30 103	50	1.69 897	80	1.90 309	110	2.04 139	140	2.14 613
21	1.32 222	51	1.70 757	81	1.90 849	111	2.04 532	141	2.14 922
22	1.34 242	52	1.71 600	82	1.91 381	112	2.04 922	142	2.15 229
23	1.36 173	53	1.72 428	83	1.91 908	113	2.05 308	143	2.15 534
24	1.38 021	54	1.73 239	84	1.92 428	114	2.05 690	144	2.15 836
25	1.39 794	55	1.74 036	85	1.92 942	115	2.06 070	145	2.16 137
26	1.41 497	56	1.74 819	86	1.93 450	116	2.06 446	146	2.16 435
27	1.43 136	57	1.75 587	87	1.93 952	117	2.06 819	147	2.16 732
28	1.44 716	58	1.76 343	88	1.94 448	118	2.07 188	148	2.17 026
29	1.46 240	59	1.77 085	89	1.94 939	119	2.07 555	149	2.17 319
30	1.47 712	60		90	1.95 424	120	2.07 918	150	2.17 609

TABLE I.

2

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
100	00 000	043	087	130	173	217	260	303	346	389	
01	432	475	518	561	604	647	689	732	775	817	
02	860	903	945	988	*030	*072	*115	*157	*199	*242	
03	01 284	326	368	410	452	494	536	578	620	662	
04	703	745	787	828	870	912	953	995	*036	*078	
05	02 119	160	202	243	284	325	366	407	449	490	
06	531	572	612	653	694	735	776	816	857	898	
07	938	979	*019	*060	*100	*141	*181	*222	*262	*302	
08	03 342	383	423	463	503	543	583	623	663	703	
09	743	782	822	862	902	941	981	*021	*060	*100	
110	04 139	179	218	258	297	336	376	415	454	493	
11	532	571	610	650	689	727	766	805	844	883	
12	922	961	999	*038	*077	*115	*154	*192	*231	*269	
13	05 308	346	385	423	461	500	538	576	614	652	
14	690	729	767	805	843	881	918	956	994	*032	
15	06 070	108	145	183	221	258	296	333	371	408	
16	446	483	521	558	595	633	670	707	744	781	
17	819	856	893	930	967	*004	*041	*078	*115	*151	
18	07 188	225	262	298	335	372	408	445	482	518	
19	555	591	628	664	700	737	773	809	846	882	
120	918	954	990	*027	*063	*099	*135	*171	*207	*243	
21	08 279	314	350	386	422	458	493	529	565	600	
22	636	672	707	743	778	814	849	884	920	955	
23	991	*026	*061	*096	*132	*167	*202	*237	*272	*307	
24	09 342	377	412	447	482	517	552	587	621	656	
25	691	726	760	795	830	864	899	934	968	*003	
26	10 037	072	106	140	175	209	243	278	312	346	
27	380	415	449	483	517	551	585	619	653	687	
28	721	755	789	823	857	890	924	958	992	*025	
29	11 059	093	126	160	193	227	261	294	327	361	
130	394	428	461	494	528	561	594	628	661	694	
31	727	760	793	826	860	893	926	959	992	*024	
32	12 057	090	123	156	189	222	254	287	320	352	
33	385	418	450	483	516	548	581	613	646	678	
34	710	743	775	808	840	872	905	937	969	*001	
35	13 033	066	098	130	162	194	226	258	290	322	
36	354	386	418	450	481	513	545	577	609	640	
37	672	704	735	767	799	830	862	893	925	956	
38	988	*019	*051	*082	*114	*145	*176	*208	*239	*270	
39	14 301	333	364	395	426	457	489	520	551	582	
140	613	644	675	706	737	768	799	829	860	891	
41	922	953	983	*014	*045	*076	*106	*137	*168	*198	
42	15 229	259	290	320	351	381	412	442	473	503	
43	534	564	594	625	655	685	715	746	776	806	
44	836	866	897	927	957	987	*017	*047	*077	*107	
45	16 137	167	197	227	256	286	316	346	376	406	
46	435	465	495	524	554	584	613	643	673	702	
47	732	761	791	820	850	879	909	938	967	997	
48	17 026	056	085	114	143	173	202	231	260	289	
49	319	348	377	406	435	464	493	522	551	580	
150	609	638	667	696	725	754	782	811	840	869	
N.	0	1	2	3	4	5					Prop. Pts.

## LOGARITHMS OF NUMBERS.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
150	17	609	638	667	696	725	754	782	811	840	869
51		898	926	955	984	*013	*041	*070	*099	*127	*156
52	18	184	213	241	270	298	327	355	384	412	441
53		469	498	526	554	583	611	639	667	696	724
54		752	780	808	837	865	893	921	949	977	*005
55.	19	033	061	089	117	145	173	201	229	257	285
56		312	340	368	396	424	451	479	507	535	562
57		590	618	645	673	700	728	756	783	811	838
58		866	893	921	948	976	*003	*030	*058	*085	*112
59	20	140	167	194	222	249	276	303	330	358	385
160		412	439	466	493	520	548	575	602	629	656
61		683	710	737	763	790	817	844	871	898	925
62		952	978	*005	*032	*059	*085	*112	*139	*165	*192
63	21	219	245	272	299	325	352	378	405	431	458
64		484	511	537	564	590	617	643	669	696	722
65		748	775	801	827	854	880	906	932	958	985
66	22	011	037	063	089	115	141	167	194	220	246
67		272	298	324	350	376	401	427	453	479	505
68		531	557	583	608	634	660	686	712	737	763
69		789	814	840	866	891	917	943	968	994	*019
170	23	045	070	096	121	147	172	198	223	249	274
71		300	325	350	376	401	426	452	477	502	528
72		553	578	603	629	654	679	704	729	754	779
73		805	830	855	880	905	930	955	980	*005	*030
74	24	055	080	105	130	155	180	204	229	254	279
75		304	329	353	378	403	428	452	477	502	527
76		551	576	601	625	650	674	699	724	748	773
77		797	822	846	871	895	920	944	969	993	*018
78	25	042	066	091	115	139	164	188	212	237	261
79		285	310	334	358	382	406	431	455	479	503
180		527	551	575	600	624	648	672	696	720	744
81		768	792	816	840	864	888	912	935	959	983
82	26	007	031	055	079	102	126	150	174	198	221
83		245	269	293	316	340	364	387	411	435	458
84		482	505	529	553	576	600	623	647	670	694
85		717	741	764	788	811	834	858	881	905	928
86		951	975	998	*021	*045	*068	*091	*114	*138	*161
87	27	184	207	231	254	277	300	323	346	370	393
88		416	439	462	485	508	531	554	577	600	623
89		646	669	692	715	738	761	784	807	830	852
190		875	898	921	944	967	989	*012	*035	*058	*081
91	28	103	126	149	171	194	217	240	262	285	307
92		330	353	375	398	421	443	466	488	511	533
93		556	578	601	623	646	668	691	713	735	758
94		780	803	825	847	870	892	914	937	959	981
95	29	003	026	048	070	092	115	137	159	181	203
96		226	248	270	292	314	336	358	380	403	425
97		447	469	491	513	535	557	579	601	623	645
98		667	688	710	732	754	776	798	820	842	863
99		885	907	929	951	973	994	*016	*038	*060	*081
200	30	103	125	146	168	190	211	233	255	276	298
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
200	30 103	125	146	168	190	211	233	255	276	298	
01	320	341	363	384	406	428	449	471	492	514	22 21
02	535	557	578	600	621	643	664	685	707	728	1 2.2 2.1
03	750	771	792	814	835	856	878	899	920	942	2 4.4 4.2
04	963	984	*006	*027	*048	*069	*091	*112	*133	*154	3 6.6 6.3
05	31 175	197	218	239	260	281	302	323	345	366	4 8.8 8.4
06	387	408	429	450	471	492	513	534	555	576	5 11.0 10.5
07	597	618	639	660	681	702	723	744	765	785	6 13.2 12.6
08	806	827	848	869	890	911	931	952	973	994	7 15.4 14.7
09	32 015	035	056	077	098	118	139	160	181	201	8 17.6 16.8
											9 19.8 18.9
210	222	243	263	284	305	325	346	366	387	408	
11	428	449	469	490	510	531	552	572	593	613	20
12	634	654	675	695	715	736	756	777	797	818	1 2.0
13	838	858	879	899	919	940	960	980	*001	*021	2 4.0
14	33 041	062	082	102	122	143	163	183	203	224	3 6.0
15	244	264	284	304	325	345	365	385	405	425	4 8.0
16	445	465	486	506	526	546	566	586	606	626	5 10.0
17	646	666	686	706	726	746	766	786	806	826	6 12.0
18	846	866	885	905	925	945	965	985	*005	*025	7 14.0
19	34 044	064	084	104	124	143	163	183	203	223	8 16.0
											9 18.0
220	242	262	282	301	321	341	361	380	400	420	
21	439	459	479	498	518	537	557	577	596	616	19
22	635	655	674	694	713	733	753	772	792	811	1 1.9
23	830	850	869	889	908	928	947	967	986	*005	2 3.8
24	35 025	044	064	083	102	122	141	160	180	199	3 5.7
25	218	238	257	276	295	315	334	353	372	392	4 7.6
26	411	430	449	468	488	507	526	545	564	583	5 9.5
27	603	622	641	660	679	698	717	736	755	774	6 11.4
28	793	813	832	851	870	889	908	927	946	965	7 13.3
29	984	*003	*021	*040	*059	*078	*097	*116	*135	*154	8 15.2
											9 17.1
230	36 173	192	211	229	248	267	286	305	324	342	
31	361	380	399	418	436	455	474	493	511	530	18
32	549	568	586	605	624	642	661	680	698	717	1 1.8
33	736	754	773	791	810	829	847	866	884	903	2 3.6
34	922	940	959	977	996	*014	*033	*051	*070	*088	3 5.4
35	37 107	125	144	162	181	199	218	236	254	273	4 7.2
36	291	310	328	346	365	383	401	420	438	457	5 9.0
37	475	493	511	530	548	566	585	603	621	639	6 10.8
38	658	676	694	712	731	749	767	785	803	822	7 12.6
39	840	858	876	894	912	931	949	967	985	*003	8 14.4
											9 16.2
240	38 021	039	057	075	093	112	130	148	166	184	
41	202	220	238	256	274	292	310	328	346	364	17
42	382	399	417	435	453	471	489	507	525	543	1 1.7
43	561	578	596	614	632	650	668	686	703	721	2 3.4
44	739	757	775	792	810	828	846	863	881	899	3 5.1
45	917	934	952	970	987	*005	*023	*041	*058	*070	4 6.8
46	39 094	111	129	146	164	182	199	217	235	252	5 8.5
47	270	287	305	322	340	358	375	393	410	428	6 10.2
48	445	463	480	498	515	533	550	568	585	602	7 11.9
49	620	637	655	672	690	707	724	742	759	777	8 13.6
250	794	811	829	846	863	881	898	915	933	950	9 15.3
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
250	39 794	811	829	846	863	881	898	915	933	950	
51	967	985	*002	*019	*037	*054	*071	*088	*106	*123	18
52	40 140	157	175	192	209	226	243	261	278	295	2 3.6
53	312	329	346	364	381	398	415	432	449	466	1 1.8
54	483	500	518	535	552	569	586	603	620	637	2 5.4
55	654	671	688	705	722	739	756	773	790	807	4 7.2
56	824	841	858	875	892	909	926	943	960	976	5 9.0
57	993	*010	*027	*044	*061	*078	*095	*111	*128	*145	6 10.8
58	41 162	179	196	212	229	246	263	280	296	313	7 12.6
59	330	347	363	380	397	414	430	447	464	481	8 14.4
260	497	514	531	547	564	581	597	614	631	647	9 16.2
61	664	681	697	714	731	747	764	780	797	814	
62	830	847	863	880	896	913	929	946	963	979	1 1.7
63	996	*012	*029	*045	*062	*078	*095	*111	*127	*144	2 3.4
64	42 160	177	193	210	226	243	259	275	292	308	3 5.1
65	325	341	357	374	390	406	423	439	455	472	4 6.8
66	488	504	521	537	553	570	586	602	619	635	5 8.5
67	651	667	684	700	716	732	749	765	781	797	6 10.2
68	813	830	846	862	878	894	911	927	943	959	7 11.9
69	975	991	*008	*034	*040	*056	*072	*088	*104	*120	8 13.6
270	43 136	152	169	185	201	217	233	249	265	281	
71	297	313	329	345	361	377	393	409	425	441	
72	457	473	489	505	521	537	553	569	584	600	1 1.6
73	616	632	648	664	680	696	712	727	743	759	2 3.2
74	775	791	807	823	838	854	870	886	902	917	3 4.8
75	933	949	965	981	996	*012	*028	*044	*059	*075	4 6.4
76	44 091	107	122	138	154	170	185	201	217	232	5 8.0
77	248	264	279	295	311	326	342	358	373	389	6 9.6
78	404	420	436	451	467	483	498	514	530	545	7 11.2
79	560	576	592	607	623	638	654	669	685	700	8 12.8
280	716	731	747	762	778	793	809	824	840	855	
81	871	886	902	917	932	948	963	979	994	*010	
82	45 025	040	056	071	086	102	117	133	148	163	1 1.5
83	179	194	209	225	240	255	271	286	301	317	2 3.0
84	332	347	362	378	393	408	423	439	454	469	3 4.5
85	484	500	515	530	545	561	576	591	606	621	4 6.0
86	637	652	667	682	697	712	728	743	758	773	5 7.5
87	788	803	818	834	849	864	879	894	909	924	6 9.0
88	939	954	969	984	*000	*015	*030	*045	*060	*075	7 10.5
89	46 090	105	120	135	150	165	180	195	210	225	8 12.0
290	240	255	270	285	300	315	330	345	359	374	9 13.5
91	389	404	419	434	449	464	479	494	509	523	1 1.4
92	538	553	568	583	598	613	627	642	657	672	2 2.8
93	687	702	716	731	746	761	776	790	805	820	3 4.2
94	835	850	864	879	894	909	923	938	953	967	4 5.6
95	982	997	*012	*026	*041	*056	*070	*085	*100	*114	5 7.0
96	47 129	144	159	173	188	202	217	232	246	261	6 8.4
97	276	290	305	319	334	349	363	378	392	407	7 9.8
98	422	436	451	465	480	494	509	524	538	553	8 11.2
99	567	582	596	611	625	640	654	669	683	698	9 12.6
300	712	727	741	756	770	784	799	813	828	842	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
300	47	712	727	741	756	770	784	799	813	828	842
01		857	871	885	900	914	929	943	958	972	986
02	48	001	015	029	044	058	073	087	101	116	130
03		144	159	173	187	202	216	230	244	259	273
04		287	302	316	330	344	359	373	387	401	416
05		430	444	458	473	487	501	515	530	544	558
06		572	586	601	615	629	643	657	671	686	700
07		714	728	742	756	770	785	799	813	827	841
08		855	869	883	897	911	926	940	954	968	982
09		996	*010	*024	*038	*052	*066	*080	*094	*108	*122
810	49	136	150	164	178	192	206	220	234	248	262
11		276	290	304	318	332	346	360	374	388	402
12		415	429	443	457	471	485	499	513	527	541
13		554	568	582	596	610	624	638	651	665	679
14		693	707	721	734	748	762	776	790	803	817
15		831	845	859	872	886	900	914	927	941	955
16		969	982	996	*010	*024	*037	*051	*065	*079	*092
17	50	106	120	133	147	161	174	188	202	215	229
18		243	256	270	284	297	311	325	338	352	365
19		379	393	406	420	433	447	461	474	488	501
820		515	529	542	556	569	583	596	610	623	637
21		651	664	678	691	705	718	732	745	759	772
22		786	799	813	826	840	853	866	880	893	907
23		920	934	947	961	974	987	*001	*014	*028	*041
24	51	055	068	081	095	108	121	135	148	162	175
25		188	202	215	228	242	255	268	282	295	308
26		322	335	348	362	375	388	402	415	428	441
27		455	468	481	495	508	521	534	548	561	574
28		587	601	614	627	640	654	667	680	693	706
29		720	733	746	759	772	786	799	812	825	838
830		851	865	878	891	904	917	930	943	957	970
31		983	996	*009	*022	*035	*048	*061	*075	*088	*101
32	52	114	127	140	153	166	179	192	205	218	231
33		244	257	270	284	297	310	323	336	349	362
34		375	388	401	414	427	440	453	466	479	492
35		504	517	530	543	556	569	582	595	608	621
36		634	647	660	673	686	699	711	724	737	750
37		763	776	789	802	815	827	840	853	866	879
38		892	905	917	930	943	956	969	982	994	*007
39	53	020	033	046	058	071	084	097	110	122	135
840		148	161	173	186	199	212	224	237	250	263
41		275	288	301	314	326	339	352	364	377	390
42		403	415	428	441	453	466	479	491	504	517
43		529	542	555	567	580	593	605	618	631	643
44		656	668	681	694	706	719	732	744	757	769
45		782	794	807	820	832	845	857	870	882	895
46		908	920	933	945	958	970	983	995	*008	*020
47	54	033	045	058	070	083	095	108	120	133	145
48		158	170	183	195	208	220	233	245	258	270
49		283	295	307	320	332	345	357	370	382	394
850		407	419	432	444	456	469	481	494	506	518
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

15

14

13

12

1.5

2.8

4.2

2.6

3.9

5.2

6.5

7.8

9.1

10.4

11.7

1.3

3.6

4.8

6.0

7.2

8.4

9.6

10.8

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
350	54	407	419	432	444	456	469	481	494	506	518
51	531	543	555	568	580	593	605	617	630	642	
52	654	667	679	691	704	716	728	741	753	765	
53	777	790	802	814	827	839	851	864	876	888	
54	900	913	925	937	949	962	974	986	998	*011	13
55	55	023	035	047	060	072	084	096	108	121	1.3
56	145	157	169	182	194	206	218	230	242	255	2.6
57	267	279	291	303	315	328	340	352	364	376	3.9
58	388	400	413	425	437	449	461	473	485	497	5.2
59	509	522	534	546	558	570	582	594	606	618	6.5
360	630	642	654	666	678	691	703	715	727	739	7.8
61	751	763	775	787	799	811	823	835	847	859	9.1
62	871	883	895	907	919	931	943	955	967	979	10.4
63	991	*003	*015	*027	*038	*050	*062	*074	*086	*098	11.7
64	56	110	122	134	146	158	170	182	194	205	217
65	229	241	253	265	277	289	301	312	324	336	
66	348	360	372	384	396	407	419	431	443	455	1.2
67	467	478	490	502	514	526	538	549	561	573	2.4
68	585	597	608	620	632	644	656	667	679	691	3.6
69	703	714	726	738	750	761	773	785	797	808	4.8
370	820	832	844	855	867	879	891	902	914	926	6.0
71	937	949	961	972	984	996	*008	*019	*031	*043	7.2
72	57	054	066	078	089	101	113	124	136	148	8.4
73	171	183	194	206	217	229	241	252	264	276	9.6
74	287	299	310	322	334	345	357	368	380	392	
75	403	415	426	438	449	461	473	484	496	507	
76	519	530	542	553	565	576	588	600	611	623	
77	634	646	657	669	680	692	703	715	726	738	
78	749	761	772	784	795	807	818	830	841	852	1.1
79	864	875	887	898	910	921	933	944	955	967	2.2
380	978	990	*001	*013	*024	*035	*047	*058	*070	*081	3.3
81	58	092	104	115	127	138	149	161	172	184	4.4
82	206	218	229	240	252	263	274	286	297	309	5.5
83	320	331	343	354	365	377	388	399	410	422	6.6
84	433	444	456	467	478	490	501	512	524	535	7.7
85	546	557	569	580	591	602	614	625	636	647	8.8
86	659	670	681	692	704	715	726	737	749	760	9.9
87	771	782	794	805	816	827	838	850	861	872	
88	883	894	906	917	928	939	950	961	973	984	
89	995	*006	*017	*028	*040	*051	*062	*073	*084	*095	10
390	59	106	118	129	140	151	162	173	184	195	207
91	218	229	240	251	262	273	284	295	306	318	2.0
92	329	340	351	362	373	384	395	406	417	428	3.0
93	439	450	461	472	483	494	506	517	528	539	4.0
94	550	561	572	583	594	605	616	627	638	649	5.0
95	660	671	682	693	704	715	726	737	748	759	6.0
96	770	780	791	802	813	824	835	846	857	868	7.0
97	879	890	901	912	923	934	945	956	966	977	
98	988	999	*010	*021	*032	*043	*054	*065	*076	*086	
99	60	097	108	119	130	141	152	163	173	184	195
400	206	217	228	239	249	260	271	282	293	304	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
400	60	206	217	228	239	249	260	271	282	293	304
01	314	325	336	347	358	369	379	390	401	412	
02	423	433	444	455	466	477	487	498	509	520	
03	531	541	552	563	574	584	595	606	617	627	
04	638	649	660	670	681	692	703	713	724	735	
05	746	756	767	778	788	799	810	821	831	842	
06	853	863	874	885	895	906	917	927	938	949	
07	959	970	981	991	*002	*013	*023	*034	*045	*055	11
08	61	066	077	087	098	109	119	130	140	151	162
09		172	183	194	204	215	225	236	247	257	268
410		278	289	300	310	321	331	342	352	363	374
11		384	395	405	416	426	437	448	458	469	479
12		490	500	511	521	532	542	553	563	574	584
13		595	606	616	627	637	648	658	669	679	690
14		700	711	721	731	742	752	763	773	784	794
15		805	815	826	836	847	857	868	878	888	899
16		909	920	930	941	951	962	972	982	993	*003
17	62	014	024	034	045	055	066	076	086	097	107
18		118	128	138	149	159	170	180	190	201	211
19		221	232	242	252	263	273	284	294	304	315
420		325	335	346	356	366	377	387	397	408	418
21		428	439	449	459	469	480	490	500	511	521
22		531	542	552	562	572	583	593	603	613	624
23		634	644	655	665	675	685	696	706	716	726
24		737	747	757	767	778	788	798	808	818	829
25		839	849	859	870	880	890	900	910	921	931
26		941	951	961	972	982	992	*002	*012	*022	*033
27	63	043	053	063	073	083	094	104	114	124	134
28		144	155	165	175	185	195	205	215	225	236
29		246	256	266	276	286	296	306	317	327	337
430		347	357	367	377	387	397	407	417	428	438
31		448	458	468	478	488	498	508	518	528	538
32		548	558	568	579	589	599	609	619	629	639
33		649	659	669	679	689	699	709	719	729	739
34		749	759	769	779	789	799	809	819	829	839
35		849	859	869	879	889	899	909	919	929	939
36		949	959	969	979	988	998	*008	*018	*028	*038
37	64	048	058	068	078	088	098	108	118	128	137
38		147	157	167	177	187	197	207	217	227	237
39		246	256	266	276	286	296	306	316	326	335
440		345	355	365	375	385	395	404	414	424	434
41		444	454	464	473	483	493	503	513	523	532
42		542	552	562	572	582	591	601	611	621	631
43		640	650	660	670	680	689	699	709	719	729
44		738	748	758	768	777	787	797	807	816	826
45		836	846	856	865	875	885	895	904	914	924
46		933	943	953	963	972	982	992	*002	*011	*021
47	65	031	040	050	060	070	079	089	099	108	118
48		128	137	147	157	167	176	186	196	205	215
49		225	234	244	254	263	273	283	292	302	312
450		321	331	341	350	360	369	379	389	398	408
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

## LOGARITHMS OF NUMBERS.

9

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
450	65	321	331	341	350	360	369	379	389	398	408
51	418	427	437	447	456	466	475	485	495	504	
52	514	523	533	543	552	562	571	581	591	600	
53	610	619	629	639	648	658	667	677	686	696	
54	706	715	725	734	744	753	763	772	782	792	
55	801	811	820	830	839	849	858	868	877	887	
56	896	906	916	925	935	944	954	963	973	982	
57	992	*001	*011	*020	*030	*039	*049	*058	*068	*077	10
58	66	087	096	106	115	124	134	143	153	162	172
59		181	191	200	210	219	229	238	247	257	266
460	276	285	295	304	314	323	332	342	351	361	
61	370	380	389	398	408	417	427	436	445	455	5
62	464	474	483	492	502	511	521	530	539	549	6
63	558	567	577	586	596	605	614	624	633	642	7
64	652	661	671	680	689	699	708	717	727	736	8
65	745	755	764	773	783	792	801	811	820	829	9
66	839	848	857	867	876	885	894	904	913	922	
67	67	932	941	950	960	969	978	987	997	*006	*015
68		025	034	043	052	062	071	080	089	099	108
69		117	127	136	145	154	164	173	182	191	201
470	210	219	228	237	247	256	265	274	284	293	
71	302	311	321	330	339	348	357	367	376	385	9
72	394	403	413	422	431	440	449	459	468	477	1
73	486	495	504	514	523	532	541	550	560	569	2
74	578	587	596	605	614	624	633	642	651	660	3
75	669	679	688	697	706	715	724	733	742	752	4
76	761	770	779	788	797	806	815	825	834	843	5
77	852	861	870	879	888	897	906	916	925	934	6
78	68	943	952	961	970	979	988	997	*006	*015	7
79		034	043	052	061	070	079	088	097	106	115
480	124	133	142	151	160	169	178	187	196	205	
81	215	224	233	242	251	260	269	278	287	296	
82	305	314	323	332	341	350	359	368	377	386	
83	395	404	413	422	431	440	449	458	467	476	
84	485	494	502	511	520	529	538	547	556	565	
85	574	583	592	601	610	619	628	637	646	655	
86	664	673	681	690	699	708	717	726	735	744	
87	753	762	771	780	789	797	806	815	824	833	1
88	842	851	860	869	878	886	895	904	913	922	2
89	931	940	949	958	966	975	984	993	*002	*011	3
490	69	020	028	037	046	055	064	073	082	090	099
91	108	117	126	135	144	152	161	170	179	188	4
92	197	205	214	223	232	241	249	258	267	276	5
93	285	294	302	311	320	329	338	346	355	364	6
94	373	381	390	399	408	417	425	434	443	452	7
95	461	469	478	487	496	504	513	522	531	539	8
96	548	557	566	574	583	592	601	609	618	627	
97	636	644	653	662	671	679	688	697	705	714	
98	723	732	740	749	758	767	775	784	793	801	
99	810	819	827	836	845	854	862	871	880	888	
500		897	906	914	923	932	940	949	958	966	975
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
500	69	897	906	914	923	932	940	949	958	966	975
01	984	992	*001	*010	*018	*027	*036	*044	*053	*062	
02	70	070	079	088	096	105	114	122	131	140	148
03	157	165	174	183	191	200	209	217	226	234	
04	243	252	260	269	278	286	295	303	312	321	
05	329	338	346	355	364	372	381	389	398	406	
06	415	424	432	441	449	458	467	475	484	492	
07	501	509	518	526	535	544	552	561	569	578	
08	586	595	603	612	621	629	638	646	655	663	
09	672	680	689	697	706	714	723	731	740	749	
510	757	766	774	783	791	800	808	817	825	834	
11	842	851	859	868	876	885	893	902	910	919	
12	927	935	944	952	961	969	978	986	995	*003	
13	71	012	020	029	037	046	054	063	071	079	088
14	096	105	113	122	130	139	147	155	164	172	
15	181	189	198	206	214	223	231	240	248	257	
16	265	273	282	290	299	307	315	324	332	341	
17	349	357	366	374	383	391	399	408	416	425	
18	433	441	450	458	466	475	483	492	500	508	
19	517	525	533	542	550	559	567	575	584	592	
520	600	609	617	625	634	642	650	659	667	675	
21	684	692	700	709	717	725	734	742	750	759	
22	767	775	784	792	800	809	817	825	834	842	
23	850	858	867	875	883	892	900	908	917	925	
24	933	941	950	958	966	975	983	991	999	*008	
25	72	016	024	032	041	049	057	066	074	082	090
26	099	107	115	123	132	140	148	156	165	173	
27	181	189	198	206	214	222	230	239	247	255	
28	263	272	280	288	296	304	313	321	329	337	
29	346	354	362	370	378	387	395	403	411	419	
530	428	436	444	452	460	469	477	485	493	501	
31	509	518	526	534	542	550	558	567	575	583	
32	591	599	607	616	624	632	640	648	656	665	
33	673	681	689	697	705	713	722	730	738	746	
34	754	762	770	779	787	795	803	811	819	827	
35	835	843	852	860	868	876	884	892	900	908	
36	916	925	933	941	949	957	965	973	981	989	
37	997	*006	*014	*022	*030	*038	*046	*054	*062	*070	
38	73	078	086	094	102	111	119	127	135	143	151
39	159	167	175	183	191	199	207	215	223	231	
540	239	247	255	263	272	280	288	296	304	312	
41	320	328	336	344	352	360	368	376	384	392	
42	400	408	416	424	432	440	448	456	464	472	
43	480	488	496	504	512	520	528	536	544	552	
44	560	568	576	584	592	600	608	616	624	632	
45	640	648	656	664	672	679	687	695	703	711	
46	719	727	735	743	751	759	767	775	783	791	
47	799	807	815	823	830	838	846	854	862	870	
48	878	886	894	902	910	918	926	933	941	949	
49	957	965	973	981	989	997	*005	*013	*029	*028	
550	74	036	044	052	060	068	076	084	092	099	107
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
550	74 036	044	052	060	068	076	084	092	099	107	
51	115	123	131	139	147	155	162	170	178	186	
52	194	202	210	218	225	233	241	249	257	265	
53	273	280	288	296	304	312	320	327	335	343	
54	351	359	367	374	382	390	398	406	414	421	
55	429	437	445	453	461	468	476	484	492	500	
56	507	515	523	531	539	547	554	562	570	578	
57	586	593	601	609	617	624	632	640	648	656	
58	663	671	679	687	695	702	710	718	726	733	
59	741	749	757	764	772	780	788	796	803	811	
560	819	827	834	842	850	858	865	873	881	889	
61	896	904	912	920	927	935	943	950	958	966	
62	974	981	989	997	*005	*012	*020	*028	*035	*043	1 0.8
63	75 051	059	066	074	082	089	097	105	113	120	2 1.6
64	128	136	143	151	159	166	174	182	189	197	3 2.4
65	205	213	220	228	236	243	251	259	266	274	4 3.2
66	282	289	297	305	312	320	328	335	343	351	5 4.0
67	358	366	374	381	389	397	404	412	420	427	6 4.8
68	435	442	450	458	465	473	481	488	496	504	8 6.4
69	511	519	526	534	542	549	557	565	572	580	9 7.2
570	587	595	603	610	618	626	633	641	648	656	
71	664	671	679	686	694	702	709	717	724	732	
72	740	747	755	762	770	778	785	793	800	808	
73	815	823	831	838	846	853	861	868	876	884	
74	891	899	906	914	921	929	937	944	952	959	
75	967	974	982	989	997	*005	*012	*020	*027	*035	
76	76 042	050	057	065	072	080	087	095	103	110	
77	118	125	133	140	148	155	163	170	178	185	
78	193	200	208	215	223	230	238	245	253	260	
79	268	275	283	290	298	305	313	320	328	335	
580	343	350	358	365	373	380	388	395	403	410	
81	418	425	433	440	448	455	462	470	477	485	
82	492	500	507	515	522	530	537	545	552	559	1 0.7
83	567	574	582	589	597	604	612	619	626	634	2 1.4
84	641	649	656	664	671	678	686	693	701	708	3 2.1
85	716	723	730	738	745	753	760	768	775	782	4 2.8
86	790	797	805	812	819	827	834	842	849	856	5 3.5
87	864	871	879	886	893	901	908	916	923	930	6 4.2
88	938	945	953	960	967	975	982	989	997	*004	7 4.9
89	77 012	019	026	034	041	048	056	063	070	078	8 5.6
590	085	093	100	107	115	122	129	137	144	151	9 6.3
91	159	166	173	181	188	195	203	210	217	225	
92	232	240	247	254	262	269	276	283	291	298	
93	305	313	320	327	335	342	349	357	364	371	
94	379	386	393	401	408	415	422	430	437	444	
95	452	459	466	474	481	488	495	503	510	517	
96	525	532	539	546	554	561	568	576	583	590	
97	597	605	612	619	627	634	641	648	656	663	
98	670	677	685	692	699	706	714	721	728	735	
99	743	750	757	764	772	779	786	793	801	808	
600	815	822	830	837	844	851	859	866	873	880	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3.	4	5	6	7	8	9	Prop. Pts.
600	77	815	822	830	837	844	851	859	866	873	880
01	887	895	902	909	916	924	931	938	945	952	
02	960	967	974	981	988	996	*003	*010	*017	*025	
03	78	032	039	046	053	061	068	075	082	089	097
04	104	111	118	125	132	140	147	154	161	168	
05	176	183	190	197	204	211	219	226	233	240	
06	247	254	262	269	276	283	290	297	305	312	
07	319	326	333	340	347	355	362	369	376	383	8
08	390	398	405	412	419	426	433	440	447	455	10.8
09	462	469	476	483	490	497	504	512	519	526	21.6
610	533	540	547	554	561	569	576	583	590	597	32.4
11	604	611	618	625	633	640	647	654	661	668	43.2
12	675	682	689	696	704	711	718	725	732	739	54.0
13	746	753	760	767	774	781	789	796	803	810	64.8
14	817	824	831	838	845	852	859	866	873	880	75.6
15	888	895	902	909	916	923	930	937	944	951	86.4
16	958	965	972	979	986	993	*000	*007	*014	*021	97.2
17	79	029	036	043	050	057	064	071	078	085	092
18	099	106	113	120	127	134	141	148	155	162	
19	169	176	183	190	197	204	211	218	225	232	
620	239	246	253	260	267	274	281	288	295	302	
21	309	316	323	330	337	344	351	358	365	372	7
22	379	386	393	400	407	414	421	428	435	442	10.7
23	449	456	463	470	477	484	491	498	505	511	21.4
24	518	525	532	539	546	553	560	567	574	581	32.1
25	588	595	602	609	616	623	630	637	644	650	42.8
26	657	664	671	678	685	692	699	706	713	720	53.5
27	727	734	741	748	754	761	768	775	782	789	64.2
28	796	803	810	817	824	831	837	844	851	858	74.9
29	865	872	879	886	893	900	906	913	920	927	85.6
630	934	941	948	955	962	969	975	982	989	996	
31	80	003	010	017	024	030	037	044	051	058	065
32	072	079	085	092	099	106	113	120	127	134	
33	140	147	154	161	168	175	182	188	195	202	
34	209	216	223	229	236	243	250	257	264	271	
35	277	284	291	298	305	312	318	325	332	339	
36	346	353	359	366	373	380	387	393	400	407	
37	414	421	428	434	441	448	455	462	468	475	6
38	482	489	496	502	509	516	523	530	536	543	10.6
39	550	557	564	570	577	584	591	598	604	611	21.2
640	618	625	632	638	645	652	659	665	672	679	31.8
41	686	693	699	706	713	720	726	733	740	747	42.4
42	754	760	767	774	781	787	794	801	808	814	53.0
43	821	828	835	841	848	855	862	868	875	882	63.6
44	889	895	902	909	916	922	929	936	943	949	74.2
45	956	963	969	976	983	990	996	*003	*010	*017	84.8
46	81	023	030	037	043	050	057	064	070	077	084
47	090	097	104	111	117	124	131	137	144	151	
48	158	164	171	178	184	191	198	204	211	218	
49	224	231	238	245	251	258	265	271	278	285	
650	291	298	305	311	318	325	331	338	345	351	
N.	0	1	2	3	4	5	6	7	8	9	Prop Pts.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
	81	291	298	305	311	318	325	331	338	345	
650	81	291	298	305	311	318	325	331	338	345	351
51	358	365	371	378	385	391	398	405	411	418	
52	425	431	438	445	451	458	465	471	478	485	
53	491	498	505	511	518	525	531	538	544	551	
54	558	564	571	578	584	591	598	604	611	617	
55	624	631	637	644	651	657	664	671	677	684	
56	690	697	704	710	717	723	730	737	743	750	
57	757	763	770	776	783	790	796	803	809	816	
58	823	829	836	842	849	856	862	869	875	882	
59	889	895	902	908	915	921	928	935	941	948	
660	954	961	968	974	981	987	994	*000	*007	*014	
61	82	020	027	033	040	046	053	060	066	073	079
62	086	092	099	105	112	119	125	132	138	145	10.7
63	151	158	164	171	178	184	191	197	204	210	21.4
64	217	223	230	236	243	249	256	263	269	276	32.1
65	282	289	295	302	308	315	321	328	334	341	42.8
66	347	354	360	367	373	380	387	393	400	406	53.5
67	413	419	426	432	439	445	452	458	465	471	64.2
68	478	484	491	497	504	510	517	523	530	536	85.6
69	543	549	556	562	569	575	582	588	595	601	96.3
670	607	614	620	627	633	640	646	653	659	666	
71	672	679	685	692	698	705	711	718	724	730	
72	737	743	750	756	763	769	776	782	789	795	
73	802	808	814	821	827	834	840	847	853	860	
74	866	872	879	885	892	898	905	911	918	924	
75	930	937	943	950	956	963	969	975	982	988	
76	995	*001	*008	*014	*020	*027	*033	*040	*046	*052	
77	83	059	065	072	078	085	091	097	104	110	117
78	123	129	136	142	149	155	161	168	174	181	
79	187	193	200	206	213	219	225	232	238	245	
680	251	257	264	270	276	283	289	296	302	308	
81	315	321	327	334	340	347	353	359	366	372	6
82	378	385	391	398	404	410	417	423	429	436	10.6
83	442	448	455	461	467	474	480	487	493	499	21.2
84	506	512	518	525	531	537	544	550	556	563	31.8
85	569	575	582	588	594	601	607	613	620	626	42.4
86	632	639	645	651	658	664	670	677	683	689	53.0
87	696	702	708	715	721	727	734	740	746	753	63.6
88	759	765	771	778	784	790	797	803	809	816	74.2
89	822	828	835	841	847	853	860	866	872	879	84.8
690	885	891	897	904	910	916	923	929	935	942	
91	948	954	960	967	973	979	985	992	998	*004	
92	84	011	017	023	029	036	042	048	055	061	067
93	073	080	086	092	098	105	111	117	123	130	
94	136	142	148	155	161	167	173	180	186	192	
95	198	205	211	217	223	230	236	242	248	255	
96	261	267	273	280	286	292	298	305	311	317	
97	323	330	336	342	348	354	361	367	373	379	
98	386	392	398	404	410	417	423	429	435	442	
99	448	454	460	466	473	479	485	491	497	504	
700	510	516	522	528	535	541	547	553	559	566	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
700	84	510	516	522	528	535	541	547	553	559	566
01	572	578	584	590	597	603	609	615	621	628	
02	634	640	646	652	658	665	671	677	683	689	
03	696	702	708	714	720	726	733	739	745	751	
04	757	763	770	776	782	788	794	800	807	813	
05	819	825	831	837	844	850	856	862	868	874	
06	880	887	893	899	905	911	917	924	930	936	
07	942	948	954	960	967	973	979	985	991	997	7
08	85	003	009	016	022	028	034	040	046	052	10.7
09		065	071	077	083	089	095	101	107	114	21.4
10		126	132	138	144	150	156	163	169	175	32.1
11		187	193	199	205	211	217	224	230	236	42.8
12		248	254	260	266	272	278	285	291	297	53.5
13		309	315	321	327	333	339	345	352	358	64.2
14		370	376	382	388	394	400	406	412	418	74.9
15		431	437	443	449	455	461	467	473	479	85.6
16		491	497	503	509	516	522	528	534	540	96.3
17		552	558	564	570	576	582	588	594	600	606
18		612	618	625	631	637	643	649	655	661	
19		673	679	685	691	697	703	709	715	721	
720		733	739	745	751	757	763	769	775	781	788
21		794	800	806	812	818	824	830	836	842	848
22		854	860	866	872	878	884	890	896	902	908
23		914	920	926	932	938	944	950	956	962	968
24		974	980	986	992	998	*004	*010	*016	*022	*028
25	86	034	040	046	052	058	064	070	076	082	10.6
26		094	100	106	112	118	124	130	136	141	21.2
27		153	159	165	171	177	183	189	195	201	31.8
28		213	219	225	231	237	243	249	255	261	42.4
29		273	279	285	291	297	303	308	314	320	53.0
730		332	338	344	350	356	362	368	374	380	63.6
31		392	390	404	410	415	421	427	433	439	74.2
32		451	457	463	469	475	481	487	493	499	84.8
33		510	516	522	528	534	540	546	552	558	95.4
34		570	576	581	587	593	599	605	611	617	623
35		629	635	641	646	652	658	664	670	676	682
36		688	694	700	705	711	717	723	729	735	741
37		747	753	759	764	770	776	782	788	794	800
38		806	812	817	823	829	835	841	847	853	859
39		864	870	876	882	888	894	900	906	911	917
740		923	929	935	941	947	953	958	964	970	976
41		982	988	994	999	*005	*011	*017	*023	*029	52.0
42	87	040	046	052	058	064	070	075	081	087	63.0
43		099	105	111	116	122	128	134	140	146	73.5
44		157	163	169	175	181	186	192	198	204	84.0
45		216	221	227	233	239	245	251	256	262	94.5
46		274	280	286	291	297	303	309	315	320	
47		332	338	344	349	355	361	367	373	379	384
48		390	396	402	408	413	419	425	431	437	442
49		448	454	460	466	471	477	483	489	495	500
750		506	512	518	523	529	535	541	547	553	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
750	87	506	512	518	523	529	535	541	547	552	558
51		564	570	576	581	587	593	599	604	610	616
52		622	628	633	639	645	651	656	662	668	674
53		679	685	691	697	703	708	714	720	726	731
54		737	743	749	754	760	766	772	777	783	789
55		795	800	806	812	818	823	829	835	841	846
56		852	858	864	869	875	881	887	892	898	904
57		910	915	921	927	933	938	944	950	955	961
58		967	973	978	984	990	996	*001	*007	*013	*018
59	88	024	030	036	041	047	053	058	064	070	076
760		081	087	093	098	104	110	116	121	127	133
61		138	144	150	156	161	167	173	173	184	190
62		195	201	207	213	218	224	230	235	241	247
63		252	258	264	270	275	281	287	292	298	304
64		309	315	321	326	332	338	343	349	355	360
65		366	372	377	383	389	395	400	406	412	417
66		423	429	434	440	446	451	457	463	468	474
67		480	485	491	497	502	508	513	519	525	530
68		536	542	547	553	559	564	570	576	581	587
69		593	598	604	610	615	621	627	632	638	643
770		649	655	660	666	672	677	683	689	694	700
71		705	711	717	722	728	734	739	745	750	756
72		762	767	773	779	784	790	795	801	807	812
73		818	824	829	835	840	846	852	857	863	868
74		874	880	885	891	897	902	908	913	919	925
75		930	936	941	947	953	958	964	969	975	981
76		986	992	997	*003	*009	*014	*020	*025	*031	*037
77	89	042	048	053	059	064	070	076	081	087	092
78		098	104	109	115	120	126	131	137	143	148
79		154	159	165	170	176	182	187	193	198	204
780		209	215	221	226	232	237	243	248	254	260
81		265	271	276	282	287	293	298	304	310	315
82		321	326	332	337	343	348	354	360	365	371
83		376	382	387	393	398	404	409	415	421	426
84		432	437	443	448	454	459	465	470	476	481
85		487	492	498	504	509	515	520	526	531	537
86		542	548	553	559	564	570	575	581	586	592
87		597	603	609	614	620	625	631	636	642	647
88		653	658	664	669	675	680	686	691	697	702
89		708	713	719	724	730	735	741	746	752	757
790		763	768	774	779	785	790	796	801	807	812
91		818	823	829	834	840	845	851	856	862	867
92		873	878	883	889	894	900	905	911	916	922
93		927	933	938	944	949	955	960	966	971	977
94		982	988	993	998	*004	*009	*015	*020	*026	*031
95	90	037	042	048	053	059	064	069	075	080	086
96		091	097	102	108	113	119	124	129	135	140
97		146	151	157	162	168	173	179	184	189	195
98		200	206	211	217	222	227	233	238	244	249
99		255	260	266	271	276	282	287	293	298	304
800		309	314	320	325	331	336	342	347	352	358
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
800	90	309	314	320	325	331	336	342	347	352	358
01	363	369	374	380	385	390	396	401	407	412	
02	417	423	428	434	439	445	450	455	461	466	
03	472	477	482	488	493	499	504	509	515	520	
04	526	531	536	542	547	553	558	563	569	574	
05	580	585	590	596	601	607	612	617	623	628	
06	634	639	644	650	655	660	666	671	677	682	
07	687	693	698	703	709	714	720	725	730	736	
08	741	747	752	757	763	768	773	779	784	789	
09	795	800	806	811	816	822	827	833	838	843	
810	849	854	859	865	870	875	881	886	891	897	
11	902	907	913	918	924	929	934	940	945	950	
12	956	961	966	972	977	982	988	993	998	*004	
13	91	009	014	020	025	030	036	041	046	052	057
14	062	068	073	078	084	089	094	100	105	110	
15	116	121	126	132	137	142	148	153	158	164	
16	169	174	180	185	190	196	201	206	212	217	
17	222	228	233	238	243	249	254	259	265	270	
18	275	281	286	291	297	302	307	312	318	323	
19	328	334	339	344	350	355	360	365	371	376	
820	381	387	392	397	403	408	413	418	424	429	
21	434	440	445	450	455	461	466	471	477	482	
22	487	492	498	503	508	514	519	524	529	535	
23	540	545	551	556	561	566	572	577	582	587	
24	593	598	603	609	614	619	624	630	635	640	
25	645	651	656	661	666	672	677	682	687	693	
26	698	703	709	714	719	724	730	735	740	745	
27	751	756	761	766	772	777	782	787	793	798	
28	803	808	814	819	824	829	834	840	845	850	
29	855	861	866	871	876	882	887	892	897	903	
830	908	913	918	924	929	934	939	944	950	955	
31	960	965	971	976	981	986	991	997	*002	*007	
32	92	012	018	023	028	033	038	044	049	054	059
33	065	070	075	080	085	091	096	101	106	111	
34	117	122	127	132	137	143	148	153	158	163	
35	169	174	179	184	189	195	200	205	210	215	
36	221	226	231	236	241	247	252	257	262	267	
37	273	278	283	288	293	298	304	309	314	319	
38	324	330	335	340	345	350	355	361	366	371	
39	376	381	387	392	397	402	407	412	418	423	
840	428	433	438	443	449	454	459	464	469	474	
41	480	485	490	495	500	505	511	516	521	526	
42	531	536	542	547	552	557	562	567	572	578	
43	583	588	593	598	603	609	614	619	624	629	
44	634	639	645	650	655	660	665	670	675	681	
45	686	691	696	701	706	711	716	722	727	732	
46	737	742	747	752	758	763	768	773	778	783	
47	788	793	799	804	809	814	819	824	829	834	
48	840	845	850	855	860	865	870	875	881	886	
49	891	896	901	906	911	916	921	927	932	937	
850	942	947	952	957	962	967	973	978	983	988	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

6  
10.6  
21.2  
31.8  
42.4  
53.0  
63.6  
74.2  
84.8  
95.4

5  
10.5  
21.0  
31.5  
42.0  
52.5  
63.0  
73.5  
84.0  
94.5

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
850	92	942	947	952	957	962	967	973	978	983	988
51		993	998	*003	*008	*013	*018	*024	*029	*034	*039
52	93	044	049	054	059	064	069	075	080	085	090
53		095	100	105	110	115	120	125	131	136	141
54		146	151	156	161	166	171	176	181	186	192
55		197	202	207	212	217	222	227	232	237	242
56		247	252	258	263	268	273	278	283	288	293
57		298	303	308	313	318	323	328	334	339	344
58		349	354	359	364	369	374	379	384	389	394
59		399	404	409	414	420	425	430	435	440	445
860		450	455	460	465	470	475	480	485	490	495
61		500	505	510	515	520	526	531	536	541	546
62		551	556	561	566	571	576	581	586	591	596
63		601	606	611	616	621	626	631	636	641	646
64		651	656	661	666	671	676	682	687	692	697
65		702	707	712	717	722	727	732	737	742	747
66		752	757	762	767	772	777	782	787	792	797
67		802	807	812	817	822	827	832	837	842	847
68		852	857	862	867	872	877	882	887	892	897
69		902	907	912	917	922	927	932	937	942	947
870		952	957	962	967	972	977	982	987	992	997
71	94	002	007	012	017	022	027	032	037	042	047
72		052	057	062	067	072	077	082	086	091	096
73		101	106	111	116	121	126	131	136	141	146
74		151	156	161	166	171	176	181	186	191	196
75		201	206	211	216	221	226	231	236	240	245
76		250	255	260	265	270	275	280	285	290	295
77		300	305	310	315	320	325	330	335	340	345
78		349	354	359	364	369	374	379	384	389	394
79		399	404	409	414	419	424	429	433	438	443
880		448	453	458	463	468	473	478	483	488	493
81		498	503	507	512	517	522	527	532	537	542
82		547	552	557	562	567	571	576	581	586	591
83		596	601	606	611	616	621	626	630	635	640
84		645	650	655	660	665	670	675	680	685	689
85		694	699	704	709	714	719	724	729	734	738
86		743	748	753	758	763	768	773	778	783	787
87		792	797	802	807	812	817	822	827	832	836
88		841	846	851	856	861	866	871	876	880	885
89		890	895	900	905	910	915	919	924	929	934
890		939	944	949	954	959	963	968	973	978	983
91		988	993	998	*002	*007	*012	*017	*022	*027	*032
92	95	036	041	046	051	056	061	066	071	075	080
93		085	090	095	100	105	109	114	119	124	129
94		134	139	143	148	153	158	163	168	173	177
95		182	187	192	197	202	207	211	216	221	226
96		231	236	240	245	250	255	260	265	270	274
97		279	284	289	294	299	303	308	313	318	323
98		328	332	337	342	347	352	357	361	366	371
99		376	381	386	390	395	400	405	410	415	419
900		424	429	434	439	444	448	453	458	463	468
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
900	95	424	429	434	439	444	448	453	458	463	468
01	472	477	482	487	492	497	501	506	511	516	
02	521	525	530	535	540	545	550	554	559	564	
03	569	574	578	583	588	593	598	602	607	612	
04	617	622	626	631	636	641	646	650	655	660	
05	665	670	674	679	684	689	694	698	703	708	
06	713	718	722	727	732	737	742	746	751	756	
07	761	766	770	775	780	785	789	794	799	804	
08	809	813	818	823	828	832	837	842	847	852	
09	856	861	866	871	875	880	885	890	895	899	
910	904	909	914	918	923	928	933	938	942	947	
11	952	957	961	966	971	976	980	985	990	995	5
12	999	*004	*009	*014	*019	*023	*028	*033	*038	*042	10.5
13	96	047	052	057	061	066	071	076	080	085	21.0
14	095	099	104	109	114	118	123	128	133	137	31.5
15	142	147	152	156	161	166	171	175	180	185	42.0
16	190	194	199	204	209	213	218	223	227	232	52.5
17	237	242	246	251	256	261	265	270	275	280	63.0
18	284	289	294	298	303	308	313	317	322	327	73.5
19	332	336	341	346	350	355	360	365	369	374	84.0
920	379	384	388	393	398	402	407	412	417	421	
21	426	431	435	440	445	450	454	459	464	468	
22	473	478	483	487	492	497	501	506	511	515	
23	520	525	530	534	539	544	548	553	558	562	
24	567	572	577	581	586	591	595	600	605	609	
25	614	619	624	628	633	638	642	647	652	656	
26	661	666	670	675	680	685	689	694	699	703	
27	708	713	717	722	727	731	736	741	745	750	
28	755	759	764	769	774	778	783	788	792	797	
29	802	806	811	816	820	825	830	834	839	844	
930	848	853	858	862	867	872	876	881	886	890	
31	895	900	904	909	914	918	923	928	932	937	4
32	942	946	951	956	960	965	970	974	979	984	10.4
33	988	993	997	*002	*007	*011	*016	*021	*025	*030	20.8
34	97	035	039	044	049	053	058	063	067	072	077
35	081	086	090	095	100	104	109	114	118	123	1.2
36	128	132	137	142	146	151	155	160	165	169	41.6
37	174	179	183	188	192	197	202	206	211	216	52.0
38	220	225	230	234	239	243	248	253	257	262	62.4
39	267	271	276	280	285	290	294	299	304	308	72.8
940	313	317	322	327	331	336	340	345	350	354	
41	359	364	368	373	377	382	387	391	396	400	
42	405	410	414	419	424	428	433	437	442	447	
43	451	456	460	465	470	474	479	483	488	493	
44	497	502	506	511	516	520	525	529	534	539	
45	543	548	552	557	562	566	571	575	580	585	
46	589	594	598	603	607	612	617	621	626	630	
47	635	640	644	649	653	658	663	667	672	676	
48	681	685	690	695	699	704	708	713	717	722	
49	727	731	736	740	745	749	754	759	763	768	
950	772	777	782	786	791	795	800	804	809	813	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
950	97	772	777	782	786	791	795	800	804	809	813
51		818	823	827	832	836	841	845	850	855	859
52		864	868	873	877	882	886	891	896	900	905
53		909	914	918	923	928	932	937	941	946	950
54		955	959	964	968	973	978	982	987	991	.996
55	98	000	005	009	014	019	023	028	032	037	041
56		046	050	055	059	064	068	073	078	082	087
57		091	096	100	105	109	114	118	123	127	132
58		137	141	146	150	155	159	164	168	173	177
59		182	186	191	195	200	204	209	214	218	223
960		227	232	236	241	245	250	254	259	263	268
61		272	277	281	286	290	295	299	304	308	313
62		318	322	327	331	336	340	345	349	354	358
63		363	367	372	376	381	385	390	394	399	403
64		408	412	417	421	426	430	435	439	444	448
65		453	457	462	466	471	475	480	484	489	493
66		498	502	507	511	516	520	525	529	534	538
67		543	547	552	556	561	565	570	574	579	583
68		588	592	597	601	605	610	614	619	623	628
69		632	637	641	646	650	655	659	664	668	673
970		677	682	686	691	695	700	704	709	713	717
71		722	726	731	735	740	744	749	753	758	762
72		767	771	776	780	784	789	793	798	802	807
73		811	816	820	825	829	834	838	843	847	851
74		856	860	865	869	874	878	883	887	892	896
75		900	905	909	914	918	923	927	932	936	941
76		945	949	954	958	963	967	972	976	981	985
77	99	989	994	998	*003	*007	*012	*016	*021	*025	*029
78		034	038	043	047	052	056	061	065	069	074
79		078	083	087	092	096	100	105	109	114	118
980		123	127	131	136	140	145	149	154	158	162
81		167	171	176	180	185	189	193	198	202	207
82		211	216	220	224	229	233	238	242	247	251
83		255	260	264	269	273	277	282	286	291	295
84		300	304	308	313	317	322	326	330	335	339
85		344	348	352	357	361	366	370	374	379	383
86		388	392	396	401	405	410	414	419	423	427
87		432	436	441	445	449	454	458	463	467	471
88		476	480	484	489	493	498	502	506	511	515
89		520	524	528	533	537	542	546	550	555	559
990		564	568	572	577	581	585	590	594	599	603
91		607	612	616	621	625	629	634	638	642	647
92		651	656	660	664	669	673	677	682	686	691
93		695	699	704	708	712	717	721	726	730	734
94		739	743	747	752	756	760	765	769	774	778
95		782	787	791	795	800	804	808	813	817	822
96		826	830	835	839	843	848	852	856	861	865
97		870	874	878	883	887	891	896	900	904	909
98		913	917	922	926	930	935	939	944	948	952
99		957	961	965	970	974	978	983	987	991	996
1000	00	000	004	009	013	017	022	026	030	035	039
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE I.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
1000	000	000	043	087	130	174	217	260	304	347	391
1001	434	477	521	564	608	651	694	738	781	824	
1002	868	911	954	998	*041	*084	*128	*171	*214	*258	
1003	001	301	344	388	431	474	517	561	604	647	690
1004	734	777	820	863	907	950	993	*036	*080	*123	44
1005	002	166	209	252	296	339	382	425	468	512	555
1006	598	641	684	727	771	814	857	900	943	986	3
1007	003	029	073	116	159	202	245	288	331	374	417
1008	461	504	547	590	633	676	719	762	805	848	17.6
1009	891	934	977	*020	*063	*106	*149	*192	*235	*278	522.0
1010	004	321	364	407	450	493	536	579	622	665	708
1011	751	794	837	880	923	966	*009	*052	*095	*138	35.2
1012	005	180	223	266	309	352	395	438	481	524	567
1013	609	652	695	738	781	824	867	909	952	995	13.2
1014	006	038	081	124	166	209	252	295	338	380	423
1015	466	509	552	594	637	680	723	765	808	851	4.3
1016	894	936	979	*022	*065	*107	*150	*193	*236	*278	2.8.6
1017	007	321	364	406	449	492	534	577	620	662	705
1018	748	790	833	876	918	961	*004	*046	*089	*132	12.9
1019	008	174	217	259	302	345	387	430	472	515	558
1020	600	643	685	728	770	813	856	898	941	983	17.2
1021	009	026	068	111	153	196	238	281	323	366	408
1022	451	493	536	578	621	663	706	748	791	833	30.1
1023	876	918	961	*003	*045	*088	*130	*173	*215	*258	34.4
1024	010	300	342	385	427	470	512	554	597	639	681
1025	724	766	809	851	893	936	978	*020	*063	*105	21.5
1026	011	147	190	232	274	317	359	401	444	486	528
1027	570	613	655	697	740	782	824	866	909	951	4.2
1028	993	*035	*078	*120	*162	*204	*247	*289	*331	*373	8.4
1029	012	415	458	500	542	584	626	669	711	753	795
1030	837	879	922	964	*006	*048	*090	*132	*174	*217	12.6
1031	013	259	301	343	385	427	469	511	553	596	638
1032	680	722	764	806	848	890	932	974	*016	*058	21.0
1033	014	100	142	184	226	268	310	352	395	437	479
1034	521	563	605	647	689	730	772	814	856	898	25.2
1035	940	982	*024	*066	*108	*150	*192	*234	*276	*318	33.6
1036	015	360	402	444	485	527	569	611	653	695	737
1037	779	821	863	904	946	988	*030	*072	*114	*156	41
1038	016	197	239	281	323	365	407	448	490	532	574
1039	616	657	699	741	783	824	866	908	950	992	29.4
1040	017	033	075	117	159	200	242	284	326	367	409
1041	451	492	534	576	618	659	701	743	784	826	8.2
1042	868	909	951	993	*034	*076	*118	*159	*201	*243	12.3
1043	018	284	326	368	409	451	492	534	576	617	659
1044	700	742	784	825	867	908	950	992	*033	*075	20.5
1045	019	116	158	199	241	282	324	366	407	449	490
1046	532	573	615	656	698	739	781	822	864	905	32.8
1047	947	988	*030	*071	*113	*154	*195	*237	*278	*320	36.9
1048	020	361	403	444	486	527	568	610	651	693	734
1049	775	817	858	900	941	982	*024	*065	*107	*148	
1050	021	189	231	272	313	355	396	437	479	520	561
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
1050	021 189	231	272	313	355	396	437	479	520	561	
1051	603	644	685	727	768	809	851	892	933	974	
1052	022 016	057	098	140	181	222	263	305	346	387	
1053	428	470	511	552	593	635	676	717	758	799	
1054	841	882	923	964	*005	*047	*088	*129	*170	*211	42
1055	023 252	294	335	376	417	458	499	541	582	623	1 4.2
1056	664	705	746	787	828	870	911	952	993	*034	2 8.4
1057	024 075	116	157	198	239	280	321	363	404	445	3 12.6
1058	486	527	568	609	650	691	732	773	814	855	4 16.8
1059	896	937	978	*019	*060	*101	*142	*183	*224	*265	5 21.0
1060	025 306	347	388	429	470	511	552	593	634	674	6 25.2
1061	715	756	797	838	879	920	961	*002	*043	*084	7 29.4
1062	026 125	165	206	247	288	329	370	411	452	492	8 33.6
1063	533	574	615	656	697	737	778	819	860	901	9 37.8
1064	942	982	*023	*064	*105	*146	*186	*227	*268	*309	
1065	027 350	390	431	472	513	553	594	635	676	716	41
1066	757	798	839	879	920	961	*002	*042	*083	*124	1 4.1
1067	028 164	205	246	287	327	368	409	449	490	531	2 8.2
1068	571	612	653	693	734	775	815	856	896	937	3 12.3
1069	978	*018	*059	*100	*140	*181	*221	*262	*303	*343	4 16.4
1070	029 384	424	465	506	546	587	627	668	708	749	5 20.5
1071	789	830	871	911	952	992	*033	*073	*114	*154	6 24.6
1072	030 195	235	276	316	357	397	438	478	519	559	7 28.7
1073	600	640	681	721	762	802	843	883	923	964	8 32.8
1074	031 004	045	085	126	166	206	247	287	328	368	9 36.9
1075	408	449	489	530	570	610	651	691	732	772	
1076	812	853	893	933	974	*014	*054	*095	*135	*175	
1077	032 216	256	296	337	377	417	458	498	538	578	40
1078	619	659	699	740	780	820	860	901	941	981	1 4.0
1079	033 021	062	102	142	182	223	263	303	343	384	2 8.0
1080	424	464	504	544	585	625	665	705	745	785	3 12.0
1081	826	866	906	946	986	*027	*067	*107	*147	*187	4 16.0
1082	034 227	267	308	348	388	428	468	508	548	588	5 20.0
1083	628	669	709	749	789	829	869	909	949	989	6 24.0
1084	035 029	069	109	149	190	230	270	310	350	390	7 28.0
1085	430	470	510	550	590	630	670	710	750	790	8 32.0
1086	830	870	910	950	990	*030	*070	*110	*150	*190	9 36.0
1087	036 230	269	309	349	389	429	469	509	549	589	
1088	629	669	709	749	789	828	868	908	948	988	
1089	037 028	068	108	148	187	227	267	307	347	387	39
1090	426	466	506	546	586	626	665	705	745	785	1 3.9
1091	825	865	904	944	984	*024	*064	*103	*143	*183	2 7.8
1092	038 223	262	302	342	382	421	461	501	541	580	3 11.7
1093	620	660	700	739	779	819	859	898	938	978	4 15.6
1094	039 017	057	097	136	176	216	255	295	335	374	5 19.5
1095	414	454	493	533	573	612	652	692	731	771	6 23.4
1096	811	850	890	929	969	*009	*048	*088	*127	*167	7 27.3
1097	040 207	246	286	325	365	405	444	484	523	563	8 31.2
1098	602	642	681	721	761	800	840	879	919	958	9 35.1
1099	998	*037	*077	*116	*156	*195	*235	*274	*314	*353	
1100	041 393	432	472	511	551	590	630	669	708	748	
N.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.



## TABLE II.

## CONSTANTS WITH THEIR LOGARITHMS.

			Number.	Logarithm.
Ratio of circumference to diameter, $\pi$ ,			3.14159265	0.49714 99
.. .. .. $\pi^2$ ,			9.86960440	0.99429 97
.. .. .. $2\pi$ ,			6.28318531	0.79817 99
.. .. .. $\sqrt{\pi}$ ,			1.77245385	0.24857 49
Number of degrees in circumference,			360°	2.55630 25
.. minutes ..			21600'	4.33445 38
.. seconds ..			1296000"	6.11260 50
Degrees in arc equal to radius,			57°.2957795	1.75812 26
Minutes .. .. ..			3437'.74677	3.53627 39
Seconds .. .. ..			206264".806	5.31442 51
Length of arc of 1 degree,			.01745329	8.24187 74-10
.. .. 1 minute,			.00029089	6.46372 61-10
.. .. 1 second,			.000004848	4.68557 49-10
Number of hours in 1 day,			24	1.38021 12
.. minutes ..			1440	3.15836 25
.. seconds ..			86400	4.93651 37
Number of days in Julian year,			365.25	2.56259 02
Naperian base,			2.718281828	0.43429 45
Modulus of common logarithms,			0.434294482	9.63778 43-10
Hours in which earth revolves through arc equal to radius,			3.8197186	0.58203 14
Minutes of time .. .. ..			229.18312	2.36018 26
Seconds of time .. .. ..			13750.987	4.13833 39



## TABLE III.



FOR

### SINES AND TANGENTS OF SMALL ANGLES.

#### TO FIND THE SINE OR TANGENT:

$$\text{Log } \sin \alpha = \log \alpha \text{ (in seconds)} + S.$$

$$\text{Log } \tan \alpha = \log \alpha \text{ (in seconds)} + T.$$

#### TO FIND A SMALL ANGLE FROM ITS SINE OR TANGENT:

$$\log \alpha \text{ (in seconds)} = \log \sin \alpha + S'.$$

$$\log \alpha \text{ (in seconds)} = \log \tan \alpha + T'.$$

TABLE III.

0°

<i>ll</i>	<i>l</i>	L. Sin.	S	T	S'	T'
0	0	—	4.68557	4.68557	5.31443	5.31443
60	1	6.46373	.68557	.68557	.31443	.31443
120	2	.76476	.68557	.68557	.31443	.31443
180	3	.94085	.68557	.68557	.31443	.31443
240	4	7.06579	.68557	.68558	.31443	.31442
300	5	7.16270	4.68557	4.68558	5.31443	5.31442
360	6	.24188	.68557	.68558	.31443	.31442
420	7	.39882	.68557	.68558	.31443	.31442
480	8	.36682	.68557	.68558	.31443	.31442
540	9	.41797	.68557	.68558	.31443	.31442
600	10	7.46373	4.68557	4.68558	5.31443	5.31442
660	11	.50512	.68557	.68558	.31443	.31442
720	12	.54291	.68557	.68558	.31443	.31442
780	13	.57767	.68557	.68558	.31443	.31442
840	14	.60985	.68557	.68558	.31443	.31442
900	15	7.63982	4.68557	4.68558	5.31443	5.31442
960	16	.66784	.68557	.68558	.31443	.31442
1020	17	.69417	.68557	.68558	.31443	.31442
1080	18	.71900	.68557	.68558	.31443	.31442
1140	19	.74248	.68557	.68558	.31443	.31442
1200	20	7.76475	4.68557	4.68558	5.31443	5.31442
1260	21	.78594	.68557	.68558	.31443	.31442
1320	22	.80615	.68557	.68558	.31443	.31442
1380	23	.82545	.68557	.68558	.31443	.31442
1440	24	.84393	.68557	.68558	.31443	.31442
1500	25	7.86166	4.68557	4.68558	5.31443	5.31442
1560	26	.87870	.68557	.68558	.31443	.31442
1620	27	.89509	.68557	.68558	.31443	.31442
1680	28	.91088	.68557	.68558	.31443	.31442
1740	29	.92612	.68557	.68559	.31443	.31441
1800	30	7.94084	4.68557	4.68559	5.31443	5.31441
1860	31	.95508	.68557	.68559	.31443	.31441
1920	32	.96887	.68557	.68559	.31443	.31441
1980	33	.98223	.68557	.68559	.31443	.31441
2040	34	.99520	.68557	.68559	.31443	.31441
2100	35	8.00779	4.68557	4.68559	5.31443	5.31441
2160	36	.02002	.68557	.68559	.31443	.31441
2220	37	.03192	.68557	.68559	.31443	.31441
2280	38	.04350	.68557	.68559	.31443	.31441
2340	39	.05478	.68557	.68559	.31443	.31441
2400	40	8.06578	4.68557	4.68559	5.31443	5.31441
2460	41	.07650	.68556	.68560	.31444	.31440
2520	42	.08696	.68556	.68560	.31444	.31440
2580	43	.09718	.68556	.68560	.31444	.31440
2640	44	.10717	.68556	.68560	.31444	.31440
2700	45	8.11693	4.68556	4.68560	5.31444	5.31440
2760	46	.12647	.68556	.68560	.31444	.31440
2820	47	.13581	.68556	.68560	.31444	.31440
2880	48	.14495	.68556	.68560	.31444	.31440
2940	49	.15391	.68556	.68560	.31444	.31440
3000	50	8.16268	4.68556	4.68561	5.31444	5.31439
3060	51	.17128	.68556	.68561	.31444	.31439
3120	52	.17971	.68556	.68561	.31444	.31439
3180	53	.18798	.68556	.68561	.31444	.31439
3240	54	.19610	.68556	.68561	.31444	.31439
3300	55	8.20407	4.68556	4.68561	5.31444	5.31439
3360	56	.21189	.68556	.68561	.31444	.31439
3420	57	.21958	.68555	.68561	.31445	.31439
3480	58	.22713	.68555	.68562	.31445	.31438
3540	59	.23456	.68555	.68562	.31445	.31438
3600	60	8.24186	4.68555	4.68562	5.31445	5.31438

$1^\circ$ 

$''$	'	L. Sin.	S	T	S'	T'
3600	0	8.24186	4.68555	4.68562	5.31445	5.31438
3660	1	.24903	.68555	.68562	.31445	.31438
3720	2	.25609	.68555	.68562	.31445	.31438
3780	3	.26304	.68555	.68562	.31445	.31438
3840	4	.26988	.68555	.68563	.31445	.31437
3900	5	8.27661	4.68555	4.68563	5.31445	5.31437
3960	6	.28324	.68555	.68563	.31445	.31437
4020	7	.28977	.68555	.68563	.31445	.31437
4080	8	.29621	.68555	.68563	.31445	.31437
4140	9	.30255	.68555	.68563	.31445	.31437
4200	10	8.30879	4.68554	4.68563	5.31446	5.31437
4260	11	.31495	.68554	.68564	.31446	.31436
4320	12	.32103	.68554	.68564	.31446	.31436
4380	13	.32702	.68554	.68564	.31446	.31436
4440	14	.33292	.68554	.68564	.31446	.31436
4500	15	8.33875	4.68554	4.68564	5.31446	5.31436
4560	16	.34450	.68554	.68565	.31446	.31435
4620	17	.35018	.68554	.68565	.31446	.31435
4680	18	.35578	.68554	.68565	.31446	.31435
4740	19	.36131	.68554	.68565	.31446	.31435
4800	20	8.36678	4.68554	4.68565	5.31446	5.31435
4860	21	.37217	.68553	.68566	.31447	.31434
4920	22	.37750	.68553	.68566	.31447	.31434
4980	23	.38276	.68553	.68566	.31447	.31434
5040	24	.38796	.68553	.68566	.31447	.31434
5100	25	8.39310	4.68553	4.68566	5.31447	5.31434
5160	26	.39818	.68553	.68567	.31447	.31433
5220	27	.40320	.68553	.68567	.31447	.31433
5280	28	.40816	.68553	.68567	.31447	.31433
5340	29	.41307	.68553	.68567	.31447	.31433
5400	30	8.41792	4.68553	4.68567	5.31447	5.31433
5460	31	.42272	.68552	.68568	.31448	.31432
5520	32	.42746	.68552	.68568	.31448	.31432
5580	33	.43216	.68552	.68568	.31448	.31432
5640	34	.43680	.68552	.68568	.31448	.31432
5700	35	8.44139	4.68552	4.68569	5.31448	5.31431
5760	36	.44594	.68552	.68569	.31448	.31431
5820	37	.45044	.68552	.68569	.31448	.31431
5880	38	.45489	.68552	.68569	.31448	.31431
5940	39	.45930	.68551	.68569	.31449	.31431
6000	40	8.46366	4.68551	4.68570	5.31449	5.31430
6060	41	.46799	.68551	.68570	.31449	.31430
6120	42	.47226	.68551	.68570	.31449	.31430
6180	43	.47650	.68551	.68570	.31449	.31430
6240	44	.48069	.68551	.68571	.31449	.31429
6300	45	8.48485	4.68551	4.68571	5.31449	5.31429
6360	46	.48896	.68551	.68571	.31449	.31429
6420	47	.49304	.68550	.68572	.31450	.31428
6480	48	.49708	.68550	.68572	.31450	.31428
6540	49	.50108	.68550	.68572	.31450	.31428
6600	50	8.50504	4.68550	4.68572	5.31450	5.31428
6660	51	.50897	.68550	.68573	.31450	.31427
6720	52	.51287	.68550	.68573	.31450	.31427
6780	53	.51673	.68550	.68573	.31450	.31427
6840	54	.52055	.68550	.68573	.31450	.31427
6900	55	8.52434	4.68549	4.68574	5.31451	5.31426
6960	56	.52810	.68549	.68574	.31451	.31426
7020	57	.53183	.68549	.68574	.31451	.31426
7080	58	.53552	.68549	.68575	.31451	.31425
7140	59	.53919	.68549	.68575	.31451	.31425
7200	60	8.54282	4.68549	4.68575	5.31451	5.31425



## TABLE IV.



## LOGARITHMS

OF THE

SINE, COSINE, TANGENT AND COTANGENT

FOR

EACH MINUTE OF THE QUADRANT.

TABLE IV.

0°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.		Prop. Pts.
0	—	—	—	—	0.00 000	60		
1	6.46 373	30103	6.46 373	30103	3.53 627	59	3476	3218 2997
2	6.76 476	17609	6.76 476	17609	3.23 524	58	.1 348	322 300
3	6.94 085	12494	6.94 085	12494	3.05 915	57	.2 695	644 599
4	7.06 579	9691	7.06 579	9691	2.93 421	56	.3 1043	965 899
5	7.16 270	7918	7.16 270	7918	2.83 730	55	.4 1390	1287 1199
6	7.24 188	6694	7.24 188	6694	2.75 812	54	.5 1738	1609 1498
7	7.30 882	5800	7.30 882	5800	2.69 118	53		
8	7.36 682	5115	7.36 682	5115	2.63 318	52	2862	2633 2483
9	7.41 797	4576	7.41 797	4576	2.58 203	51	.1 280	263 248
10	7.46 373	4139	7.46 373	4139	2.53 627	50	.2 560	527 497
11	7.50 512	3779	7.50 512	3779	2.49 488	49	.3 841	790 745
12	7.54 291	3476	7.54 291	3476	2.45 709	48	.4 1221	1053 993
13	7.57 767	3218	7.57 767	3218	2.42 233	47	.5 1401	1316 1242
14	7.60 985	2997	7.60 985	2996	2.39 014	46		
15	7.63 982	2802	7.63 982	2803	2.36 018	45	.1 2227	2021 1848
16	7.66 784	2633	7.66 785	2633	2.33 215	44	.2 223	202 185
17	7.69 417	2483	7.69 418	2482	2.30 582	43	.3 445	404 370
18	7.71 900	2348	7.71 900	2348	2.28 100	42	.4 668	606 554
19	7.74 248	2227	7.74 248	2228	2.25 752	41	.5 891	808 739
20	7.76 475	2119	7.76 476	2119	2.23 524	40	.1 1113	1010 924
21	7.78 594	2021	7.78 595	2020	2.21 405	39	1704	1579 1478
22	7.80 615	1930	7.80 615	1931	2.19 385	38	.1 170	158 147
23	7.82 545	1848	7.82 546	1848	2.17 454	37	.2 341	316 294
24	7.84 393	1773	7.84 394	1773	2.15 606	36	.3 511	474 442
25	7.86 166	1704	7.86 167	1704	2.13 833	35	.4 682	632 589
26	7.87 870	1639	7.87 871	1639	2.12 129	34	.5 852	829 736
27	7.89 509	1579	7.89 510	1579	2.10 490	33		
28	7.91 088	1524	7.91 089	1524	2.08 911	32	1379	1297 1223
29	7.92 612	1472	7.92 613	1473	2.07 387	31	.1 138	130 128
30	7.94 084	1424	7.94 086	1424	2.05 914	30	.2 276	259 245
31	7.95 508	1379	7.95 510	1379	2.04 490	29	.3 414	389 367
32	7.96 887	1336	7.96 889	1336	2.03 111	28	.4 552	519 489
33	7.98 223	1297	7.98 225	1297	2.01 775	27	.5 690	649 612
34	7.99 520	1259	7.99 522	1259	2.00 478	26		
35	8.00 779	1223	8.00 781	1223	1.99 219	25	1158	1100 1046
36	8.02 002	1190	8.02 004	1190	1.97 996	24	.1 116	110 105
37	8.03 192	1158	8.03 194	1159	1.96 806	23	.2 232	220 209
38	8.04 350	1128	8.04 353	1128	1.95 647	22	.3 347	330 314
39	8.05 478	1100	8.05 481	1100	1.94 519	21	.4 463	440 418
40	8.06 578	1072	8.06 581	1072	1.93 419	20	.5 579	550 523
41	8.07 650	1046	8.07 653	1047	1.92 347	19	999	954 914
42	8.08 696	1022	8.08 700	1022	1.91 300	18	.1 100	95 91
43	8.09 718	999	8.10 720	998	1.90 278	17	.2 200	191 183
44	8.10 717	976		976	1.89 280	16	.3 300	286 274
45	8.11 693	954	8.11 696	955	1.88 304	15	.4 400	382 366
46	8.12 647	934	8.12 651	934	1.87 349	14	.5 500	477 457
47	8.13 581	914	8.13 585	915	1.86 415	13		
48	8.14 495	896	8.14 500	895	1.85 500	12	877	843 812
49	8.15 391	877	8.15 395	878	1.84 605	11	.1 88	84 81
50	8.16 268	860	8.16 273	860	1.83 727	10	.2 175	169 162
51	8.17 128	843	8.17 133	843	1.82 867	9	.3 263	253 244
52	8.17 971	827	8.17 976	828	1.82 024	8	.4 351	337 325
53	8.18 798	812	8.18 804	812	1.81 196	7	.5 438	422 406
54	8.19 610	797	8.19 616	797	1.80 384	6		
55	8.20 497	782	8.20 413	782	1.79 587	5	782	755 730
56	8.21 189	769	8.21 195	769	1.78 805	4	.1 78	75 73
57	8.21 958	755	8.21 964	756	1.78 036	3	.2 156	151 146
58	8.22 713	743	8.23 462	742	1.77 280	2	.3 235	226 219
59	8.23 456	730	8.24 192	730	1.76 538	1	.4 313	302 292
60	8.24 186				1.75 808	0	.5 301	377 365
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.		Prop. Pts.

1°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.		Prop. Pts.		
0	8.24 186		8.24 192		1.75 808	9.99 993	60			
1	8.24 903	717	8.24 91C		1.75 090	9.99 993	59	.1	717	695
2	8.25 609	706	8.25 616		1.74 384	9.99 993	58	.2	717	69.5
3	8.26 304	695	8.26 312		1.73 688	9.99 993	57	.3	143.4	139.0
4	8.26 988	684	8.26 996		1.73 004	9.99 992	56	.4	215.1	208.5
5	8.27 661	673	8.27 669		1.72 331	9.99 992	55	.5	286.8	278.2
6	8.28 324	663	8.28 332		1.71 668	9.99 992	54		358.5	347.5
7	8.28 977	653	8.28 986		1.71 014	9.99 992	53			336.5
8	8.29 621	644	8.29 629		1.70 371	9.99 992	52		653	634
9	8.30 255	634	8.30 263		1.69 737	9.99 991	51	.1	65.3	63.4
10	8.30 879	616	8.30 888		1.69 112	9.99 991	50	.2	130.6	126.8
11	8.31 495	608	8.31 505		1.68 495	9.99 991	49	.3	195.9	190.2
12	8.32 103	599	8.32 112		1.67 888	9.99 990	48	.4	261.2	253.6
13	8.32 702	599	8.32 711		1.67 289	9.99 990	47	.5	326.5	317.0
14	8.33 292	583	8.33 302		1.66 698	9.99 990	46			308.0
15	8.33 875		8.33 886		1.66 114	9.99 990	45		599	583
16	8.34 450	575	8.34 461		1.65 539	9.99 989	44	.1	59.9	58.3
17	8.35 018	568	8.35 029		1.64 971	9.99 989	43	.2	119.8	116.6
18	8.35 578	560	8.35 590		1.64 410	9.99 989	42	.3	179.7	174.9
19	8.36 131	553	8.36 143		1.63 857	9.99 989	41	.4	239.6	232.2
20	8.36 678		8.36 689		1.63 311	9.99 988	40	.5	299.5	291.5
21	8.37 217	539	8.37 229		1.62 771	9.99 988	39		553	539
22	8.37 750	533	8.37 762		1.62 238	9.99 988	38	.1	55.3	53.9
23	8.38 276	526	8.38 289		1.61 711	9.99 987	37	.2	110.6	107.8
24	8.38 796	520	8.38 809		1.61 191	9.99 987	36	.3	165.9	161.7
25	8.39 310	514	8.39 323		1.60 677	9.99 987	35	.4	221.2	215.6
26	8.39 818	508	8.39 832		1.60 168	9.99 986	34	.5	276.5	269.5
27	8.40 320	502	8.40 334		1.59 666	9.99 986	33			263.0
28	8.40 816	496	8.40 830		1.59 170	9.99 986	32		514	502
29	8.41 307	491	8.41 321		1.58 679	9.99 985	31	.1	51.4	50.2
30	8.41 792	480	8.41 807		1.58 193	9.99 985	30	.2	102.8	100.4
31	8.42 272	480	8.42 287		1.57 713	9.99 985	29	.3	154.2	150.6
32	8.42 746	474	8.42 762		1.57 238	9.99 984	28	.4	205.6	200.8
33	8.43 213	470	8.43 232		1.56 768	9.99 984	27	.5	257.0	251.0
34	8.43 680	464	8.43 696		1.56 304	9.99 984	26		480	470
35	8.44 139	459	8.44 156		1.55 844	9.99 983	25			460
36	8.44 594	455	8.44 611		1.55 389	9.99 983	24	.1	48	47
37	8.45 044	450	8.45 061		1.54 939	9.99 983	23	.2	96	94
38	8.45 489	445	8.45 507		1.54 493	9.99 982	22	.3	144	143
39	8.45 930	441	8.45 948		1.54 052	9.99 982	21	.4	192	188
40	8.46 366	436	8.46 385		1.53 615	9.99 982	20	.5	240	235
41	8.46 799	433	8.46 817		1.53 183	9.99 981	19			230
42	8.47 226	427	8.47 245		1.52 755	9.99 981	18	.1	450	440
43	8.47 650	424	8.47 669		1.52 331	9.99 981	17	.2	45	44
44	8.48 069	419	8.48 089		1.51 911	9.99 980	16	.3	90	88
45	8.48 482	416	8.48 505		1.51 495	9.99 980	15	.4	135	132
46	8.48 896	411	8.48 917		1.51 083	9.99 979	14	.5	180	176
47	8.49 304	408	8.49 325		1.50 675	9.99 979	13		225	220
48	8.49 708	404	8.49 729		1.50 271	9.99 979	12		420	410
49	8.50 105	400	8.50 130		1.49 870	9.99 978	11	.1	42	41
50	8.50 504	396	8.50 527		1.49 473	9.99 978	10	.2	84	82
51	8.50 897	393	8.50 920		1.49 080	9.99 977	9	.3	126	123
52	8.51 287	390	8.51 310		1.48 690	9.99 977	8	.4	168	164
53	8.51 673	386	8.51 696		1.48 304	9.99 977	7	.5	210	205
54	8.52 055	382	8.52 079		1.47 921	9.99 976	6			200
55	8.52 434	379	8.52 459		1.47 541	9.99 976	5		390	380
56	8.52 810	376	8.52 835		1.47 165	9.99 975	4	.1	39	38
57	8.53 183	373	8.53 208		1.46 792	9.99 975	3	.2	78	76
58	8.53 552	369	8.53 578		1.46 422	9.99 974	2	.3	117	114
59	8.53 919	367	8.53 945		1.46 055	9.99 974	1	.4	156	152
60	8.54 282	363	8.54 308		1.45 692	9.99 974	0	.5	195	190
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	/	Prop. Pts.		

TABLE IV.

2°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.		Prop. Pts.
0	8.54 282	360	8.54 308	361	1.45 692	9.99 974	60	
1	8.54 642	357	8.54 669	358	1.45 531	9.99 973	59	360 350 340
2	8.54 999	355	8.55 027	355	1.44 973	9.99 973	58	.1 .2 .3 .4 .5 .6 .7 .8 .9
3	8.55 354	351	8.55 382	352	1.44 618	9.99 972	57	144 140 136 130 125 120 115 110 105
4	8.55 705	349	8.55 734	349	1.44 266	9.99 972	56	108 105 102 100 98 96 94 92 90
5	8.56 054	346	8.56 083	346	1.43 917	9.99 971	55	144 140 136 130 125 120 115 110 105
6	8.56 400	343	8.56 429	344	1.43 571	9.99 971	54	180 175 170 165 160 155 150 145 140
7	8.56 743	341	8.56 773	341	1.43 227	9.99 970	53	216 210 204 198 192 186 180 174 170
8	8.57 084	337	8.57 114	338	1.42 886	9.99 970	52	252 245 238 230 225 218 210 204 200
9	8.57 421	336	8.57 452	336	1.42 548	9.99 969	51	288 280 272 265 258 250 244 238 230
10	8.57 757	332	8.57 788	333	1.42 212	9.99 969	50	324 315 306 300 290 280 272 265 258
11	8.58 089	330	8.58 121	331	1.41 879	9.99 968	49	330 320 310 300 290 280 272 265 258
12	8.58 419	328	8.58 451	329	1.41 549	9.99 968	48	.1 .2 .3 .4 .5 .6 .7 .8 .9
13	8.58 747	325	8.58 779	326	1.41 221	9.99 967	47	132 128 124 120 116 112 108 104 100
14	8.59 072	323	8.59 105	323	1.40 895	9.99 967	46	139 135 131 128 124 120 116 112 108
15	8.59 395	320	8.59 428	321	1.40 572	9.99 967	45	165 160 155 150 145 140 136 130 125
16	8.59 715	318	8.59 749	319	1.40 251	9.99 966	44	198 192 186 180 174 168 162 156 150
17	8.60 033	316	8.60 068	317	1.39 932	9.99 966	43	231 224 217 210 203 196 188 180 174
18	8.60 349	313	8.60 384	314	1.39 616	9.99 965	42	264 256 248 240 232 224 216 208 200
19	8.60 662	311	8.60 698	311	1.39 302	9.99 964	41	297 288 275 270 262 254 246 238 230
20	8.60 973	309	8.61 009	310	1.38 991	9.99 964	40	
21	8.61 282	307	8.61 319	307	1.38 681	9.99 963	39	300 290 285 280 270 265 258 250 245
22	8.61 589	305	8.61 626	305	1.38 374	9.99 963	38	.1 .2 .3 .4 .5 .6 .7 .8 .9
23	8.61 894	303	8.61 931	303	1.38 069	9.99 962	37	120 116 112 108 104 100 96 92 88
24	8.62 196	301	8.62 234	301	1.37 766	9.99 962	36	150 145 140 136 130 126 122 118 114
25	8.62 497	298	8.62 535	299	1.37 465	9.99 961	35	180 175 170 165 160 155 150 145 140
26	8.62 793	296	8.62 834	297	1.37 166	9.99 961	34	210 203 195 190 185 178 172 168 162
27	8.63 091	294	8.63 131	295	1.36 869	9.99 960	33	240 232 224 218 210 203 195 188 180
28	8.63 385	293	8.63 426	295	1.36 574	9.99 960	32	270 262 254 246 238 230 222 214 206
29	8.63 678	290	8.63 718	291	1.36 282	9.99 959	31	300 290 285 280 270 262 254 246 238
30	8.63 968	288	8.64 009	289	1.35 991	9.99 959	30	
31	8.64 256	287	8.64 298	287	1.35 702	9.99 958	29	320 290 275 270 265 258 250 245 238
32	8.64 543	284	8.64 585	285	1.35 415	9.99 958	28	.1 .2 .3 .4 .5 .6 .7 .8 .9
33	8.64 827	283	8.64 870	284	1.35 130	9.99 957	27	150 145 140 136 130 126 122 118 114
34	8.65 110	281	8.65 154	281	1.34 846	9.99 956	26	180 175 170 165 160 155 150 145 140
35	8.65 391	279	8.65 435	280	1.34 565	9.99 956	25	210 203 195 190 185 178 172 168 162
36	8.65 670	277	8.65 715	278	1.34 285	9.99 955	24	240 232 224 218 210 203 195 188 180
37	8.65 947	276	8.65 993	276	1.34 007	9.99 955	23	270 262 254 246 238 230 222 214 206
38	8.66 223	274	8.66 269	274	1.33 731	9.99 954	22	300 290 285 280 270 262 254 246 238
39	8.66 497	272	8.66 543	273	1.33 457	9.99 954	21	
40	8.66 769	270	8.66 816	271	1.33 184	9.99 953	20	320 290 275 270 265 258 250 245 238
41	8.67 039	269	8.67 087	269	1.32 913	9.99 952	19	.1 .2 .3 .4 .5 .6 .7 .8 .9
42	8.67 308	267	8.67 356	268	1.32 644	9.99 952	18	150 145 140 136 130 126 122 118 114
43	8.67 575	266	8.67 624	266	1.32 379	9.99 951	17	180 175 170 165 160 155 150 145 140
44	8.67 841	263	8.67 890	266	1.32 110	9.99 951	16	210 203 195 190 185 178 172 168 162
45	8.68 104	263	8.68 154	264	1.31 846	9.99 950	15	240 232 224 218 210 203 195 188 180
46	8.68 367	260	8.68 417	263	1.31 583	9.99 949	14	270 262 254 246 238 230 222 214 206
47	8.68 627	260	8.68 678	261	1.31 322	9.99 949	13	300 290 285 280 270 262 254 246 238
48	8.68 886	259	8.68 938	258	1.31 062	9.99 948	12	
49	8.69 144	258	8.69 196	258	1.30 804	9.99 948	11	330 320 310 300 290 280 270 260 250
50	8.69 400	256	8.69 453	257	1.30 547	9.99 947	10	
51	8.69 654	254	8.69 708	255	1.30 292	9.99 946	9	350 340 330 320 310 300 290 280 270
52	8.69 907	253	8.69 962	254	1.30 038	9.99 946	8	.1 .2 .3 .4 .5 .6 .7 .8 .9
53	8.70 159	252	8.70 214	252	1.29 786	9.99 945	7	380 370 360 350 340 330 320 310 300
54	8.70 409	249	8.70 465	251	1.29 535	9.99 944	6	.1 .2 .3 .4 .5 .6 .7 .8 .9
55	8.70 658	249	8.70 714	249	1.29 286	9.99 944	5	410 400 390 380 370 360 350 340 330
56	8.70 905	247	8.70 962	248	1.29 038	9.99 943	4	.1 .2 .3 .4 .5 .6 .7 .8 .9
57	8.71 151	246	8.71 208	246	1.28 792	9.99 942	3	440 430 420 410 400 390 380 370 360
58	8.71 395	244	8.71 453	245	1.28 547	9.99 942	2	.1 .2 .3 .4 .5 .6 .7 .8 .9
59	8.71 638	243	8.71 697	244	1.28 303	9.99 941	1	470 460 450 440 430 420 410 400 390
60	8.71 880	242	8.71 940	243	1.28 060	9.99 940	0	.1 .2 .3 .4 .5 .6 .7 .8 .9
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	/	Prop. Pts.

3°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.		Prop. Pts.
<b>0</b>	8.71 880	240	8.71 940	241	1.28 060	9.99 940	<b>60</b>	
<b>1</b>	8.72 120	239	8.72 181	239	1.27 819	9.99 940	59	238 234 229
<b>2</b>	8.72 359	238	8.72 420	239	1.27 580	9.99 939	58	23.8 23.4 22.9
<b>3</b>	8.72 597	237	8.72 659	237	1.27 341	9.99 938	57	.1 .2 .3
<b>4</b>	8.72 834	235	8.72 896	236	1.27 104	9.99 938	56	47.6 46.8 45.8
<b>5</b>	8.73 069	234	8.73 132	234	1.26 868	9.99 937	55	.4 .5 .6
<b>6</b>	8.73 303	232	8.73 366	234	1.26 634	9.99 936	54	119.0 117.0 114.5
<b>7</b>	8.73 535	232	8.73 600	234	1.26 400	9.99 936	53	142.8 140.4 137.4
<b>8</b>	8.73 767	230	8.73 832	232	1.26 168	9.99 935	52	166.6 163.8 160.3
<b>9</b>	8.73 997	229	8.74 063	229	1.25 937	9.99 934	51	190.4 187.2 183.2
<b>10</b>	8.74 226	228	8.74 292	229	1.25 708	9.99 934	<b>50</b>	214.2 210.6 206.1
<b>11</b>	8.74 454	226	8.74 521	227	1.25 479	9.99 933	49	
<b>12</b>	8.74 680	226	8.74 748	226	1.25 252	9.99 932	48	.1 .2 .3
<b>13</b>	8.74 906	224	8.74 974	225	1.25 026	9.99 932	47	45.0 44.0 43.2
<b>14</b>	8.75 130	223	8.75 199	224	1.24 801	9.99 931	46	.3 .4 .5
<b>15</b>	8.75 353	222	8.75 423	222	1.24 577	9.99 930	45	67.5 66.0 64.8
<b>16</b>	8.75 575	220	8.75 645	222	1.24 355	9.99 929	44	90.0 88.0 86.4
<b>17</b>	8.75 795	220	8.75 867	220	1.24 133	9.99 929	43	112.5 110.0 108.0
<b>18</b>	8.76 015	219	8.76 087	219	1.23 913	9.99 928	42	.6 .7 .8
<b>19</b>	8.76 234	217	8.76 306	219	1.23 694	9.99 927	41	157.5 154.0 151.2
<b>20</b>	8.76 451	216	8.76 525	217	1.23 475	9.99 926	<b>40</b>	.9 .10 .11
<b>21</b>	8.76 667	216	8.76 742	216	1.23 258	9.99 926	39	
<b>22</b>	8.76 883	216	8.76 958	215	1.23 042	9.99 925	38	.1 .2 .3
<b>23</b>	8.77 097	214	8.77 173	215	1.22 827	9.99 924	37	42.4 41.6 40.8
<b>24</b>	8.77 310	212	8.77 387	214	1.22 613	9.99 923	36	.6 .7 .8
<b>25</b>	8.77 522	211	8.77 600	211	1.22 400	9.99 923	35	.4 .5 .6
<b>26</b>	8.77 733	210	8.77 811	211	1.22 189	9.99 922	34	84.8 83.2 81.6
<b>27</b>	8.77 943	210	8.78 022	211	1.21 978	9.99 921	33	.5 .6 .7
<b>28</b>	8.78 152	209	8.78 232	210	1.21 768	9.99 920	32	127.2 124.8 122.4
<b>29</b>	8.78 360	208	8.78 441	209	1.21 559	9.99 920	31	.8 .9 .10
<b>30</b>	8.78 568	206	8.78 649	206	1.21 351	9.99 919	<b>30</b>	
<b>31</b>	8.78 774	205	8.78 855	205	1.21 145	9.99 918	29	
<b>32</b>	8.78 979	204	8.79 061	205	1.20 939	9.99 917	28	.1 .2 .3
<b>33</b>	8.79 183	203	8.79 266	204	1.20 734	9.99 917	27	40.2 39.4 38.6
<b>34</b>	8.79 386	202	8.79 470	203	1.20 530	9.99 916	26	.6 .7 .8
<b>35</b>	8.79 588	201	8.79 673	202	1.20 327	9.99 915	25	.4 .5 .6
<b>36</b>	8.79 789	201	8.79 875	202	1.20 200	9.99 914	24	100.5 98.5 96.5
<b>37</b>	8.79 990	199	8.80 076	201	1.19 924	9.99 913	23	.6 .7 .8
<b>38</b>	8.80 189	199	8.80 277	201	1.19 723	9.99 913	22	120.6 118.2 115.8
<b>39</b>	8.80 388	199	8.80 476	199	1.19 524	9.99 912	21	.8 .9 .10
<b>40</b>	8.80 585	197	8.80 674	198	1.19 326	9.99 911	<b>20</b>	
<b>41</b>	8.80 782	197	8.80 872	198	1.19 128	9.99 910	19	
<b>42</b>	8.80 978	196	8.81 068	196	1.18 932	9.99 909	18	.1 .2 .3
<b>43</b>	8.81 173	195	8.81 264	196	1.18 730	9.99 909	17	37.8 37.0 36.2
<b>44</b>	8.81 307	194	8.81 459	195	1.18 541	9.99 908	16	.5 .6 .7
<b>45</b>	8.81 560	193	8.81 653	194	1.18 347	9.99 907	15	.4 .5 .6
<b>46</b>	8.81 752	192	8.81 846	193	1.18 154	9.99 906	14	94.5 92.5 90.5
<b>47</b>	8.81 944	192	8.82 038	192	1.17 962	9.99 905	13	.6 .7 .8
<b>48</b>	8.82 134	190	8.82 230	192	1.17 770	9.99 904	12	113.4 111.0 108.6
<b>49</b>	8.82 324	190	8.82 420	190	1.17 580	9.99 904	11	.8 .9 .10
<b>50</b>	8.82 513	188	8.82 610	189	1.17 390	9.99 903	<b>10</b>	
<b>51</b>	8.82 701	188	8.82 799	188	1.17 201	9.99 902	9	
<b>52</b>	8.82 888	187	8.82 987	188	1.17 013	9.99 901	8	.1 .2 .3
<b>53</b>	8.83 075	187	8.83 175	188	1.16 825	9.99 900	7	0.4 0.3 0.2
<b>54</b>	8.83 261	186	8.83 361	186	1.16 639	9.99 899	6	.8 .9 .10
<b>55</b>	8.83 446	185	8.83 547	186	1.16 453	9.99 898	5	.4 .5 .6
<b>56</b>	8.83 630	184	8.83 732	185	1.16 268	9.99 898	4	2.0 1.5 1.0
<b>57</b>	8.83 813	183	8.83 916	184	1.16 084	9.99 897	3	.6 .7 .8
<b>58</b>	8.83 996	183	8.84 100	184	1.15 900	9.99 896	2	2.4 2.1 1.4
<b>59</b>	8.84 177	181	8.84 282	182	1.15 718	9.99 895	1	.8 .9 .10
<b>60</b>	8.84 358	181	8.84 464	182	1.15 536	9.99 894	<b>0</b>	.3 .4 .5
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	/	Prop. Pts.

86°

TABLE IV.

4°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	60	Prop. Pts.
	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	60	Prop. Pts.
0	8.84 358	181	8.84 464	182	1.15 536	9.99 894	60	
1	8.84 539	179	8.84 646	180	1.15 554	9.99 893	59	
2	8.84 718	179	8.84 826	180	1.15 892	9.99 892	58	.1 181 179 177
3	8.84 897	178	8.85 006	179	1.14 904	9.99 891	57	.2 181 179 177
4	8.85 075	177	8.85 185	178	1.14 815	9.99 891	56	.3 181 179 177
5	8.85 252	177	8.85 363	177	1.14 637	9.99 890	55	.4 181 179 177
6	8.85 429	176	8.85 540	177	1.14 460	9.99 889	54	.5 181 179 177
7	8.85 605	175	8.85 717	176	1.14 283	9.99 888	53	.6 181 179 177
8	8.85 780	175	8.85 893	176	1.14 107	9.99 887	52	.7 181 179 177
9	8.85 955	175	8.86 069	174	1.13 931	9.99 886	51	.8 181 179 177
10	8.86 128	173	8.86 243	174	1.13 757	9.99 885	50	.9 181 179 177
11	8.86 301	173	8.86 417	174	1.13 583	9.99 884	49	
12	8.86 474	173	8.86 591	174	1.13 409	9.99 883	48	.1 175 173 171
13	8.86 645	171	8.86 763	172	1.13 237	9.99 882	47	.2 175 173 171
14	8.86 816	171	8.86 935	171	1.13 065	9.99 881	46	.3 175 173 171
15	8.86 987	169	8.87 106	171	1.12 894	9.99 880	45	.4 175 173 171
16	8.87 156	169	8.87 277	171	1.12 723	9.99 879	44	.5 175 173 171
17	8.87 325	169	8.87 447	169	1.12 553	9.99 879	43	.6 175 173 171
18	8.87 494	167	8.87 616	169	1.12 384	9.99 878	42	.7 175 173 171
19	8.87 661	168	8.87 785	168	1.12 215	9.99 877	41	.8 175 173 171
20	8.87 829	166	8.87 953	167	1.12 047	9.99 876	40	.9 175 173 171
21	8.87 995	166	8.88 120	167	1.11 880	9.99 875	39	
22	8.88 161	166	8.88 287	166	1.11 713	9.99 874	38	.1 168 166 164
23	8.88 326	165	8.88 453	165	1.11 547	9.99 873	37	.2 168 166 164
24	8.88 490	164	8.88 618	165	1.11 382	9.99 872	36	.3 168 166 164
25	8.88 654	163	8.88 783	165	1.11 217	9.99 871	35	.4 168 166 164
26	8.88 817	163	8.88 948	165	1.11 052	9.99 870	34	.5 168 166 164
27	8.88 980	163	8.89 111	163	1.10 889	9.99 869	33	.6 168 166 164
28	8.89 142	162	8.89 274	163	1.10 726	9.99 868	32	.7 168 166 164
29	8.89 304	162	8.89 437	163	1.10 563	9.99 867	31	.8 168 166 164
30	8.89 464	160	8.89 598	161	1.10 402	9.99 866	30	.9 168 166 164
31	8.89 625	161	8.89 760	162	1.10 240	9.99 865		
32	8.89 784	159	8.89 920	160	1.10 080	9.99 864	29	
33	8.89 943	159	8.90 080	160	1.09 920	9.99 863	28	.1 162 159 157
34	8.90 102	158	8.90 240	159	1.09 760	9.99 862	27	.2 162 159 157
35	8.90 260	158	8.90 399	159	1.09 601	9.99 861	26	.3 162 159 157
36	8.90 417	157	8.90 557	158	1.09 443	9.99 860	25	.4 162 159 157
37	8.90 574	157	8.90 715	158	1.09 285	9.99 859	24	.5 162 159 157
38	8.90 730	156	8.90 872	157	1.09 128	9.99 858	23	.6 162 159 157
39	8.90 885	155	8.91 029	157	1.08 971	9.99 857	22	.7 162 159 157
40	8.91 040	155	8.91 185	156	1.08 815	9.99 856	20	.8 162 159 157
41	8.91 195	155	8.91 340	155	1.08 660	9.99 855		
42	8.91 349	154	8.91 495	155	1.08 505	9.99 854	19	
43	8.91 502	153	8.91 650	155	1.08 350	9.99 853	18	.1 155 153 151
44	8.91 655	152	8.91 803	153	1.08 197	9.99 852	17	.2 155 153 151
45	8.91 807	152	8.91 957	154	1.08 043	9.99 851	16	.3 155 153 151
46	8.91 959	152	8.92 110	152	1.07 890	9.99 850	15	.4 155 153 151
47	8.92 110	151	8.92 262	152	1.07 738	9.99 848	14	.5 155 153 151
48	8.92 261	151	8.92 414	152	1.07 586	9.99 847	13	.6 155 153 151
49	8.92 411	150	8.92 565	151	1.07 435	9.99 846	12	.7 155 153 151
50	8.92 561	149	8.92 716	151	1.07 284	9.99 845	10	.8 155 153 151
51	8.92 710	149	8.92 866	150	1.07 134	9.99 844		
52	8.92 859	149	8.93 016	150	1.06 984	9.99 843	9	
53	8.93 007	148	8.93 165	149	1.06 835	9.99 842	8	.1 149 147 145
54	8.93 154	147	8.93 313	149	1.06 687	9.99 841	7	.2 149 147 145
55	8.93 301	147	8.93 462	149	1.06 538	9.99 840	6	.3 149 147 145
56	8.93 448	147	8.93 609	147	1.06 391	9.99 839	5	.4 149 147 145
57	8.93 594	146	8.93 756	147	1.06 244	9.99 838		
58	8.93 740	146	8.93 903	147	1.06 097	9.99 837	4	.5 149 147 145
59	8.93 885	145	8.94 049	146	1.05 951	9.99 836	3	.6 149 147 145
60	8.94 030	145	8.94 195	146	1.05 805	9.99 834	0	.7 149 147 145
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	/	Prop. Pts.

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.		Prop. Pts.		
0	8.94 030		8.94 195		1.05 805	9.99 834	60			
1	8.94 174	144	8.94 340		1.05 660	9.99 833	59	.1	145	143
2	8.94 317	143	8.94 485		1.05 515	9.99 832	58	.2	14.5	14.3
3	8.94 461	144	8.94 630		1.05 370	9.99 831	57	.3	29.0	28.6
4	8.94 603	142	8.94 773		1.05 227	9.99 830	56	.4	43.5	42.9
5	8.94 746	143	8.94 917		1.05 083	9.99 829	55	.5	58.0	57.2
6	8.94 887	141	8.95 060		1.04 940	9.99 828	54	.6	72.5	71.5
7	8.95 029	142	8.95 202		1.04 798	9.99 827	53	.7	87.0	85.8
8	8.95 170	140	8.95 344		1.04 656	9.99 825	52	.8	101.5	100.1
9	8.95 310	140	8.95 486		1.04 514	9.99 824	51	.9	116.0	114.4
10	8.95 450		8.95 627		1.04 373	9.99 823	50	.9	130.5	128.7
11	8.95 589	139	8.95 767		1.04 233	9.99 822	49		139	138
12	8.95 728	139	8.95 908		1.04 092	9.99 821	48	.1	13.9	13.8
13	8.95 867	139	8.96 047		1.03 953	9.99 820	47	.2	27.8	27.6
14	8.96 005	138	8.96 187		1.03 813	9.99 819	46	.3	41.7	41.4
15	8.96 143		8.96 325		1.03 675	9.99 817	45	.4	55.6	55.2
16	8.96 280	137	8.96 464		1.03 536	9.99 816	44	.5	69.5	69.0
17	8.96 417	137	8.96 602		1.03 398	9.99 815	43	.6	83.4	82.8
18	8.96 553	136	8.96 739		1.03 261	9.99 814	42	.7	97.3	96.6
19	8.96 689	136	8.96 877		1.03 123	9.99 813	41	.8	111.2	110.4
20	8.96 825		8.97 013		1.02 987	9.99 812	40	.9	125.1	124.2
21	8.96 960	135	8.97 150		1.02 850	9.99 810	39		135	133
22	8.97 095	135	8.97 285		1.02 715	9.99 809	38	.1	13.5	13.3
23	8.97 229	134	8.97 421		1.02 579	9.99 808	37	.2	27.0	26.6
24	8.97 363	134	8.97 556		1.02 444	9.99 807	36	.3	40.5	39.9
25	8.97 496	133	8.97 691		1.02 309	9.99 806	35	.4	54.0	53.2
26	8.97 629	133	8.97 825		1.02 175	9.99 804	34	.5	67.5	66.5
27	8.97 762	133	8.97 959		1.02 041	9.99 803	33	.6	81.0	79.8
28	8.97 894	132	8.98 092		1.01 908	9.99 802	32	.7	94.5	93.1
29	8.98 026	132	8.98 225		1.01 775	9.99 801	31	.8	108.0	106.4
30	8.98 157	131	8.98 358		1.01 642	9.99 800	30	.9	121.5	119.7
31	8.98 288	131	8.98 490		1.01 510	9.99 798	29		129	128
32	8.98 419	131	8.98 622		1.01 378	9.99 797	28	.1	12.9	12.8
33	8.98 549	130	8.98 753		1.01 247	9.99 796	27	.2	25.8	25.6
34	8.98 679	130	8.98 884		1.01 116	9.99 795	26	.3	38.7	38.4
35	8.98 808	129	8.99 015		1.00 985	9.99 793	25	.4	51.6	51.2
36	8.98 937	129	8.99 145		1.00 855	9.99 792	24	.5	64.5	64.0
37	8.99 066	129	8.99 275		1.00 725	9.99 791	23	.6	77.4	76.8
38	8.99 194	128	8.99 405		1.00 595	9.99 790	22	.7	90.3	89.6
39	8.99 322	128	8.99 534		1.00 466	9.99 788	21	.8	103.2	102.4
40	8.99 450	127	8.99 662		1.00 338	9.99 787	20	.9	116.1	115.2
41	8.99 577	127	8.99 791		1.00 209	9.99 786	19		125	123
42	8.99 704	127	8.99 919		1.00 081	9.99 785	18	.1	12.5	12.3
43	8.99 830	126	9.00 046		0.99 954	9.99 783	17	.2	25.0	24.6
44	8.99 956	126	9.00 174		0.99 826	9.99 782	16	.3	37.5	36.9
45	9.00 082		9.00 301		0.99 699	9.99 781	15	.4	50.0	49.2
46	9.00 207	125	9.00 427		0.99 573	9.99 780	14	.5	62.5	61.5
47	9.00 332	125	9.00 553		0.99 447	9.99 778	13	.6	75.0	73.8
48	9.00 456	124	9.00 679		0.99 321	9.99 777	12	.7	87.5	86.1
49	9.00 581	125	9.00 805		0.99 195	9.99 776	11	.8	100.0	98.4
50	9.00 704	124	9.00 930		0.99 070	9.99 775	10	.9	112.5	110.7
51	9.00 828	124	9.01 055		0.98 945	9.99 773	9		121	120
52	9.00 951	123	9.01 179		0.98 821	9.99 772	8	.1	12.1	12.0
53	9.01 074	123	9.01 303		0.98 697	9.99 771	7	.2	24.2	24.0
54	9.01 196	122	9.01 427		0.98 573	9.99 769	6	.3	36.3	36.0
55	9.01 318	122	9.01 550		0.98 450	9.99 768	5	.4	48.4	48.0
56	9.01 440	122	9.01 673		0.98 327	9.99 767	4	.5	60.5	60.0
57	9.01 561	121	9.01 796		0.98 204	9.99 765	3	.6	72.6	72.0
58	9.01 682	121	9.01 918		0.98 082	9.99 764	2	.7	84.7	84.0
59	9.01 803	120	9.02 040		0.97 960	9.99 763	1	.8	96.8	96.0
60	9.01 923		9.02 162		0.97 838	9.99 761	0	.9	108.9	108.0
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.		Prop. Pts.		

TABLE IV.

6°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.		Prop. Pts.		
0	9.01 923	120	9.02 162	121	0.97 838	9.99 761	60			
1	9.02 043	120	9.02 283	121	0.97 717	9.99 760	59	121	120	119
2	9.02 103	120	9.02 404	121	0.97 596	9.99 759	58	121	120	119
3	9.02 283	119	9.02 525	120	0.97 475	9.99 757	57	24.2	24.0	23.8
4	9.02 402	118	9.02 645	121	0.97 355	9.99 756	56	.3	36.3	35.0
5	9.02 520	119	9.02 766		0.97 234	9.99 755	55	.4	48.4	48.0
6	9.02 639	118	9.02 885		0.97 115	9.99 753	54	.5	60.5	60.0
7	9.02 757	117	9.03 005		0.96 995	9.99 752	53	.6	72.6	72.0
8	9.02 874	118	9.03 124		0.96 876	9.99 751	52	.7	84.7	84.0
9	9.02 992	117	9.03 242		0.96 758	9.99 749	51	.8	96.8	96.0
10	9.03 109	117	9.03 361		0.96 639	9.99 748	50	.9	108.9	108.0
11	9.03 226	116	9.03 479		0.96 521	9.99 747	49		118	117
12	9.03 342	116	9.03 597		0.96 403	9.99 745	48	.1	11.8	11.7
13	9.03 458	116	9.03 714		0.96 286	9.99 744	47	.2	23.6	23.4
14	9.03 574	116	9.03 832		0.96 168	9.99 742	46	.3	35.4	35.2
15	9.03 690		9.03 948		0.96 052	9.99 741	45	.4	47.2	46.8
16	9.03 805	115	9.04 065		0.95 935	9.99 740	44	.5	59.0	58.5
17	9.03 920	115	9.04 181		0.95 819	9.99 738	43	.6	70.8	70.2
18	9.04 034	114	9.04 297		0.95 703	9.99 737	42	.7	82.6	81.9
19	9.04 149	115	9.04 413		0.95 587	9.99 736	41	.8	94.4	93.6
20	9.04 262	114	9.04 528		0.95 472	9.99 734	40	.9	106.2	105.3
21	9.04 376	114	9.04 643		0.95 357	9.99 733	39		115	114
22	9.04 490	113	9.04 758		0.95 242	9.99 731	38	.1	11.5	11.4
23	9.04 603	113	9.04 873		0.95 127	9.99 730	37	.2	23.0	22.8
24	9.04 715	113	9.04 987		0.95 013	9.99 728	36	.3	34.5	34.2
25	9.04 828		9.05 101		0.94 899	9.99 727	35	.4	46.0	45.6
26	9.04 940	112	9.05 214		0.94 786	9.99 726	34	.5	57.5	57.0
27	9.05 052	112	9.05 328		0.94 672	9.99 724	33	.6	69.0	68.4
28	9.05 164	112	9.05 441		0.94 559	9.99 723	32	.7	80.5	79.8
29	9.05 275	111	9.05 553		0.94 447	9.99 721	31	.8	92.0	91.2
30	9.05 386	111	9.05 666		0.94 334	9.99 720	30	.9	103.5	102.6
31	9.05 497	110	9.05 778		0.94 222	9.99 718	29		112	111
32	9.05 607	110	9.05 890		0.94 110	9.99 717	28	.1	11.2	11.1
33	9.05 717	110	9.06 002		0.93 998	9.99 716	27	.2	22.4	22.2
34	9.05 827	110	9.06 113		0.93 887	9.99 714	26	.3	33.6	33.3
35	9.05 937	109	9.06 224		0.93 776	9.99 713	25	.4	44.8	44.4
36	9.06 046	109	9.06 335		0.93 665	9.99 711	24	.5	56.0	55.5
37	9.06 155	109	9.06 445		0.93 555	9.99 710	23	.6	67.2	66.6
38	9.06 264	108	9.06 556		0.93 444	9.99 708	22	.7	78.4	77.7
39	9.06 372	108	9.06 666		0.93 334	9.99 707	21	.8	89.6	88.8
40	9.06 481	109	9.06 775		0.93 225	9.99 705	20	.9	100.8	99.9
41	9.06 589	108	9.06 885		0.93 115	9.99 704	19		109	108
42	9.06 696	107	9.06 994		0.93 006	9.99 702	18	.1	10.9	10.8
43	9.06 804	108	9.07 103		0.92 897	9.99 701	17	.2	21.8	21.6
44	9.06 911	107	9.07 211		0.92 789	9.99 699	16	.3	32.7	32.1
45	9.07 018	106	9.07 320		0.92 680	9.99 698	15	.4	43.6	43.2
46	9.07 124	107	9.07 428		0.92 572	9.99 696	14	.5	54.5	54.0
47	9.07 231	106	9.07 536		0.92 464	9.99 695	13	.6	65.4	64.8
48	9.07 337	105	9.07 643		0.92 357	9.99 693	12	.7	76.3	75.6
49	9.07 442	106	9.07 751		0.92 249	9.99 692	11	.8	87.2	86.4
50	9.07 548	105	9.07 858		0.92 142	9.99 690	10	.9	98.1	97.2
51	9.07 653	105	9.07 964		0.92 036	9.99 689	9		106	105
52	9.07 753	105	9.08 071		0.91 929	9.99 687	8	.1	10.6	10.5
53	9.07 863	105	9.08 177		0.91 823	9.99 686	7	.2	21.2	21.0
54	9.07 968	104	9.08 283		0.91 717	9.99 684	6	.3	31.8	31.5
55	9.08 072	104	9.08 389		0.91 611	9.99 683	5	.4	42.4	42.0
56	9.08 176	104	9.08 495		0.91 505	9.99 681	4	.5	53.0	52.5
57	9.08 280	104	9.08 600		0.91 400	9.99 680	3	.6	63.6	63.0
58	9.08 383	103	9.08 705		0.91 295	9.99 678	2	.7	74.2	73.5
59	9.08 486	103	9.08 810		0.91 190	9.99 677	1	.8	84.8	84.0
60	9.08 589	103	9.08 914		0.91 086	9.99 675	0	.9	95.4	94.5
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	/	Prop. Pts.		

7°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.		Prop. Pts.
0	9.08 589	103	9.08 914	105	0.91 086	9.99 675	60	
1	9.08 692	103	9.09 019	104	0.90 981	9.99 674	.1	105 104 103
2	9.08 795	102	9.09 123	104	0.90 777	9.99 672	.2	10.5 10.4 10.3
3	9.08 897	102	9.09 227	103	0.90 773	9.99 670	.5	21.0 20.8 20.6
4	9.08 999	102	9.09 330	104	0.90 670	9.99 669	.6	31.5 31.2 30.9
5	9.09 101	101	9.09 434	103	0.90 566	9.99 667	.4	42.0 41.6 41.2
6	9.09 202	102	9.09 537	103	0.90 463	9.99 666	.5	52.5 52.0 51.5
7	9.09 304	101	9.09 640	103	0.90 360	9.99 664	.6	63.0 62.4 61.8
8	9.09 405	101	9.09 742	102	0.90 258	9.99 663	.7	73.5 72.8 72.1
9	9.09 506	100	9.09 845	103	0.90 155	9.99 661	.8	84.0 83.2 82.4
10	9.09 606	101	9.09 947	102	0.90 053	9.99 659	.9	94.5 93.6 92.7
11	9.09 707	100	9.10 049	101	0.89 951	9.99 658		102 101 100
12	9.09 807	100	9.10 150	102	0.89 850	9.99 656		10.2 10.1 10.0
13	9.09 907	99	9.10 252	101	0.89 748	9.99 655		20.4 20.2 20.0
14	9.10 006	100	9.10 353	101	0.89 647	9.99 653		30.6 30.3 30.0
15	9.10 106	99	9.10 454	101	0.89 546	9.99 651		40.8 40.4 40.0
16	9.10 205	99	9.10 555	101	0.89 445	9.99 650		51.0 50.5 50.0
17	9.10 304	98	9.10 656	100	0.89 344	9.99 648		61.2 60.6 60.0
18	9.10 402	98	9.10 756	100	0.89 244	9.99 647		71.4 70.7 70.0
19	9.10 501	98	9.10 856	100	0.89 144	9.99 645		81.6 80.8 80.0
20	9.10 599	98	9.10 956	100	0.89 044	9.99 643		91.8 90.9 90.0
21	9.10 697	98	9.11 056	99	0.88 944	9.99 642		99 98
22	9.10 795	98	9.11 155	99	0.88 845	9.99 640		9.9 9.8
23	9.10 893	97	9.11 254	99	0.88 746	9.99 638		19.8 19.6
24	9.10 990	97	9.11 353	99	0.88 647	9.99 637		29.7 29.4
25	9.11 087	97	9.11 452	99	0.88 548	9.99 635		39.6 39.2
26	9.11 184	97	9.11 551	98	0.88 449	9.99 633		49.5 49.0
27	9.11 281	96	9.11 649	98	0.88 351	9.99 632		59.4 58.8
28	9.11 377	97	9.11 747	98	0.88 253	9.99 630		69.3 68.6
29	9.11 474	96	9.11 845	98	0.88 155	9.99 629		79.2 78.4
30	9.11 570	96	9.11 943	97	0.88 057	9.99 627		89.1 88.2
31	9.11 666	95	9.12 040	97	0.87 960	9.99 625		
32	9.11 761	95	9.12 138	98	0.87 862	9.99 624		
33	9.11 857	96	9.12 235	97	0.87 765	9.99 622		
34	9.11 952	95	9.12 332	97	0.87 668	9.99 620		
35	9.12 047	95	9.12 428	97	0.87 572	9.99 618		
36	9.12 142	94	9.12 525	97	0.87 475	9.99 617		
37	9.12 236	94	9.12 621	96	0.87 379	9.99 615		
38	9.12 331	95	9.12 717	96	0.87 283	9.99 613		
39	9.12 425	94	9.12 813	96	0.87 187	9.99 612		
40	9.12 519	93	9.12 909	95	0.87 091	9.99 610		
41	9.12 612	93	9.13 004	95	0.86 996	9.99 608		
42	9.12 706	94	9.13 099	95	0.86 901	9.99 607		
43	9.12 799	93	9.13 194	95	0.86 806	9.99 605		
44	9.12 892	93	9.13 289	95	0.86 711	9.99 603		
45	9.12 985	93	9.13 384	94	0.86 616	9.99 601		
46	9.13 078	93	9.13 478	94	0.86 522	9.99 600		
47	9.13 171	93	9.13 573	95	0.86 427	9.99 598		
48	9.13 263	92	9.13 667	94	0.86 333	9.99 596		
49	9.13 355	92	9.13 761	94	0.86 239	9.99 595		
50	9.13 447	92	9.13 854	93	0.86 146	9.99 593		
51	9.13 539	91	9.13 948	94	0.86 052	9.99 591		
52	9.13 630	92	9.14 041	93	0.85 959	9.99 589		
53	9.13 722	91	9.14 134	93	0.85 866	9.99 588		
54	9.13 813	91	9.14 227	93	0.85 773	9.99 586		
55	9.13 904	90	9.14 320	93	0.85 680	9.99 584		
56	9.13 994	92	9.14 412	92	0.85 588	9.99 582		
57	9.14 085	91	9.14 504	92	0.85 496	9.99 581		
58	9.14 175	91	9.14 597	93	0.85 403	9.99 579		
59	9.14 266	91	9.14 688	92	0.85 312	9.99 577		
60	9.14 356	90	9.14 780	92	0.85 220	9.99 575		
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.		Prop. Pts.

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TABLE IV.

8°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	60	Prop. Pts.		
0	9.14 356	89	9.14 780	92	0.85 220	9.99 575	60	.1	92	91
1	9.14 445	90	9.14 872	91	0.85 128	9.99 574	59	.2	9.2	9.1
2	9.14 535	89	9.14 963	91	0.85 037	9.99 572	58	.2	18.4	18.2
3	9.14 624	90	9.15 054	91	0.84 946	9.99 570	57	.3	27.6	27.3
4	9.14 714	89	9.15 145	91	0.84 855	9.99 568	56	.4	36.8	36.4
5	9.14 803	88	9.15 236	92	0.84 764	9.99 566	55	.5	46.0	45.5
6	9.14 891	89	9.15 327	90	0.84 673	9.99 565	54	.6	55.2	54.6
7	9.14 980	89	9.15 417	91	0.84 583	9.99 563	53	.7	64.4	63.7
8	9.15 069	88	9.15 508	90	0.84 492	9.99 561	52	.8	73.6	72.8
9	9.15 157	88	9.15 598	90	0.84 402	9.99 559	51	9	82.8	81.9
10	9.15 245	88	9.15 688	89	0.84 312	9.99 557	50		89	88
11	9.15 333	88	9.15 777	90	0.84 223	9.99 556	49			
12	9.15 421	87	9.15 867	89	0.84 133	9.99 554	48	.1	8.9	8.8
13	9.15 508	88	9.15 956	90	0.84 044	9.99 552	47	.2	17.8	17.6
14	9.15 596	87	9.16 046	89	0.83 954	9.99 550	46	.3	26.7	26.4
15	9.15 683	87	9.16 135	89	0.83 865	9.99 548	45	.4	35.6	35.2
16	9.15 770	87	9.16 224	88	0.83 776	9.99 546	44	.5	44.5	44.0
17	9.15 857	87	9.16 312	89	0.83 688	9.99 545	43	.6	53.4	52.8
18	9.15 944	86	9.16 401	88	0.83 599	9.99 543	42	.7	62.3	61.6
19	9.16 030	86	9.16 489	88	0.83 511	9.99 541	41	.8	71.2	70.4
20	9.16 116	87	9.16 577	88	0.83 423	9.99 539	40	.9	80.1	79.2
21	9.16 203	86	9.16 665	88	0.83 335	9.99 537	39		87	86
22	9.16 289	85	9.16 753	88	0.83 247	9.99 535	38	.1	8.7	8.6
23	9.16 374	86	9.16 841	87	0.83 159	9.99 533	37	.2	17.4	17.2
24	9.16 460	85	9.16 928	88	0.83 072	9.99 532	36	.3	26.1	25.8
25	9.16 545	86	9.17 016	87	0.82 984	9.99 530	35	.4	34.8	34.4
26	9.16 631	86	9.17 103	87	0.82 897	9.99 528	34	.5	43.5	43.0
27	9.16 716	85	9.17 190	87	0.82 810	9.99 526	33	.6	52.2	51.6
28	9.16 801	85	9.17 277	86	0.82 723	9.99 524	32	.7	60.9	60.2
29	9.16 886	84	9.17 363	87	0.82 637	9.99 522	31	.8	69.6	68.8
30	9.16 970	85	9.17 450	86	0.82 550	9.99 520	30	.9	78.3	77.4
31	9.17 055	84	9.17 536	86	0.82 464	9.99 518	29		85	84
32	9.17 139	84	9.17 622	86	0.82 378	9.99 517	28	.1	8.5	8.4
33	9.17 223	84	9.17 708	86	0.82 292	9.99 515	27	.2	17.0	16.8
34	9.17 307	84	9.17 794	86	0.82 206	9.99 513	26	.3	25.5	25.2
35	9.17 391	83	9.17 880	85	0.82 120	9.99 511	25	.4	34.0	33.6
36	9.17 474	83	9.17 965	86	0.82 035	9.99 509	24	.5	42.5	42.0
37	9.17 558	84	9.18 051	86	0.81 949	9.99 507	23	.6	51.0	50.4
38	9.17 641	83	9.18 136	85	0.81 864	9.99 505	22	.7	59.5	58.8
39	9.17 724	83	9.18 221	85	0.81 779	9.99 503	21	.8	68.0	67.2
40	9.17 807	83	9.18 306	85	0.81 694	9.99 501	20	.9	76.5	75.6
41	9.17 890	83	9.18 391	84	0.81 609	9.99 499	19		83	82
42	9.17 973	83	9.18 475	85	0.81 525	9.99 497	18	.1	8.3	8.2
43	9.18 055	82	9.18 560	84	0.81 440	9.99 495	17	.2	16.6	16.4
44	9.18 137	83	9.18 644	84	0.81 356	9.99 494	16	.3	24.9	24.6
45	9.18 220	82	9.18 728	84	0.81 272	9.99 492	15	.4	33.2	32.8
46	9.18 302	81	9.18 812	84	0.81 188	9.99 490	14	.5	41.5	41.0
47	9.18 383	82	9.18 896	84	0.81 104	9.99 488	13	.6	49.8	49.2
48	9.18 465	82	9.18 979	83	0.81 021	9.99 486	12	.7	58.1	57.4
49	9.18 547	81	9.19 063	84	0.80 937	9.99 484	11	.8	66.4	65.6
50	9.18 628	81	9.19 146	83	0.80 854	9.99 482	10	.9	74	73.8
51	9.18 709	81	9.19 229	83	0.80 771	9.99 480	9		81	80
52	9.18 790	81	9.19 312	83	0.80 688	9.99 478	8	.1	8.1	8.0
53	9.18 871	81	9.19 395	83	0.80 605	9.99 476	7	.2	16.2	16.0
54	9.18 952	81	9.19 478	83	0.80 522	9.99 474	6	.3	24.3	24.0
55	9.19 033	80	9.19 561	82	0.80 439	9.99 472	5	.4	32.4	32.0
56	9.19 113	80	9.19 643	82	0.80 357	9.99 470	4	.5	40.5	40.0
57	9.19 193	80	9.19 725	82	0.80 275	9.99 468	3	.6	48.0	48.0
58	9.19 273	80	9.19 807	82	0.80 193	9.99 466	2	.7	56.7	56.0
59	9.19 353	80	9.19 889	82	0.80 111	9.99 464	1	.8	64.8	64.0
60	9.19 433	80	9.19 971	82	0.80 029	9.99 462	0	.9	72.9	72.0
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	/	Prop. Pts.		

9°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.		Prop. Pts.
0	9.19 433	80	9.19 971	82	0.80 029	9.99 462	60	
1	9.19 513	79	9.20 053	81	0.79 947	9.99 460	59	82 81 80
2	9.19 592	80	9.20 134	82	0.79 866	9.99 458	58	1 8.2 8.1 8.0
3	9.19 672	79	9.20 216	81	0.79 784	9.99 456	57	2 16.4 16.2 16.0
4	9.19 751	79	9.20 297	81	0.79 703	9.99 454	56	3 24.6 24.3 24.0
5	9.19 830	79	9.20 378	81	0.79 622	9.99 452	55	4 32.8 32.4 32.0
6	9.19 909	79	9.20 459	81	0.79 541	9.99 450	54	5 41.0 40.5 40.0
7	9.19 988	79	9.20 540	81	0.79 460	9.99 448	53	6 49.2 48.6 48.0
8	9.20 067	79	9.20 621	81	0.79 379	9.99 446	52	7 57.4 56.7 56.0
9	9.20 145	78	9.20 701	81	0.79 299	9.99 444	51	8 65.6 64.8 64.0
10	9.20 223	78	9.20 782	80	0.79 218	9.99 442	50	9 73.8 72.9 72.0
11	9.20 302	79	9.20 862	80	0.79 138	9.99 440	49	79 78
12	9.20 380	78	9.20 942	80	0.79 058	9.99 438	48	1 7.9 7.8
13	9.20 458	78	9.21 022	80	0.78 978	9.99 436	47	2 15.8 15.6
14	9.20 535	77	9.21 102	80	0.78 898	9.99 434	46	3 23.7 23.4
15	9.20 613	78	9.21 182	79	0.78 818	9.99 432	45	4 31.6 31.2
16	9.20 691	78	9.21 261	79	0.78 739	9.99 429	44	5 39.5 39.0
17	9.20 768	77	9.21 341	79	0.78 659	9.99 427	43	6 47.4 46.8
18	9.20 845	77	9.21 420	79	0.78 580	9.99 425	42	7 55.3 54.6
19	9.20 922	77	9.21 499	79	0.78 501	9.99 423	41	8 63.2 62.4
20	9.20 999	77	9.21 578	79	0.78 422	9.99 421	40	9 71.1 70.2
21	9.21 076	77	9.21 657	79	0.78 343	9.99 419	39	77 76
22	9.21 153	77	9.21 736	79	0.78 264	9.99 417	38	1 7.7 7.6
23	9.21 229	76	9.21 814	78	0.78 186	9.99 415	37	2 15.4 15.2
24	9.21 306	77	9.21 893	79	0.78 107	9.99 413	36	3 23.1 22.8
25	9.21 382	76	9.21 971	78	0.78 029	9.99 411	35	4 30.8 30.4
26	9.21 458	76	9.22 049	78	0.77 951	9.99 409	34	5 38.5 38.0
27	9.21 534	76	9.22 127	78	0.77 873	9.99 407	33	6 46.2 45.6
28	9.21 610	76	9.22 205	78	0.77 795	9.99 404	32	7 53.9 53.2
29	9.21 685	75	9.22 283	78	0.77 717	9.99 402	31	8 61.6 60.8
30	9.21 761	76	9.22 361	78	0.77 639	9.99 400	30	9 69.3 68.4
31	9.21 836	75	9.22 438	77	0.77 552	9.99 398	29	75 74
32	9.21 912	76	9.22 516	78	0.77 484	9.99 396	28	1 7.5 7.4
33	9.21 987	75	9.22 593	77	0.77 407	9.99 394	27	2 15.0 14.8
34	9.22 062	75	9.22 670	77	0.77 330	9.99 392	26	3 22.5 22.2
35	9.22 137	75	9.22 747	77	0.77 253	9.99 390	25	4 30.0 29.6
36	9.22 211	74	9.22 824	77	0.77 176	9.99 388	24	5 37.5 37.0
37	9.22 286	75	9.22 901	77	0.77 109	9.99 385	23	6 45.0 44.4
38	9.22 361	75	9.22 977	76	0.77 023	9.99 383	22	7 52.5 51.8
39	9.22 435	74	9.23 054	77	0.76 946	9.99 381	21	8 60.0 59.2
40	9.22 509	74	9.23 130	76	0.76 870	9.99 379	20	9 67.5 66.6
41	9.22 583	74	9.23 206	76	0.76 794	9.99 377	19	73 72
42	9.22 657	74	9.23 283	77	0.76 717	9.99 375	18	1 7.3 7.2
43	9.22 731	74	9.23 359	76	0.76 641	9.99 372	17	2 14.6 14.4
44	9.22 805	74	9.23 435	76	0.76 565	9.99 370	16	3 21.9 21.6
45	9.22 878	73	9.23 510	75	0.76 490	9.99 368	15	4 29.2 28.8
46	9.22 952	74	9.23 586	76	0.76 414	9.99 366	14	5 36.5 36.0
47	9.23 025	73	9.23 661	75	0.76 339	9.99 364	13	6 43.8 43.2
48	9.23 098	73	9.23 737	76	0.76 263	9.99 362	12	7 51.1 50.4
49	9.23 171	73	9.23 812	75	0.76 188	9.99 359	11	8 58.4 57.6
50	9.23 244	73	9.23 887	75	0.76 113	9.99 357	10	9.65.71 64.8
51	9.23 317	73	9.23 962	75	0.76 038	9.99 355	9	71 3 2
52	9.23 390	73	9.24 037	75	0.75 963	9.99 353	8	1 0.3 0.2
53	9.23 462	72	9.24 112	75	0.75 888	9.99 351	7	2 14.2 0 6 0.4
54	9.23 535	73	9.24 186	74	0.75 814	9.99 348	6	3 21.3 0.9 0.6
55	9.23 607	72	9.24 261	75	0.75 739	9.99 346	5	4 28.4 1.2 0.8
56	9.23 679	72	9.24 335	74	0.75 665	9.99 344	4	5 35.5 1.5 1.0
57	9.23 752	73	9.24 410	75	0.75 590	9.99 342	3	6 42.6 1 8 1.2
58	9.23 823	71	9.24 484	74	0.75 516	9.99 340	2	7 49.7 2 1 1.4
59	9.23 895	72	9.24 558	74	0.75 442	9.99 337	1	8 56.8 2 4 1.6
60	9.23 967	72	9.24 632	74	0.75 368	9.99 335	0	9.63.9 2 7 1.8
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	,	Prop. Pts.

TABLE IV.

10°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.		Prop. Pts.
	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	60	Prop. Pts.
0	9.23 967	72	9.24 632	74	0.75 368	9.99 335	60	
1	9.24 039	71	9.24 706	73	0.75 294	9.99 333	59	.1 7.4 7.3
2	9.24 110	71	9.24 779	74	0.75 221	9.99 331	58	.2 14.8 14.6
3	9.24 181	72	9.24 853	73	0.75 147	9.99 328	57	.3 22.2 21.9
4	9.24 253	71	9.24 926	74	0.75 074	9.99 326	56	.4 29.6 29.2
5	9.24 324	71	9.25 000	73	0.75 000	9.99 324	55	.5 37.0 36.5
6	9.24 395	71	9.25 073	73	0.74 927	9.99 322	54	.6 44.4 43.8
7	9.24 466	70	9.25 146	73	0.74 854	9.99 319	53	.7 51.8 51.1
8	9.24 536	70	9.25 219	73	0.74 781	9.99 317	52	.8 59.2 58.4
9	9.24 607	71	9.25 292	73	0.74 708	9.99 315	51	.9 66.6 65.7
10	9.24 677	70	9.25 365	73	0.74 635	9.99 313	50	
11	9.24 748	71	9.25 437	72	0.74 563	9.99 310	49	.1 7.2 7.1
12	9.24 818	70	9.25 510	73	0.74 490	9.99 308	48	.2 14.4 14.2
13	9.24 888	70	9.25 582	72	0.74 418	9.99 306	47	.3 21.6 21.3
14	9.24 958	70	9.25 655	73	0.74 345	9.99 304	46	.4 28.8 28.4
15	9.25 028	70	9.25 727	72	0.74 273	9.99 301	45	.5 36.0 35.5
16	9.25 098	70	9.25 799	72	0.74 201	9.99 299	44	.6 43.2 42.6
17	9.25 168	70	9.25 871	72	0.74 129	9.99 297	43	.7 50.4 49.7
18	9.25 237	69	9.25 943	72	0.74 057	9.99 294	42	.8 57.6 56.8
19	9.25 307	70	9.26 015	72	0.73 985	9.99 292	41	.9 64.8 63.9
20	9.25 376	69	9.26 085	71	0.73 914	9.99 290	40	
21	9.25 445	69	9.26 158	72	0.73 842	9.99 288	39	.1 7.0 6.9
22	9.25 514	69	9.26 229	71	0.73 771	9.99 285	38	.2 14.0 13.8
23	9.25 583	69	9.26 301	72	0.73 699	9.99 283	37	.3 21.0 20.7
24	9.25 652	69	9.26 372	71	0.73 628	9.99 281	36	.4 28.0 27.6
25	9.25 721	69	9.26 443	71	0.73 557	9.99 278	35	.5 35.0 34.5
26	9.25 790	68	9.26 514	71	0.73 486	9.99 276	34	.6 42.0 41.4
27	9.25 858	69	9.26 585	70	0.73 415	9.99 274	33	.7 49.0 48.3
28	9.25 927	68	9.26 655	70	0.73 345	9.99 271	32	.8 56.0 55.2
29	9.25 995	68	9.26 726	71	0.73 274	9.99 269	31	.9 63.0 62.1
30	9.26 063	68	9.26 797	70	0.73 203	9.99 267	30	
31	9.26 131	68	9.26 867	70	0.73 133	9.99 264	29	.1 6.8 6.7
32	9.26 199	68	9.26 937	70	0.73 063	9.99 262	28	.2 13.6 13.4
33	9.26 267	68	9.27 008	71	0.72 992	9.99 260	27	.3 20.4 20.1
34	9.26 335	68	9.27 078	70	0.72 922	9.99 257	26	.4 27.2 26.8
35	9.26 403	67	9.27 148	70	0.72 852	9.99 255	25	.5 34.0 33.5
36	9.26 470	67	9.27 218	70	0.72 782	9.99 252	24	.6 40.8 40.2
37	9.26 538	68	9.27 288	69	0.72 712	9.99 250	23	.7 47.6 46.9
38	9.26 605	67	9.27 357	70	0.72 643	9.99 248	22	.8 54.4 53.6
39	9.26 672	67	9.27 427	69	0.72 573	9.99 245	21	.9 61.2 60.3
40	9.26 739	67	9.27 496	70	0.72 504	9.99 243	20	
41	9.26 806	67	9.27 566	69	0.72 434	9.99 241	19	.1 6.6 6.5
42	9.26 873	67	9.27 635	69	0.72 365	9.99 238	18	.2 13.2 13.0
43	9.26 940	67	9.27 704	69	0.72 296	9.99 236	17	.3 19.8 19.5
44	9.27 007	66	9.27 773	69	0.72 227	9.99 233	16	.4 26.4 26.0
45	9.27 073	67	9.27 842	69	0.72 158	9.99 231	15	.5 33.0 32.3
46	9.27 140	67	9.27 911	69	0.72 089	9.99 229	14	.6 39.6 39.0
47	9.27 206	66	9.27 980	69	0.72 020	9.99 226	13	.7 46.2 45.5
48	9.27 273	67	9.28 049	68	0.71 951	9.99 224	12	.8 52.8 52.0
49	9.27 339	66	9.28 117	68	0.71 883	9.99 221	11	.9 59.4 58.5
50	9.27 405	66	9.28 186	68	0.71 814	9.99 219	10	
51	9.27 471	66	9.28 254	69	0.71 746	9.99 217	9	.1 0.1 0.2
52	9.27 537	65	9.28 323	68	0.71 677	9.99 214	8	.2 0.6 0.4
53	9.27 602	65	9.28 391	68	0.71 609	9.99 212	7	.3 0.9 0.6
54	9.27 668	66	9.28 459	68	0.71 541	9.99 209	6	.4 1.2 0.8
55	9.27 734	65	9.28 527	68	0.71 473	9.99 207	5	.5 1.5 1.0
56	9.27 799	65	9.28 595	67	0.71 405	9.99 204	4	.6 1.8 1.2
57	9.27 864	66	9.28 662	68	0.71 338	9.99 202	3	.7 2.1 1.4
58	9.27 930	65	9.28 730	68	0.71 270	9.99 200	2	.8 2.4 1.6
59	9.27 995	65	9.28 798	68	0.71 202	9.99 197	1	.9 2.7 1.8
60	9.28 060	65	9.28 865	67	0.71 135	9.99 195	0	
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	/	Prop. Pts.

## 11°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.		Prop. Pts.
0	9.28 060	65	9.28 865	68	0.71 135	9.99 195	60	
1	9.28 125	65	9.28 933	67	0.71 067	9.99 192	59	68 67
2	9.28 190	64	9.29 000	67	0.71 000	9.99 190	58	6.8 6.7
3	9.28 254	65	9.29 067	67	0.70 933	9.99 187	57	.1 13.0 13.4
4	9.28 319	65	9.29 134	67	0.70 866	9.99 185	56	.2 20.4 20.1
5	9.28 384		9.29 201	67	0.70 799	9.99 182	55	.3 27.2 26.8
6	9.28 448	64	9.29 268	67	0.70 732	9.99 180	54	.5 34.0 33.5
7	9.28 512	64	9.29 335	67	0.70 665	9.99 177	53	.6 40.8 40.2
8	9.28 577	65	9.29 402	66	0.70 598	9.99 175	52	.7 47.6 46.9
9	9.28 641	64	9.29 468	67	0.70 532	9.99 172	51	.8 54.4 53.6
10	9.28 705	64	9.29 535	66	0.70 465	9.99 170	50	.9 61.2 60.3
11	9.28 769	64	9.29 601	67	0.70 399	9.99 167	49	66 65
12	9.28 833	63	9.29 668	66	0.70 332	9.99 165	48	6.6 6.5
13	9.28 896	64	9.29 734	66	0.70 266	9.99 162	47	.2 13.2 13.0
14	9.28 960	64	9.29 800	66	0.70 200	9.99 160	46	.3 19.8 19.5
15	9.29 024		9.29 866	66	0.70 134	9.99 157	45	.4 26.4 26.0
16	9.29 087	63	9.29 932	66	0.70 068	9.99 155	44	.5 33.0 32.5
17	9.29 150	63	9.29 998	66	0.70 002	9.99 152	43	.6 39.6 39.0
18	9.29 214	64	9.30 064	66	0.69 936	9.99 150	42	.7 46.2 45.5
19	9.29 277	63	9.30 130	65	0.69 870	9.99 147	41	.8 52.8 52.0
20	9.29 340		9.30 195	66	0.69 805	9.99 145	40	.9 59.4 58.5
21	9.29 403	63	9.30 261	66	0.69 739	9.99 142	39	64 63
22	9.29 466	63	9.30 326	65	0.69 674	9.99 140	38	.1 6.4 6.3
23	9.29 529	62	9.30 391	65	0.69 609	9.99 137	37	.2 12.8 12.6
24	9.29 591	63	9.30 457	65	0.69 543	9.99 135	36	.3 19.2 18.9
25	9.29 654	62	9.30 522	65	0.69 478	9.99 132	35	.4 25.6 25.2
26	9.29 716	63	9.30 587	65	0.69 413	9.99 130	34	.5 32.0 31.5
27	9.29 779	62	9.30 652	65	0.69 348	9.99 127	33	.6 38.4 37.8
28	9.29 841	62	9.30 717	65	0.69 283	9.99 124	32	.7 44.8 44.1
29	9.29 903	63	9.30 782	65	0.69 218	9.99 122	31	.8 51.2 50.4
30	9.29 966	62	9.30 846	64	0.69 154	9.99 119	30	.9 57.6 56.7
31	9.30 028	62	9.30 911	64	0.69 089	9.99 117	29	62 61
32	9.30 090	61	9.30 975	65	0.69 025	9.99 114	28	.1 6.2 6.1
33	9.30 151	62	9.31 040	64	0.68 960	9.99 112	27	.2 12.4 12.2
34	9.30 213	62	9.31 104	64	0.68 896	9.99 109	26	.3 18.6 18.3
35	9.30 275	61	9.31 168	64	0.68 832	9.99 106	25	.4 24.8 24.4
36	9.30 336	62	9.31 233	65	0.68 767	9.99 104	24	.5 31.0 30.5
37	9.30 398	61	9.31 297	64	0.68 703	9.99 101	23	.6 37.2 36.6
38	9.30 459	62	9.31 361	64	0.68 639	9.99 099	22	.7 43.4 42.7
39	9.30 521	61	9.31 425	64	0.68 575	9.99 096	21	.8 49.6 48.8
40	9.30 582	61	9.31 489	64	0.68 511	9.99 093	20	.9 55.8 54.9
41	9.30 643	61	9.31 552	63	0.68 448	9.99 091	19	60 59
42	9.30 704	61	9.31 616	64	0.68 384	9.99 088	18	.1 6.0 5.9
43	9.30 765	61	9.31 679	63	0.68 321	9.99 086	17	.2 12.0 11.8
44	9.30 826	61	9.31 743	64	0.68 257	9.99 083	16	.3 18.0 17.7
45	9.30 887	60	9.31 806	63	0.68 194	9.99 080	15	.4 24.0 23.6
46	9.30 947	61	9.31 870	63	0.68 130	9.99 078	14	.5 30.0 29.5
47	9.31 008	60	9.31 933	63	0.68 067	9.99 075	13	.6 36.0 35.4
48	9.31 068	61	9.31 996	63	0.68 004	9.99 072	12	.7 42.0 41.3
49	9.31 129	60	9.32 059	63	0.67 941	9.99 070	11	.8 48.0 47.2
50	9.31 189	61	9.32 122	63	0.67 878	9.99 067	10	.9 54.0 53.1
51	9.31 250	60	9.32 185	63	0.67 815	9.99 064	9	3 2
52	9.31 310	60	9.32 248	63	0.67 752	9.99 062	8	.1 0.3 0.2
53	9.31 370	60	9.32 311	63	0.67 689	9.99 059	7	.2 0.6 0.4
54	9.31 430	60	9.32 373	63	0.67 627	9.99 056	6	.3 0.9 0.6
55	9.31 490		9.32 436	62	0.67 564	9.99 054	5	.4 1.2 0.8
56	9.31 549	59	9.32 498	62	0.67 502	9.99 051	4	.5 1.5 1.0
57	9.31 609	60	9.32 561	63	0.67 439	9.99 048	3	.6 1.8 1.2
58	9.31 669	60	9.32 623	62	0.67 377	9.99 046	2	.7 2.1 1.4
59	9.31 728	59	9.32 685	62	0.67 315	9.99 043	1	.8 2.4 1.6
60	9.31 788	60	9.32 747	62	0.67 253	9.99 040	0	.9 2.7 1.8
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	'	Prop. Pts.

TABLE IV.

12°

/	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.		Prop. Pts.
0	9.31 788	59	9.32 747	63	0.67 253	9.99 040	60	
1	9.31 847	60	9.32 810	62	0.67 190	9.99 038	59	63 62
2	9.31 907	59	9.32 872	61	0.67 128	9.99 035	58	.1 6.3 6.2
3	9.31 966	59	9.32 933	62	0.67 067	9.99 032	57	.2 12.6 12.4
4	9.32 025	59	9.32 995	62	0.67 005	9.99 030	56	.3 18.9 18.6
5	9.32 084	59	9.33 057	62	0.66 943	9.99 027	55	.4 25.2 24.8
6	9.32 143	59	9.33 119	61	0.66 881	9.99 024	54	.5 31.5 31.0
7	9.32 202	59	9.33 180	62	0.66 820	9.99 022	53	.6 37.8 37.2
8	9.32 261	58	9.33 242	61	0.66 758	9.99 019	52	.7 44.1 43.4
9	9.32 319	59	9.33 303	62	0.66 697	9.99 016	51	.8 50.4 49.6
10	9.32 378	59	9.33 365	61	0.66 635	9.99 013	50	.9 56.7 55.8
11	9.32 437	58	9.33 426	61	0.66 574	9.99 011	49	
12	9.32 495	58	9.33 487	61	0.66 513	9.99 008	48	.1 6.1 6.0
13	9.32 553	59	9.33 548	61	0.66 452	9.99 005	47	.2 12.2 12.0
14	9.32 612	58	9.33 609	61	0.66 391	9.99 002	46	.3 18.3 18.0
15	9.32 670	58	9.33 670	61	0.66 330	9.99 000	45	.4 24.4 24.0
16	9.32 728	58	9.33 731	61	0.66 269	9.98 997	44	.5 30.5 30.0
17	9.32 786	58	9.33 792	61	0.66 208	9.98 994	43	.6 36.6 36.0
18	9.32 844	58	9.33 853	60	0.66 147	9.98 991	42	.7 42.7 42.0
19	9.32 902	58	9.33 913	61	0.66 087	9.98 989	41	.8 48.8 48.0
20	9.32 960	58	9.33 974	60	0.66 026	9.98 986	40	.9 54.9 54.0
21	9.33 018	58	9.34 034	61	0.65 966	9.98 983	39	
22	9.33 075	57	9.34 095	60	0.65 905	9.98 980	38	.1 5.9
23	9.33 133	58	9.34 155	60	0.65 845	9.98 978	37	.2 11.8
24	9.33 190	57	9.34 215	61	0.65 785	9.98 975	36	.3 17.7
25	9.33 248	57	9.34 276	61	0.65 724	9.98 972	35	.4 23.6
26	9.33 305	57	9.34 336	60	0.65 664	9.98 969	34	.5 29.5
27	9.33 362	57	9.34 396	60	0.65 604	9.98 967	33	.6 35.4
28	9.33 420	58	9.34 456	60	0.65 544	9.98 964	32	.7 41.3
29	9.33 477	57	9.34 516	60	0.65 484	9.98 961	31	.8 47.2
30	9.33 534	57	9.34 576	59	0.65 424	9.98 958	30	.9 53.1
31	9.33 591	56	9.34 635	60	0.65 365	9.98 955	29	
32	9.33 647	56	9.34 695	60	0.65 305	9.98 953	28	.1 5.8 5.7
33	9.33 704	57	9.34 755	59	0.65 245	9.98 950	27	.2 11.6 11.4
34	9.33 761	57	9.34 814	60	0.65 186	9.98 947	26	.3 17.4 17.1
35	9.33 818	56	9.34 874	59	0.65 126	9.98 944	25	.4 23.2 22.8
36	9.33 874	57	9.34 933	59	0.65 067	9.98 941	24	.5 29.0 28.5
37	9.33 931	57	9.34 992	59	0.65 008	9.98 938	23	.6 34.8 34.2
38	9.33 987	56	9.35 051	60	0.64 949	9.98 936	22	.7 40.6 39.9
39	9.34 043	57	9.35 III	59	0.64 889	9.98 933	21	.8 46.4 45.6
40	9.34 100	56	9.35 170	59	0.64 830	9.98 930	20	.9 52.2 51.3
41	9.34 156	56	9.35 229	59	0.64 771	9.98 927	19	
42	9.34 212	56	9.35 288	59	0.64 712	9.98 924	18	.1 5.6 5.5
43	9.34 268	56	9.35 347	58	0.64 653	9.98 921	17	.2 11.2 11.0
44	9.34 324	56	9.35 405	59	0.64 595	9.98 919	16	.3 16.8 16.5
45	9.34 380	56	9.35 464	59	0.64 536	9.98 916	15	.4 22.4 22.0
46	9.34 436	55	9.35 523	58	0.64 477	9.98 913	14	.5 28.0 27.5
47	9.34 491	55	9.35 581	58	0.64 419	9.98 910	13	.6 33.6 33.0
48	9.34 547	56	9.35 640	58	0.64 360	9.98 907	12	.7 39.2 38.5
49	9.34 602	55	9.35 698	58	0.64 302	9.98 904	11	.8 44.8 44.0
50	9.34 658	55	9.35 757	58	0.64 243	9.98 901	10	.9 50.4 49.5
51	9.34 713	55	9.35 815	58	0.64 185	9.98 898	9	
52	9.34 769	56	9.35 873	58	0.64 127	9.98 896	8	.1 0.3 0.2
53	9.34 824	55	9.35 931	58	0.64 069	9.98 893	7	.2 0.6 0.4
54	9.34 879	55	9.35 989	58	0.64 011	9.98 890	6	.3 0.9 0.6
55	9.34 934	55	9.36 047	58	0.63 953	9.98 887	5	.4 1.2 0.8
56	9.34 989	55	9.36 105	58	0.63 895	9.98 884	4	.5 1.5 1.0
57	9.35 044	55	9.36 163	58	0.63 837	9.98 881	3	.6 1.8 1.2
58	9.35 099	55	9.36 221	58	0.63 779	9.98 878	2	.7 2.1 1.4
59	9.35 154	55	9.36 279	57	0.63 721	9.98 875	1	.8 2.4 1.6
60	9.35 209	55	9.36 336	57	0.63 664	9.98 872	0	.9 2.7 1.8
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	/	Prop. Pts.

77°

## 13°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.		Prop. Pts.
0	9.35 209	54	9.36 336	58	0.63 664	9.98 872	60	
1	9.35 263	55	9.36 394	58	0.63 606	9.98 869	59	.1 5.8 5.7
2	9.35 318	55	9.36 452	57	0.63 548	9.98 867	58	.2 11.6 11.4
3	9.35 373	55	9.36 509	57	0.63 491	9.98 864	57	.3 17.4 17.1
4	9.35 427	54	9.36 566	58	0.63 434	9.98 861	56	
5	9.35 481	55	9.36 624	57	0.63 376	9.98 858	55	.4 23.2 22.8
6	9.35 536	54	9.36 681	57	0.63 319	9.98 855	54	.5 29.0 28.5
7	9.35 590	54	9.36 738	57	0.63 262	9.98 852	53	.6 34.8 34.2
8	9.35 644	54	9.36 795	57	0.63 205	9.98 849	52	.7 40.6 39.9
9	9.35 698	54	9.36 852	57	0.63 148	9.98 846	51	.8 46.4 45.6
10	9.35 752	54	9.36 909	57	0.63 091	9.98 843	50	.9 52.2 51.3
11	9.35 806	54	9.36 966	57	0.63 034	9.98 840	49	
12	9.35 860	54	9.37 023	57	0.62 977	9.98 837	48	.1 5.6 5.5
13	9.35 914	54	9.37 080	57	0.62 920	9.98 834	47	.2 11.2 11.0
14	9.35 968	54	9.37 137	57	0.62 863	9.98 831	46	.3 16.8 16.5
15	9.36 022	53	9.37 193	57	0.62 807	9.98 828	45	.4 22.4 22.0
16	9.36 075	53	9.37 250	56	0.62 750	9.98 825	44	.5 28.0 27.5
17	9.36 129	54	9.37 306	56	0.62 694	9.98 822	43	.6 33.6 33.0
18	9.36 182	53	9.37 363	57	0.62 637	9.98 819	42	.7 39.2 38.5
19	9.36 236	54	9.37 419	56	0.62 581	9.98 816	41	.8 44.8 44.0
20	9.36 289	53	9.37 476	56	0.62 524	9.98 813	40	.9 50.4 49.5
21	9.36 342	53	9.37 532	56	0.62 468	9.98 810	39	
22	9.36 395	53	9.37 588	56	0.62 412	9.98 807	38	.1 5.4
23	9.36 449	54	9.37 644	56	0.62 356	9.98 804	37	.2 10.8
24	9.36 502	53	9.37 700	56	0.62 300	9.98 801	36	.3 16.2
25	9.36 555	53	9.37 756	56	0.62 244	9.98 798	35	.4 21.6
26	9.36 608	53	9.37 812	56	0.62 188	9.98 795	34	.5 27.0
27	9.36 660	52	9.37 868	56	0.62 132	9.98 792	33	.6 32.4
28	9.36 713	53	9.37 924	56	0.62 076	9.98 789	32	.7 37.8
29	9.36 766	53	9.37 980	56	0.62 020	9.98 786	31	.8 43.2
30	9.36 819	53	9.38 035	56	0.61 965	9.98 783	30	.9 48.6
31	9.36 871	52	9.38 091	56	0.61 909	9.98 780	29	
32	9.36 924	53	9.38 147	56	0.61 853	9.98 777	28	.1 5.3 5.2
33	9.36 976	52	9.38 202	55	0.61 798	9.98 774	27	.2 10.6 10.4
34	9.37 028	53	9.38 257	56	0.61 743	9.98 771	26	.3 15.9 15.6
35	9.37 081	52	9.38 313	55	0.61 687	9.98 768	25	.4 21.2 20.8
36	9.37 133	52	9.38 368	55	0.61 632	9.98 765	24	.5 26.5 26.0
37	9.37 185	52	9.38 423	56	0.61 577	9.98 762	23	.6 31.8 31.7
38	9.37 237	52	9.38 479	56	0.61 521	9.98 759	22	.7 37.1 36.4
39	9.37 289	52	9.38 534	55	0.61 466	9.98 756	21	.8 42.4 41.6
40	9.37 341	52	9.38 589	55	0.61 411	9.98 753	20	.9 47.7 46.8
41	9.37 393	52	9.38 644	55	0.61 356	9.98 750	19	
42	9.37 445	52	9.38 699	55	0.61 301	9.98 749	18	.1 5.1 0.4
43	9.37 497	52	9.38 754	55	0.61 246	9.98 743	17	.2 10.2 0.8
44	9.37 549	51	9.38 808	55	0.61 192	9.98 740	16	.3 15.3 1.2
45	9.37 600	52	9.38 863	55	0.61 137	9.98 737	15	.4 20.4 1.6
46	9.37 652	52	9.38 918	55	0.61 082	9.98 734	14	.5 25.5 2.0
47	9.37 703	51	9.38 972	54	0.61 028	9.98 731	13	.6 30.6 2.4
48	9.37 755	52	9.39 027	55	0.60 973	9.98 728	12	.7 35.7 2.8
49	9.37 806	51	9.39 082	55	0.60 918	9.98 725	11	.8 40.8 3.2
50	9.37 858	52	9.39 136	54	0.60 864	9.98 722	10	.9 45.9 3.6
51	9.37 909	51	9.39 190	54	0.60 810	9.98 719	9	
52	9.37 960	51	9.39 245	55	0.60 755	9.98 715	8	.1 0.3 0.2
53	9.38 011	51	9.39 299	54	0.60 701	9.98 712	7	.2 0.6 0.4
54	9.38 062	51	9.39 353	54	0.60 647	9.98 709	6	.3 0.9 0.6
55	9.38 113	51	9.39 407	54	0.60 593	9.98 706	5	.4 1.2 0.8
56	9.38 164	51	9.39 461	54	0.60 539	9.98 703	4	.5 1.5 1.0
57	9.38 215	51	9.39 515	54	0.60 485	9.98 700	3	.6 1.8 1.2
58	9.38 266	51	9.39 569	54	0.60 431	9.98 697	2	.7 2.1 1.4
59	9.38 317	51	9.39 623	54	0.60 377	9.98 694	1	.8 2.4 1.6
60	9.38 368	51	9.39 677	54	0.60 323	9.98 690	0	.9 2.7 1.8
L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	'	Prop. Pts.	

TABLE IV.

14°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.38 368		9.39 677		0.60 323	9.98 690	3	60	
1	9.38 418	50	9.39 731	54	0.60 269	9.98 687	3	59	.1 5.4 5.3
2	9.38 469	51	9.39 785	54	0.60 215	9.98 684	3	58	.2 10.8 10.6
3	9.38 519	50	9.39 838	53	0.60 162	9.98 681	3	57	.1 5.4 5.3
4	9.38 570	51	9.39 892	54	0.60 108	9.98 678	3	56	.2 10.8 10.6
5	9.38 620	50	9.39 945	53	0.60 055	9.98 675	3	55	.3 16.2 15.9
6	9.38 670	50	9.39 999	54	0.60 001	9.98 671	4	54	.4 21.6 21.2
7	9.38 721	51	9.40 052	53	0.59 948	9.98 668	3	53	.5 27.0 26.5
8	9.38 771	50	9.40 106	53	0.59 894	9.98 665	3	52	.6 32.4 31.8
9	9.38 821	50	9.40 159	53	0.59 841	9.98 662	3	51	.7 37.8 37.1
10	9.38 871	50	9.40 212	53	0.59 788	9.98 659	3	50	.8 43.2 42.4
11	9.38 921	50	9.40 266	54	0.59 734	9.98 656	3	49	.9 48.6 47.7
12	9.38 971	50	9.40 319	53	0.59 681	9.98 652	4	48	
13	9.39 021	50	9.40 372	53	0.59 628	9.98 649	3	47	
14	9.39 071	50	9.40 425	53	0.59 575	9.98 646	3	46	1 52 51
15	9.39 121		9.40 478	53	0.59 522	9.98 643	3	45	.1 5.2 5.1
16	9.39 170	49	9.40 531	53	0.59 469	9.98 640	3	44	.2 10.4 10.2
17	9.39 220	50	9.40 584	53	0.59 416	9.98 636	4	43	.3 15.6 15.3
18	9.39 270	50	9.40 636	52	0.59 364	9.98 633	3	42	.4 20.8 20.4
19	9.39 319	49	9.40 689	53	0.59 311	9.98 630	3	41	.5 26.0 25.5
20	9.39 369		9.40 742	53	0.59 258	9.98 627	3	40	.6 31.2 30.6
21	9.39 418	49	9.40 795	53	0.59 205	9.98 623	4	39	.7 36.4 35.7
22	9.39 467	49	9.40 847	52	0.59 153	9.98 620	3	38	.8 41.6 40.8
23	9.39 517	50	9.40 900	53	0.59 100	9.98 617	3	37	.9 46.8 45.9
24	9.39 566	49	9.40 952	53	0.59 048	9.98 614	3	36	
25	9.39 615		9.41 005	52	0.58 995	9.98 610	4	35	
26	9.39 664	49	9.41 057	52	0.58 943	9.98 607	3	34	.1 50 49
27	9.39 713	49	9.41 109	52	0.58 891	9.98 604	3	33	.2 10.0 9.8
28	9.39 762	49	9.41 161	52	0.58 839	9.98 601	3	32	.3 15.0 14.7
29	9.39 811	49	9.41 214	53	0.58 786	9.98 597	4	31	.4 20.0 19.6
30	9.39 860		9.41 266	52	0.58 734	9.98 594	3	30	.5 25.0 24.5
31	9.39 909	49	9.41 318	52	0.58 682	9.98 591	3	29	.6 30.0 29.4
32	9.39 958	49	9.41 370	52	0.58 630	9.98 588	3	28	
33	9.40 006	48	9.41 422	52	0.58 578	9.98 584	4	27	.7 35.0 34.3
34	9.40 055	49	9.41 474	52	0.58 526	9.98 581	3	26	.8 40.0 39.2
35	9.40 103		9.41 526	52	0.58 474	9.98 578	3	25	.9 45.0 44.1
36	9.40 152	49	9.41 578	52	0.58 422	9.98 574	4	24	
37	9.40 200	48	9.41 629	51	0.58 371	9.98 571	3	23	
38	9.40 249	49	9.41 681	52	0.58 319	9.98 568	3	22	
39	9.40 297	48	9.41 733	52	0.58 267	9.98 565	3	21	.1 4.8 4.7
40	9.40 346	49	9.41 784	51	0.58 216	9.98 561	4	20	.2 9.6 9.4
41	9.40 394	48	9.41 836	52	0.58 164	9.98 558	3	19	
42	9.40 442	48	9.41 887	51	0.58 113	9.98 555	3	18	.4 19.2 18.8
43	9.40 490	48	9.41 939	52	0.58 061	9.98 551	4	17	.5 24.0 23.5
44	9.40 538	48	9.41 990	51	0.58 010	9.98 548	3	16	.6 28.8 28.2
45	9.40 586		9.42 041	52	0.57 959	9.98 545	3	15	.7 33.6 32.9
46	9.40 634	48	9.42 093	52	0.57 907	9.98 541	4	14	.8 38.4 37.6
47	9.40 682	48	9.42 144	51	0.57 856	9.98 538	3	13	.9 43.2 42.3
48	9.40 730	48	9.42 195	52	0.57 805	9.98 535	3	12	
49	9.40 778	48	9.42 246	51	0.57 754	9.98 531	4	11	
50	9.40 825	47	9.42 297	51	0.57 703	9.98 528	3	10	.1 0.4 0.3
51	9.40 873	48	9.42 348	52	0.57 652	9.98 525	3	9	.2 0.8 0.6
52	9.40 921	48	9.42 399	51	0.57 601	9.98 521	4	8	.3 1.2 0.9
53	9.40 968	47	9.42 450	52	0.57 550	9.98 518	3	7	.4 1.6 1.2
54	9.41 016	48	9.42 501	51	0.57 499	9.98 515	3	6	.5 2.0 1.5
55	9.41 063	47	9.42 552	52	0.57 448	9.98 511	4	5	.6 2.4 1.8
56	9.41 111	48	9.42 603	51	0.57 397	9.98 508	3	4	.7 2.8 2.1
57	9.41 158	47	9.42 653	50	0.57 347	9.98 505	3	3	.8 3.2 2.4
58	9.41 205	47	9.42 704	51	0.57 296	9.98 501	4	2	
59	9.41 252	47	9.42 755	50	0.57 245	9.98 498	3	1	.9 3.6 2.7
60	9.41 300	48	9.42 805	50	0.57 195	9.98 494	4	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

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## 15°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.41 300	47	9.42 805	51	0.57 195	9.98 494	3	<b>60</b>	
1	9.41 347	47	9.42 856	50	0.57 144	9.98 491	3	59	.1 5.1 5.0
2	9.41 394	47	9.42 906	51	0.57 094	9.98 488	3	58	.2 10.2 10.0
3	9.41 441	47	9.42 957	50	0.57 043	9.98 484	4	57	.3 15.3 15.0
4	9.41 488	47	9.43 007	50	0.56 993	9.98 481	3	56	.4 20.4 20.0
5	9.41 535	47	9.43 057	51	0.56 943	9.98 477	4	55	.5 25.5 25.0
6	9.41 582	46	9.43 108	50	0.56 892	9.98 474	3	54	.6 30.6 30.0
7	9.41 628	47	9.43 158	50	0.56 842	9.98 471	4	53	.7 35.7 35.0
8	9.41 675	47	9.43 208	50	0.56 792	9.98 467	3	52	.8 40.8 40.0
9	9.41 722	46	9.43 258	50	0.56 742	9.98 464	4	51	.9 45.9 45.0
10	9.41 768	47	9.43 308	50	0.56 692	9.98 460		<b>50</b>	
11	9.41 815	47	9.43 358	50	0.56 642	9.98 457	3	49	.1 49 4.8
12	9.41 861	46	9.43 408	50	0.56 592	9.98 453	4	48	.2 9.8 9.6
13	9.41 908	47	9.43 458	50	0.56 542	9.98 450	3	47	.3 14.7 14.4
14	9.41 954	46	9.43 508	50	0.56 492	9.98 447	4	46	.4 19.6 19.2
15	9.42 001	46	9.43 558	49	0.56 442	9.98 443	3	45	.5 24.5 24.0
16	9.42 047	46	9.43 607	50	0.56 393	9.98 440	3	44	.6 29.4 28.8
17	9.42 093	47	9.43 657	50	0.56 343	9.98 436	4	43	.7 34.3 33.6
18	9.42 140	46	9.43 707	49	0.56 293	9.98 433	3	42	.8 39.2 38.4
19	9.42 186	46	9.43 756	50	0.56 244	9.98 429	4	41	.9 44.1 43.2
20	9.42 232	46	9.43 806	50	0.56 194	9.98 426	3	<b>40</b>	
21	9.42 278	46	9.43 855	50	0.56 145	9.98 422	4	39	.1 4.7 4.6
22	9.42 324	46	9.43 905	49	0.56 095	9.98 419	3	38	.2 9.4 9.2
23	9.42 370	46	9.43 954	50	0.56 046	9.98 415	4	37	.3 14.1 13.8
24	9.42 416	45	9.44 004	49	0.55 996	9.98 412	3	36	.4 18.8 18.4
25	9.42 461	46	9.44 053	49	0.55 947	9.98 409	4		.5 23.5 23.0
26	9.42 507	46	9.44 102	49	0.55 898	9.98 405	3	34	.6 28.2 27.6
27	9.42 553	46	9.44 151	50	0.55 849	9.98 402	4	33	.7 32.9 32.2
28	9.42 599	46	9.44 201	49	0.55 799	9.98 398	3	32	.8 37.6 36.8
29	9.42 644	46	9.44 250	49	0.55 750	9.98 395	3	31	.9 42.3 41.4
30	9.42 690	45	9.44 299	49	0.55 701	9.98 391	4	<b>30</b>	
31	9.42 735	46	9.44 348	49	0.55 652	9.98 388	3	29	.1 4.7 4.6
32	9.42 781	45	9.44 397	49	0.55 603	9.98 384	4	28	.2 9.4 9.2
33	9.42 826	46	9.44 446	49	0.55 554	9.98 381	3	27	.3 14.1 13.8
34	9.42 872	45	9.44 495	49	0.55 505	9.98 377	4	26	.4 18.8 18.4
35	9.42 917	45	9.44 544	48	0.55 456	9.98 373	3	25	.5 23.5 23.0
36	9.42 962	46	9.44 592	49	0.55 408	9.98 370	3	24	.6 28.2 27.6
37	9.43 008	45	9.44 641	49	0.55 359	9.98 366	4	23	.7 32.9 32.2
38	9.43 053	45	9.44 690	49	0.55 310	9.98 363	3	22	.8 37.6 36.8
39	9.43 098	45	9.44 738	49	0.55 262	9.98 359	3	21	.9 42.3 41.4
40	9.43 143	45	9.44 787	49	0.55 213	9.98 356	4	<b>20</b>	
41	9.43 188	45	9.44 836	48	0.55 164	9.98 352	4	19	.1 13.5 13.2
42	9.43 233	45	9.44 884	48	0.55 116	9.98 349	3	18	.2 18.0 17.6
43	9.43 278	45	9.44 933	48	0.55 067	9.98 345	4	17	.3 22.5 22.0
44	9.43 323	44	9.44 981	48	0.55 019	9.98 342	3	16	.4 27.0 26.4
45	9.43 367	45	9.45 029	49	0.54 971	9.98 338	4	15	.5 31.5 30.8
46	9.43 412	45	9.45 078	49	0.54 922	9.98 334	4	14	.6 36.0 35.2
47	9.43 457	45	9.45 126	48	0.54 874	9.98 331	3	13	.7 40.5 39.6
48	9.43 502	45	9.45 174	48	0.54 826	9.98 327	4	12	
49	9.43 546	44	9.45 222	48	0.54 778	9.98 324	3	11	.1 4 3
50	9.43 591	45	9.45 271	48	0.54 729	9.98 320	4	<b>10</b>	.2 0.4 0.3
51	9.43 635	44	9.45 319	48	0.54 681	9.98 317	3	9	.3 0.8 0.6
52	9.43 680	45	9.45 367	48	0.54 633	9.98 313	4	8	.4 1.2 0.9
53	9.43 724	44	9.45 415	48	0.54 585	9.98 309	4	7	.5 1.6 1.2
54	9.43 769	45	9.45 463	48	0.54 537	9.98 306	3	6	.6 2.0 1.5
55	9.43 813	44	9.45 511	48	0.54 489	9.98 302	4	5	.7 2.4 1.8
56	9.43 857	44	9.45 559	47	0.54 441	9.98 299	3	4	.8 2.8 2.1
57	9.43 901	44	9.45 606	47	0.54 394	9.98 295	4	3	.9 3.2 2.4
58	9.43 946	45	9.45 654	48	0.54 346	9.98 291	4	2	
59	9.43 990	44	9.45 702	48	0.54 298	9.98 288	3	1	.9 3.6 2.7
60	9.44 034	44	9.45 750	48	0.54 250	9.98 284	4	<b>0</b>	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	,	Prop. Pts.

TABLE IV.

16°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.44 034	44	9.45 750	47	0.54 250	9.98 284	3	60	
1	9.44 078	44	9.45 797	48	0.54 203	9.98 281	4	59	
2	9.44 122	44	9.45 845	47	0.54 155	9.98 277	4	58	
3	9.44 166	44	9.45 892	48	0.54 108	9.98 273	4	57	
4	9.44 210	44	9.45 940	47	0.54 060	9.98 270	3	56	.1 48 47
5	9.44 253	43	9.45 987	48	0.54 013	9.98 266	4	55	.2 9.6 9.4
6	9.44 297	44	9.46 035	47	0.53 965	9.98 262	4	54	.3 14.4 14.1
7	9.44 341	44	9.46 082	48	0.53 918	9.98 259	3	53	.4 19.2 18.8
8	9.44 385	43	9.46 130	47	0.53 870	9.98 255	4	52	.5 24.0 23.5
9	9.44 428	43	9.46 177	47	0.53 823	9.98 251	4	51	.6 28.8 28.2
10	9.44 472	44	9.46 224	47	0.53 776	9.98 248	3	50	.7 33.6 32.9
11	9.44 516	44	9.46 271	48	0.53 729	9.98 244	4	49	.8 38.4 37.6
12	9.44 559	43	9.46 319	47	0.53 681	9.98 240	4	48	.9 43.2 42.3
13	9.44 602	43	9.46 366	47	0.53 634	9.98 237	3	47	
14	9.44 646	44	9.46 413	47	0.53 587	9.98 233	4	46	
15	9.44 689	44	9.46 460	47	0.53 540	9.98 229	4	45	.1 4.6 4.5
16	9.44 733	43	9.46 507	47	0.53 493	9.98 226	3	44	.2 9.2 9.0
17	9.44 776	43	9.46 554	47	0.53 446	9.98 222	4	43	.3 13.8 13.5
18	9.44 819	43	9.46 601	47	0.53 399	9.98 218	4	42	.4 18.4 18.0
19	9.44 862	43	9.46 648	47	0.53 352	9.98 215	3	41	.5 23.0 22.5
20	9.44 905	43	9.46 694	47	0.53 306	9.98 211	4	40	.6 27.6 27.0
21	9.44 948	43	9.46 741	47	0.53 259	9.98 207	4	39	.7 32.2 31.5
22	9.44 992	44	9.46 788	47	0.53 212	9.98 204	3	38	.8 36.8 36.0
23	9.45 035	43	9.46 835	47	0.53 165	9.98 200	4	37	.9 41.4 40.5
24	9.45 077	43	9.46 881	47	0.53 119	9.98 196	4	36	
25	9.45 120	43	9.46 928	47	0.53 072	9.98 192	3	35	
26	9.45 163	43	9.46 975	46	0.53 025	9.98 189	3	34	.1 4.4 4.3
27	9.45 206	43	9.47 021	47	0.52 979	9.98 185	4	33	.2 8.8 8.6
28	9.45 249	43	9.47 068	47	0.52 932	9.98 181	4	32	.3 13.2 12.9
29	9.45 292	43	9.47 114	46	0.52 886	9.98 177	3	31	
30	9.45 334	43	9.47 160	47	0.52 840	9.98 174	4	30	.4 17.6 17.2
31	9.45 377	43	9.47 207	46	0.52 793	9.98 170	4	29	.5 22.0 21.5
32	9.45 419	42	9.47 253	46	0.52 747	9.98 166	4	28	.6 26.4 25.8
33	9.45 462	43	9.47 299	47	0.52 701	9.98 162	4	27	.7 30.8 30.1
34	9.45 504	43	9.47 346	46	0.52 654	9.98 159	3	26	.8 35.2 34.4
35	9.45 547	42	9.47 392	46	0.52 608	9.98 155	4	25	.9 39.6 38.7
36	9.45 589	42	9.47 438	46	0.52 562	9.98 151	4	24	
37	9.45 632	43	9.47 484	46	0.52 516	9.98 147	4	23	
38	9.45 674	42	9.47 530	46	0.52 470	9.98 144	3	22	
39	9.45 716	42	9.47 576	46	0.52 424	9.98 140	4	21	
40	9.45 758	42	9.47 622	46	0.52 378	9.98 136	4	20	
41	9.45 801	43	9.47 668	46	0.52 332	9.98 132	4	19	.1 4.2 4.1
42	9.45 843	42	9.47 714	46	0.52 286	9.98 129	3	18	.2 8.4 8.2
43	9.45 885	42	9.47 760	46	0.52 240	9.98 125	4	17	.3 12.6 12.3
44	9.45 927	42	9.47 806	46	0.52 194	9.98 121	4	16	.4 16.8 16.4
45	9.45 969	42	9.47 852	45	0.52 148	9.98 117	4	15	.5 21.0 20.5
46	9.46 011	42	9.47 897	45	0.52 103	9.98 113	4	14	.6 25.2 24.6
47	9.46 053	42	9.47 943	46	0.52 057	9.98 110	3	13	.7 29.4 28.7
48	9.46 095	42	9.47 989	46	0.52 011	9.98 106	4	12	.8 33.6 32.8
49	9.46 136	41	9.48 035	45	0.51 965	9.98 102	4	11	.9 37.8 36.9
50	9.46 178	42	9.48 080	45	0.51 920	9.98 098	4	10	.1 0.4 0.3
51	9.46 220	42	9.48 126	46	0.51 874	9.98 094	4	9	.2 0.8 0.6
52	9.46 262	42	9.48 171	45	0.51 829	9.98 090	4	8	.3 1.2 0.9
53	9.46 303	41	9.48 217	46	0.51 783	9.98 087	3	7	.4 1.6 1.2
54	9.46 345	42	9.48 262	45	0.51 738	9.98 083	4	6	.5 2.0 1.5
55	9.46 386	42	9.48 307	46	0.51 693	9.98 079	4	5	.6 2.4 1.8
56	9.46 428	42	9.48 353	46	0.51 647	9.98 075	4	4	.7 2.8 2.1
57	9.46 469	41	9.48 398	45	0.51 602	9.98 071	4	3	.8 3.2 2.4
58	9.46 511	42	9.48 443	45	0.51 557	9.98 067	4	2	.9 3.6 2.7
59	9.46 552	41	9.48 489	46	0.51 511	9.98 063	4	1	
60	9.46 594	42	9.48 534	45	0.51 466	9.98 060	3	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.		Prop. Pts.

## 17°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.46 594		9.48 534	45	0.51 466	9.98 060	4	60	
1	9.46 635	41	9.48 579	45	0.51 421	9.98 056	4	59	.1 45 4.4
2	9.46 676	41	9.48 624	45	0.51 376	9.98 052	4	58	.2 9.0 8.8
3	9.46 717	41	9.48 669	45	0.51 331	9.98 048	4	57	.3 13.5 13.2
4	9.46 758	42	9.48 714	45	0.51 286	9.98 044	4	56	.4 18.0 17.6
5	9.46 800	41	9.48 759	45	0.51 241	9.98 040	4	55	.5 22.5 22.0
6	9.46 841	41	9.48 804	45	0.51 196	9.98 036	4	54	.6 27.0 26.4
7	9.46 882	41	9.48 849	45	0.51 151	9.98 032	3	53	.7 31.5 30.8
8	9.46 923	41	9.48 894	45	0.51 106	9.98 029	4	52	.8 36.0 35.2
9	9.46 964	41	9.48 939	45	0.51 061	9.98 025	4	51	.9 40.5 39.6
10	9.47 005	40	9.48 984	45	0.51 016	9.98 021	4	50	
11	9.47 045	41	9.49 029	45	0.50 971	9.98 017	4	49	
12	9.47 086	41	9.49 073	45	0.50 927	9.98 013	4	48	
13	9.47 127	41	9.49 118	45	0.50 882	9.98 009	4	47	
14	9.47 168	41	9.49 163	45	0.50 837	9.98 005	4	46	
15	9.47 209	40	9.49 207	45	0.50 793	9.98 001	4	45	.1 4.3 4.2
16	9.47 249	40	9.49 252	45	0.50 748	9.97 997	4	44	.2 8.0 8.4
17	9.47 290	41	9.49 296	45	0.50 704	9.97 993	4	43	.3 12.9 12.6
18	9.47 330	40	9.49 341	45	0.50 659	9.97 989	4	42	.4 17.2 16.8
19	9.47 371	40	9.49 385	45	0.50 615	9.97 986	3	41	.5 21.5 21.0
20	9.47 411	41	9.49 430	45	0.50 570	9.97 982	4	40	.6 25.8 25.2
21	9.47 452	40	9.49 474	45	0.50 526	9.97 978	4	39	.7 30.1 29.4
22	9.47 492	40	9.49 519	45	0.50 481	9.97 974	4	38	.8 34.4 33.6
23	9.47 533	40	9.49 563	45	0.50 437	9.97 970	4	37	.9 38.7 37.8
24	9.47 573	40	9.49 607	45	0.50 393	9.97 966	4	36	
25	9.47 613	41	9.49 652	45	0.50 348	9.97 962	4	35	
26	9.47 654	41	9.49 696	44	0.50 304	9.97 958	4	34	.1 4.1 4.0
27	9.47 694	40	9.49 740	44	0.50 260	9.97 954	4	33	.2 8.2 8.0
28	9.47 734	40	9.49 784	44	0.50 216	9.97 950	4	32	
29	9.47 774	40	9.49 828	44	0.50 172	9.97 946	4	31	.3 12.3 12.0
30	9.47 814	40	9.49 872	44	0.50 128	9.97 942	4	30	.4 16.4 16.0
31	9.47 854	40	9.49 916	44	0.50 084	9.97 938	4	29	.5 20.5 20.0
32	9.47 894	40	9.49 960	44	0.50 040	9.97 934	4	28	.6 24.6 24.0
33	9.47 934	40	9.50 004	44	0.49 996	9.97 930	4	27	.7 28.7 28.0
34	9.47 974	40	9.50 048	44	0.49 952	9.97 926	4	26	.8 32.8 32.0
35	9.48 014	40	9.50 092	44	0.49 908	9.97 922	4	25	.9 36.9 36.0
36	9.48 054	40	9.50 136	44	0.49 864	9.97 918	4	24	
37	9.48 094	40	9.50 180	44	0.49 820	9.97 914	4	23	
38	9.48 133	39	9.50 223	43	0.49 777	9.97 910	4	22	
39	9.48 173	40	9.50 267	44	0.49 733	9.97 906	4	21	.1 3.9 0.5
40	9.48 213	39	9.50 311	44	0.49 689	9.97 902	4	20	.2 7.8 1.0
41	9.48 252	39	9.50 355	44	0.49 645	9.97 898	4	19	.3 11.7 1.5
42	9.48 292	40	9.50 398	43	0.49 602	9.97 894	4	18	.4 15.6 2.0
43	9.48 332	40	9.50 442	44	0.49 558	9.97 890	4	17	.5 19.5 2.5
44	9.48 371	39	9.50 485	43	0.49 515	9.97 886	4	16	.6 23.4 3.0
45	9.48 411	39	9.50 529	43	0.49 471	9.97 882	4	15	.7 27.3 3.5
46	9.48 450	39	9.50 572	43	0.49 428	9.97 878	4	14	.8 31.2 4.0
47	9.48 490	40	9.50 616	44	0.49 384	9.97 874	4	13	.9 35.1 4.5
48	9.48 529	39	9.50 659	43	0.49 341	9.97 870	4	12	
49	9.48 568	39	9.50 703	44	0.49 297	9.97 866	4	11	
50	9.48 607	39	9.50 746	43	0.49 254	9.97 861	5	10	.1 0.4 0.3
51	9.48 647	40	9.50 789	43	0.49 211	9.97 857	4	9	.2 0.8 0.6
52	9.48 686	39	9.50 833	44	0.49 167	9.97 853	4	8	.3 1.2 0.9
53	9.48 725	39	9.50 876	43	0.49 124	9.97 849	4	7	.4 1.6 1.2
54	9.48 764	39	9.50 919	43	0.49 081	9.97 845	4	6	.5 2.0 1.5
55	9.48 803	39	9.50 962	43	0.49 038	9.97 841	5	5	.6 2.4 1.8
56	9.48 842	39	9.51 005	43	0.48 995	9.97 837	4	4	.7 2.8 2.1
57	9.48 881	39	9.51 048	43	0.48 952	9.97 833	4	3	.8 3.2 2.4
58	9.48 920	39	9.51 092	44	0.48 908	9.97 829	4	2	.9 3.6 2.7
59	9.48 959	39	9.51 135	43	0.48 865	9.97 825	4	1	
60	9.48 998	39	9.51 178	43	0.48 822	9.97 821	0		
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	d.		Prop. Pts.

18°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.	60	Prop. Pts.
<b>0</b>	9.48 998	39	9.51 178	43	0.48 822	9.97 821	4	<b>60</b>	
<b>1</b>	9.49 037	39	9.51 221	43	0.48 779	9.97 817	5	59	
<b>2</b>	9.49 076	39	9.51 264	42	0.48 736	9.97 812	4	58	
<b>3</b>	9.49 115	38	9.51 306	43	0.48 694	9.97 808	4	57	.1 43 4.2
<b>4</b>	9.49 153	39	9.51 349	43	0.48 651	9.97 804	4	56	.2 8.6 8.4
<b>5</b>	9.49 192	39	9.51 392	43	0.48 608	9.97 800	4	55	.3 12.9 12.6
<b>6</b>	9.49 231	38	9.51 435	43	0.48 565	9.97 796	4	54	.4 17.2 16.8
<b>7</b>	9.49 269	39	9.51 478	42	0.48 522	9.97 792	4	53	.5 21.5 21.0
<b>8</b>	9.49 308	39	9.51 520	43	0.48 480	9.97 788	4	52	.6 25.8 25.2
<b>9</b>	9.49 347	39	9.51 563	43	0.48 437	9.97 784	4	51	.7 30.1 29.4
<b>10</b>	9.49 385	39	9.51 606	42	0.48 394	9.97 779	5	<b>50</b>	.8 34.4 33.6
<b>11</b>	9.49 424	38	9.51 648	43	0.48 352	9.97 775	4	49	.9 38.7 37.8
<b>12</b>	9.49 462	38	9.51 691	43	0.48 309	9.97 771	4	48	
<b>13</b>	9.49 500	39	9.51 734	42	0.48 266	9.97 767	4	47	
<b>14</b>	9.49 539	38	9.51 776	43	0.48 224	9.97 763	4	46	
<b>15</b>	9.49 577	38	9.51 819	42	0.48 181	9.97 759	5	45	.1 4.1
<b>16</b>	9.49 615	39	9.51 861	42	0.48 139	9.97 754	4	44	.2 8 2
<b>17</b>	9.49 654	38	9.51 903	43	0.48 097	9.97 750	4	43	.3 12.3
<b>18</b>	9.49 692	38	9.51 946	42	0.48 054	9.97 746	4	42	.4 16.4
<b>19</b>	9.49 730	38	9.51 988	43	0.48 012	9.97 742	4	41	.5 20.5
<b>20</b>	9.49 768	38	9.52 031	42	0.47 969	9.97 738	4	<b>40</b>	.6 24.6
<b>21</b>	9.49 806	38	9.52 073	42	0.47 927	9.97 734	4	39	.7 28.7
<b>22</b>	9.49 844	38	9.52 115	42	0.47 885	9.97 729	5	38	.8 32.8
<b>23</b>	9.49 882	38	9.52 157	43	0.47 843	9.97 725	4	37	.9 36.9
<b>24</b>	9.49 920	38	9.52 200	42	0.47 800	9.97 721	4	36	
<b>25</b>	9.49 958	38	9.52 242	42	0.47 758	9.97 717	4	35	
<b>26</b>	9.49 996	38	9.52 284	42	0.47 716	9.97 713	5	34	.1 39 3.8
<b>27</b>	9.50 034	38	9.52 326	42	0.47 674	9.97 708	4	33	.2 7.8
<b>28</b>	9.50 072	38	9.52 368	42	0.47 632	9.97 704	4	32	.3 12.3
<b>29</b>	9.50 110	38	9.52 410	42	0.47 590	9.97 700	4	31	.4 16.4
<b>30</b>	9.50 148	37	9.52 452	42	0.47 548	9.97 696	4	<b>30</b>	.5 20.5
<b>31</b>	9.50 185	38	9.52 494	42	0.47 506	9.97 691	5	29	.6 19.5 19.0
<b>32</b>	9.50 223	38	9.52 536	42	0.47 464	9.97 687	4	28	.7 23.4
<b>33</b>	9.50 261	38	9.52 578	42	0.47 422	9.97 683	4	27	.8 27.3
<b>34</b>	9.50 298	38	9.52 620	41	0.47 380	9.97 679	4	26	.9 31.2 30.4
<b>35</b>	9.50 336	38	9.52 661	42	0.47 339	9.97 674	5	25	
<b>36</b>	9.50 374	37	9.52 703	42	0.47 297	9.97 670	4	24	
<b>37</b>	9.50 411	38	9.52 745	42	0.47 255	9.97 666	4	23	
<b>38</b>	9.50 449	37	9.52 787	42	0.47 213	9.97 662	4	22	
<b>39</b>	9.50 486	37	9.52 829	42	0.47 171	9.97 657	5	21	.1 3.7 3.6
<b>40</b>	9.50 523	38	9.52 870	42	0.47 130	9.97 653	4	<b>20</b>	.2 7.4 7.2
<b>41</b>	9.50 561	37	9.52 912	42	0.47 088	9.97 649	4	19	.3 11.1 10.8
<b>42</b>	9.50 598	37	9.52 953	42	0.47 047	9.97 645	4	18	.4 14.8 14.4
<b>43</b>	9.50 635	38	9.52 995	42	0.47 005	9.97 640	5	17	.5 18.5 18.0
<b>44</b>	9.50 673	37	9.53 037	42	0.46 963	9.97 636	4	16	.6 22.2 21.6
<b>45</b>	9.50 710	37	9.53 078	42	0.46 922	9.97 632	4	15	.7 25.9 25.2
<b>46</b>	9.50 747	37	9.53 120	42	0.46 880	9.97 628	4	14	.8 29.6 28.8
<b>47</b>	9.50 784	37	9.53 161	42	0.46 839	9.97 623	5	13	.9 33.3 32.4
<b>48</b>	9.50 821	37	9.53 202	42	0.46 798	9.97 619	4	12	
<b>49</b>	9.50 858	37	9.53 244	42	0.46 756	9.97 615	4	11	
<b>50</b>	9.50 896	37	9.53 285	42	0.46 715	9.97 610	5	<b>10</b>	.5 5 4
<b>51</b>	9.50 933	37	9.53 327	42	0.46 673	9.97 606	4	9	.6 0.5 0.8
<b>52</b>	9.50 970	37	9.53 368	42	0.46 632	9.97 602	4	8	.7 1.5 1.2
<b>53</b>	9.51 007	37	9.53 409	42	0.46 591	9.97 597	5	7	.8 2.0 1.6
<b>54</b>	9.51 043	36	9.53 450	42	0.46 550	9.97 593	4	6	.9 2.5 2.0
<b>55</b>	9.51 080	37	9.53 492	42	0.46 508	9.97 589	4	5	.6 3.0 2.4
<b>56</b>	9.51 117	37	9.53 533	42	0.46 467	9.97 584	5	4	.7 3.5 2.8
<b>57</b>	9.51 154	37	9.53 574	42	0.46 426	9.97 580	4	3	.8 4.0 3.2
<b>58</b>	9.51 191	37	9.53 615	42	0.46 385	9.97 576	4	2	.9 4.5 3.6
<b>59</b>	9.51 227	36	9.53 656	42	0.46 344	9.97 571	5	1	
<b>60</b>	9.51 264	37	9.53 697	42	0.46 303	9.97 567	4	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.		Prop. Pts.

## 19°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.51 264	37	9.53 697	41	0.46 303	9.97 567	4	<b>60</b>	
1	9.51 301	37	9.53 738	41	0.46 262	9.97 563	5	59	
2	9.51 338	36	9.53 779	41	0.46 221	9.97 558	4	58	
3	9.51 374	37	9.53 820	41	0.46 180	9.97 554	4	57	
4	9.51 411	36	9.53 861	41	0.46 139	9.97 550	4	56	
5	9.51 447	37	9.53 902	41	0.46 098	9.97 545	5	55	.1 4x 40
6	9.51 484	36	9.53 943	41	0.46 057	9.97 541	4	54	.2 8.2 8.0
7	9.51 520	37	9.53 984	41	0.46 016	9.97 536	5	53	.3 12.3 12.0
8	9.51 557	36	9.54 025	41	0.45 975	9.97 532	4	52	.4 16.4 16.0
9	9.51 593	36	9.54 065	40	0.45 935	9.97 528	4	51	.5 20.5 20.0
10	9.51 629	37	9.54 106	41	0.45 894	9.97 523	5	<b>50</b>	.6 24.6 24.0
11	9.51 666	37	9.54 147	41	0.45 853	9.97 519	4	49	.7 28.7 28.0
12	9.51 702	36	9.54 187	41	0.45 813	9.97 515	5	48	.8 32.8 32.0
13	9.51 738	36	9.54 228	41	0.45 772	9.97 510	5	47	.9 36.9 36.0
14	9.51 774	37	9.54 269	40	0.45 731	9.97 506	4	46	
15	9.51 811	36	9.54 309	41	0.45 691	9.97 501	5	45	.1 3.9
16	9.51 847	36	9.54 350	40	0.45 650	9.97 497	4	44	.2 7.8
17	9.51 883	36	9.54 390	40	0.45 610	9.97 492	5	43	.3 11.7
18	9.51 919	36	9.54 431	41	0.45 569	9.97 488	4	42	.4 15.6
19	9.51 955	36	9.54 471	40	0.45 529	9.97 484	4	41	.5 19.5
20	9.51 991	36	9.54 512	41	0.45 488	9.97 479	5	<b>40</b>	.6 23.4
21	9.52 027	36	9.54 552	40	0.45 448	9.97 475	4	39	.7 27.3
22	9.52 063	36	9.54 593	41	0.45 407	9.97 470	5	38	.8 31.2
23	9.52 099	36	9.54 633	40	0.45 367	9.97 466	4	37	.9 35.1
24	9.52 135	36	9.54 673	41	0.45 327	9.97 461	5	36	
25	9.52 171	36	9.54 714	40	0.45 286	9.97 457	4	35	.1 37 36
26	9.52 207	35	9.54 754	40	0.45 246	9.97 453	4	34	.2 3.7 3.6
27	9.52 242	36	9.54 794	41	0.45 206	9.97 448	5	33	.3 7.4 7.2
28	9.52 278	36	9.54 835	40	0.45 165	9.97 444	4	32	.4 11.1 10.8
29	9.52 314	36	9.54 875	40	0.45 125	9.97 439	5	31	.5 14.8 14.4
30	9.52 350	35	9.54 915	40	0.45 085	9.97 435	4	<b>30</b>	.6 18.5 18.0
31	9.52 385	36	9.54 955	40	0.45 045	9.97 430	5	29	.7 22.2 21.6
32	9.52 421	35	9.54 995	40	0.45 005	9.97 426	4	28	.8 25.9 25.2
33	9.52 456	36	9.55 035	40	0.44 965	9.97 421	5	27	.9 29.6 28.8
34	9.52 492	35	9.55 075	40	0.44 925	9.97 417	4	26	.1 33.3 32.4
35	9.52 527	36	9.55 115	40	0.44 885	9.97 412	5	25	
36	9.52 563	35	9.55 155	40	0.44 845	9.97 408	4	24	.1 3.5 3.4
37	9.52 598	35	9.55 195	40	0.44 805	9.97 403	5	23	.2 7.0 6.8
38	9.52 634	36	9.55 235	40	0.44 765	9.97 399	4	22	.3 21.0 20.4
39	9.52 669	35	9.55 275	40	0.44 725	9.97 394	5	21	.4 24.5 23.8
40	9.52 705	35	9.55 315	40	0.44 685	9.97 390	4	<b>20</b>	.5 28.0 27.2
41	9.52 740	35	9.55 355	40	0.44 645	9.97 385	5	19	.6 31.5 30.6
42	9.52 775	35	9.55 395	39	0.44 605	9.97 381	4	18	.7 14.0 13.6
43	9.52 811	36	9.55 434	40	0.44 565	9.97 376	5	17	.8 17.5 17.0
44	9.52 846	35	9.55 474	40	0.44 526	9.97 372	4	16	.9 21.0 20.4
45	9.52 881	35	9.55 514	40	0.44 486	9.97 367	5	15	
46	9.52 916	35	9.55 554	39	0.44 446	9.97 363	4	14	.1 3.5 3.4
47	9.52 951	35	9.55 593	40	0.44 407	9.97 358	5	13	.2 7.0 6.8
48	9.52 986	35	9.55 633	40	0.44 367	9.97 353	5	12	.3 10.5 10.2
49	9.53 021	35	9.55 673	39	0.44 327	9.97 349	4	11	.4 14.0 13.6
50	9.53 056	36	9.55 712	40	0.44 288	9.97 344	5	<b>10</b>	.5 17.5 17.0
51	9.53 092	34	9.55 752	39	0.44 248	9.97 340	4	9	.6 21.0 20.4
52	9.53 126	35	9.55 791	40	0.44 209	9.97 335	5	8	.7 1.5 1.2
53	9.53 161	35	9.55 831	40	0.44 169	9.97 331	4	7	.8 2.0 1.6
54	9.53 196	35	9.55 870	39	0.44 130	9.97 326	5	6	.9 2.5 2.0
55	9.53 231	35	9.55 910	39	0.44 090	9.97 322	4	5	.6 3.0 2.4
56	9.53 266	35	9.55 949	40	0.44 051	9.97 317	5	4	.7 3.5 2.8
57	9.53 301	35	9.55 989	39	0.44 011	9.97 312	5	3	.8 4.0 3.2
58	9.53 336	34	9.56 028	39	0.43 972	9.97 308	4	2	.9 4.5 3.6
59	9.53 370	34	9.56 067	39	0.43 933	9.97 303	5	1	
60	9.53 405	35	9.56 107	40	0.43 893	9.97 299	4	0	
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	d.		Prop. Pts.

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20°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.53 405	35	9.56 107	39	0.43 803	9.97 299	5	<b>60</b>	
1	9.53 440	35	9.56 146	39	0.43 854	9.97 294	5	59	.1 4.0 3.9
2	9.53 475	34	9.56 185	39	0.43 815	9.97 289	4	58	.2 8.0 7.8
3	9.53 509	35	9.56 224	40	0.43 776	9.97 285	5	57	.3 12.0 11.7
4	9.53 544	34	9.56 264	39	0.43 736	9.97 280	4	56	.4 16.0 15.6
5	9.53 578	35	9.56 303	39	0.43 697	9.97 276	5	55	.5 20.0 19.5
6	9.53 613	34	9.56 342	39	0.43 658	9.97 271	5	54	.6 24.0 23.4
7	9.53 647	35	9.56 381	39	0.43 619	9.97 266	4	53	.7 28.0 27.3
8	9.53 682	34	9.56 420	39	0.43 580	9.97 262	5	52	.8 32.0 31.2
9	9.53 716	35	9.56 459	39	0.43 541	9.97 257	5	51	.9 36.0 35.1
10	9.53 751	34	9.56 498	39	0.43 502	9.97 252	4	<b>50</b>	
11	9.53 785	34	9.56 537	39	0.43 463	9.97 248	5	49	.1 3.8 3.7
12	9.53 819	35	9.56 576	39	0.43 424	9.97 243	5	48	.2 7.6 7.4
13	9.53 854	34	9.56 615	39	0.43 385	9.97 238	4	47	.3 11.4 11.1
14	9.53 888	34	9.56 654	39	0.43 340	9.97 234	5	46	.4 15.2 14.8
15	9.53 922	35	9.56 693	39	0.43 307	9.97 229	5	45	.5 19.0 18.5
16	9.53 957	34	9.56 732	39	0.43 268	9.97 224	4	44	.6 22.8 22.2
17	9.53 991	34	9.56 771	39	0.43 229	9.97 220	5	43	.7 26.6 25.9
18	9.54 025	34	9.56 810	39	0.43 190	9.97 215	5	42	.8 30.4 29.6
19	9.54 059	34	9.56 849	38	0.43 151	9.97 210	4	41	.9 34.2 33.3
20	9.54 093	34	9.56 887	39	0.43 113	9.97 206	4	<b>40</b>	
21	9.54 127	34	9.56 926	39	0.43 074	9.97 201	5	39	.1 3.5
22	9.54 161	34	9.56 965	39	0.43 035	9.97 196	5	38	.2 7.0
23	9.54 195	34	9.57 004	39	0.42 996	9.97 192	4	37	.3 10.5
24	9.54 229	34	9.57 042	39	0.42 958	9.97 187	5	36	.4 14.0
25	9.54 263	34	9.57 081	39	0.42 919	9.97 182	4	35	.5 17.5
26	9.54 297	34	9.57 120	38	0.42 880	9.97 178	5	34	.6 21.0
27	9.54 331	34	9.57 158	39	0.42 842	9.97 173	5	33	.7 24.5
28	9.54 365	34	9.57 197	38	0.42 803	9.97 168	5	32	.8 28.0
29	9.54 399	34	9.57 235	39	0.42 765	9.97 163	5	31	.9 31.5
30	9.54 433	33	9.57 274	38	0.42 726	9.97 159	4	<b>30</b>	
31	9.54 466	33	9.57 312	39	0.42 688	9.97 154	5	29	.1 3.3
32	9.54 500	34	9.57 351	38	0.42 649	9.97 149	5	28	.2 6.8
33	9.54 534	34	9.57 389	39	0.42 611	9.97 145	4	27	.3 10.5
34	9.54 567	34	9.57 428	38	0.42 572	9.97 140	5	26	.4 14.0
35	9.54 601	34	9.57 466	38	0.42 534	9.97 135	5	25	.5 17.5
36	9.54 635	33	9.57 504	39	0.42 496	9.97 130	5	24	.6 21.0
37	9.54 668	33	9.57 543	38	0.42 457	9.97 126	4	23	.7 24.5
38	9.54 702	33	9.57 581	38	0.42 419	9.97 121	5	22	.8 28.0
39	9.54 735	34	9.57 619	39	0.42 381	9.97 116	5	21	.9 31.5
40	9.54 769	33	9.57 658	38	0.42 342	9.97 111	4	<b>20</b>	
41	9.54 802	33	9.57 696	38	0.42 304	9.97 107	4	19	.1 10.2
42	9.54 836	34	9.57 734	38	0.42 266	9.97 102	5	18	.2 13.6
43	9.54 869	33	9.57 772	38	0.42 228	9.97 097	5	17	.3 17.0
44	9.54 903	33	9.57 810	39	0.42 190	9.97 092	5	16	.4 20.4
45	9.54 936	33	9.57 849	39	0.42 151	9.97 087	5	15	.5 23.8
46	9.54 969	33	9.57 887	38	0.42 113	9.97 083	4	14	.6 27.2
47	9.55 003	34	9.57 925	38	0.42 075	9.97 078	5	13	.7 30.6
48	9.55 036	33	9.57 963	38	0.42 037	9.97 073	5	12	.8 34.0
49	9.55 069	33	9.58 001	38	0.41 999	9.97 068	5	11	.9 37.4
50	9.55 102	34	9.58 039	38	0.41 961	9.97 063	5	<b>10</b>	
51	9.55 136	33	9.58 077	38	0.41 923	9.97 059	4	9	.1 0.5
52	9.55 169	33	9.58 115	38	0.41 885	9.97 054	5	8	.2 1.0
53	9.55 202	33	9.58 153	38	0.41 847	9.97 049	5	7	.3 1.5
54	9.55 235	33	9.58 191	38	0.41 809	9.97 044	5	6	.4 2.0
55	9.55 268	33	9.58 229	38	0.41 771	9.97 039	5	5	.5 2.5
56	9.55 301	33	9.58 267	37	0.41 733	9.97 035	4	4	.6 3.0
57	9.55 334	33	9.58 304	37	0.41 696	9.97 030	5	3	.7 3.5
58	9.55 367	33	9.58 342	38	0.41 658	9.97 025	5	2	.8 4.0
59	9.55 400	33	9.58 380	38	0.41 620	9.97 020	5	1	.9 4.5
60	9.55 433	33	9.58 418	38	0.41 582	9.97 015	5	<b>0</b>	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	r	Prop. Pts.

21°

'	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.55 433	33	9.58 418	37	0.41 582	9.97 015	5	60	
1	9.55 466	33	9.58 455	38	0.41 545	9.97 010	5	59	
2	9.55 499	33	9.58 493	38	0.41 507	9.97 005	4	58	
3	9.55 532	33	9.58 531	38	0.41 469	9.97 001	5	57	.1 38 3.7
4	9.55 564	33	9.58 569	37	0.41 431	9.96 996	5	56	.2 7.6 7.4
5	9.55 597	33	9.58 606	38	0.41 394	9.96 991	5	55	.3 11.4 11.1
6	9.55 630	33	9.58 644	37	0.41 356	9.96 986	5	54	.4 15.2 14.8
7	9.55 663	33	9.58 681	38	0.41 319	9.96 981	5	53	.5 19.0 18.5
8	9.55 695	33	9.58 719	38	0.41 281	9.96 976	5	52	.6 22.8 22.2
9	9.55 728	33	9.58 757	37	0.41 243	9.96 971	5	51	.7 26.6 25.9
10	9.55 761	32	9.58 794	38	0.41 206	9.96 966	4	50	.8 30.4 29.6
11	9.55 793	32	9.58 832	37	0.41 168	9.96 962	5	49	.9 34.2 33.3
12	9.55 826	32	9.58 869	38	0.41 131	9.96 957	5	48	
13	9.55 858	32	9.58 907	37	0.41 093	9.96 952	5	47	
14	9.55 891	32	9.58 944	37	0.41 056	9.96 947	5	46	36 33
15	9.55 923	33	9.58 981	38	0.41 019	9.96 942	5	45	.1 3.6 3.3
16	9.55 956	33	9.59 019	37	0.40 981	9.96 937	5	44	.2 7.2 6.6
17	9.55 988	32	9.59 056	38	0.40 944	9.96 932	5	43	.3 10.8 9.9
18	9.56 021	33	9.59 094	37	0.40 906	9.96 927	5	42	.4 14.4 13.2
19	9.56 053	32	9.59 131	37	0.40 869	9.96 922	5	41	.5 18.0 16.5
20	9.56 085	32	9.59 168	37	0.40 832	9.96 917	5	40	.6 21.6 19.8
21	9.56 118	33	9.59 205	37	0.40 795	9.96 912	5	39	.7 25.2 23.1
22	9.56 150	32	9.59 243	38	0.40 757	9.96 907	5	38	.8 28.8 26.4
23	9.56 182	33	9.59 280	37	0.40 720	9.96 903	4	37	.9 32.4 29.7
24	9.56 215	33	9.59 317	37	0.40 683	9.96 898	5	36	
25	9.56 247	32	9.59 354	37	0.40 646	9.96 893	5	35	32
26	9.56 279	32	9.59 391	38	0.40 609	9.96 888	5	34	.1 3.2
27	9.56 311	32	9.59 429	37	0.40 571	9.96 883	5	33	.2 6.4
28	9.56 343	32	9.59 466	37	0.40 534	9.96 878	5	32	.3 9.6
29	9.56 375	33	9.59 503	37	0.40 497	9.96 873	5	31	.4 12.8
30	9.56 408	32	9.59 540	37	0.40 460	9.96 868	5	30	.5 16.0
31	9.56 440	32	9.59 577	37	0.40 423	9.96 863	5	29	.6 19.2
32	9.56 472	32	9.59 614	37	0.40 386	9.96 858	5	28	.7 22.4
33	9.56 504	32	9.59 651	37	0.40 349	9.96 853	5	27	.8 25.6
34	9.56 536	32	9.59 688	37	0.40 312	9.96 848	5	26	.9 28.8
35	9.56 568	31	9.59 725	37	0.40 275	9.96 843	5	25	
36	9.56 599	31	9.59 762	37	0.40 238	9.96 838	5	24	
37	9.56 631	32	9.59 799	37	0.40 201	9.96 833	5	23	
38	9.56 663	32	9.59 835	36	0.40 165	9.96 828	5	22	
39	9.56 695	32	9.59 872	37	0.40 128	9.96 823	5	21	
40	9.56 727	32	9.59 909	37	0.40 091	9.96 818	5	20	
41	9.56 759	31	9.59 946	37	0.40 054	9.96 813	5	19	.3 9.3 1.8
42	9.56 790	31	9.59 983	37	0.40 017	9.96 808	5	18	.4 12.4 2.4
43	9.56 822	32	9.60 019	36	0.39 981	9.96 803	5	17	.5 15.5 3.0
44	9.56 854	32	9.60 056	37	0.39 944	9.96 798	5	16	.6 18.6 3.6
45	9.56 886	32	9.60 093	37	0.39 907	9.96 793	5	15	.7 21.7 4.2
46	9.56 917	31	9.60 130	37	0.39 870	9.96 788	5	14	.8 24.8 4.8
47	9.56 949	32	9.60 166	36	0.39 834	9.96 783	5	13	.9 27.9 5.4
48	9.56 980	31	9.60 203	37	0.39 797	9.96 778	5	12	
49	9.57 012	32	9.60 240	37	0.39 760	9.96 772	6	11	
50	9.57 044	32	9.60 276	36	0.39 724	9.96 767	5	10	.1 0.5 0.4
51	9.57 075	31	9.60 313	36	0.39 687	9.96 762	5	9	.2 1.0 0.8
52	9.57 107	32	9.60 349	37	0.39 651	9.96 757	5	8	.3 1.5 1.2
53	9.57 138	31	9.60 386	37	0.39 614	9.96 752	5	7	.4 2.0 1.6
54	9.57 169	32	9.60 422	36	0.39 578	9.96 747	5	6	.5 2.5 2.0
55	9.57 201	32	9.60 459	37	0.39 541	9.96 742	5	5	.6 3.0 2.4
56	9.57 232	31	9.60 495	36	0.39 505	9.96 737	5	4	.7 3.5 2.8
57	9.57 264	32	9.60 532	37	0.39 468	9.96 732	5	3	.8 4.0 3.2
58	9.57 295	31	9.60 568	36	0.39 432	9.96 727	5	2	.9 4.5 3.6
59	9.57 326	31	9.60 605	37	0.39 395	9.96 722	5	1	
60	9.57 358	32	9.60 641	36	0.39 359	9.96 717	5	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

TABLE IV.

22°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.57 358	31	9.60 641	36	0.39 359	9.96 717	6	60	
1	9.57 389	31	9.60 677	37	0.39 323	9.96 711	5	59	.1 37 3.6
2	9.57 420	31	9.60 714	36	0.39 286	9.96 706	5	58	.2 7.4 7.2
3	9.57 451	31	9.60 750	36	0.39 250	9.96 701	5	57	.3 11.1 10.8
4	9.57 482	32	9.60 786	37	0.39 214	9.96 696	5	56	.4 14.8 14.4
5	9.57 514	31	9.60 823	36	0.39 177	9.96 691	5	55	.5 18.5 18.0
6	9.57 545	31	9.60 859	36	0.39 141	9.96 686	5	54	.6 22.2 21.6
7	9.57 576	31	9.60 895	36	0.39 105	9.96 681	5	53	.7 25.9 25.2
8	9.57 607	31	9.60 931	36	0.39 069	9.96 676	6	52	.8 29.6 28.8
9	9.57 638	31	9.60 967	37	0.39 033	9.96 670	5	51	.9 33.3 32.4
10	9.57 669	31	9.61 004	36	0.38 996	9.96 665	5	50	
11	9.57 700	31	9.61 040	36	0.38 960	9.96 660	5	49	I 3.5
12	9.57 731	31	9.61 076	36	0.38 924	9.96 655	5	48	.2 7.0
13	9.57 762	31	9.61 112	36	0.38 888	9.96 650	5	47	.3 10.5
14	9.57 793	31	9.61 148	36	0.38 852	9.96 645	5	46	.4 14.0
15	9.57 824	31	9.61 184	36	0.38 816	9.96 640	6	45	.5 17.5
16	9.57 855	31	9.61 220	36	0.38 780	9.96 634	5	44	.6 21.0
17	9.57 885	30	9.61 256	36	0.38 744	9.96 629	5	43	.7 24.5
18	9.57 916	31	9.61 292	36	0.38 708	9.96 624	5	42	.8 28.0
19	9.57 947	31	9.61 328	36	0.38 672	9.96 619	5	41	.9 31.5
20	9.57 978	30	9.61 364	36	0.38 636	9.96 614	6	40	
21	9.58 008	30	9.61 400	36	0.38 600	9.96 608	5	39	I 3.5
22	9.58 039	31	9.61 436	36	0.38 564	9.96 603	5	38	.2 7.0
23	9.58 070	31	9.61 472	36	0.38 528	9.96 598	5	37	.3 10.5
24	9.58 101	30	9.61 508	36	0.38 492	9.96 593	5	36	.4 14.0
25	9.58 131	31	9.61 544	35	0.38 456	9.96 588	6	35	.5 17.5
26	9.58 162	31	9.61 579	36	0.38 421	9.96 582	5	34	.6 21.0
27	9.58 192	30	9.61 615	36	0.38 385	9.96 577	5	33	.7 24.5
28	9.58 223	31	9.61 651	36	0.38 349	9.96 572	5	32	.8 28.0
29	9.58 253	30	9.61 687	36	0.38 313	9.96 567	5	31	.9 31.5
30	9.58 284	31	9.61 722	36	0.38 278	9.96 562	6	30	
31	9.58 314	30	9.61 758	36	0.38 242	9.96 556	6	29	I 3.5
32	9.58 345	31	9.61 794	36	0.38 206	9.96 551	5	28	.2 6.4
33	9.58 375	30	9.61 830	36	0.38 170	9.96 546	5	27	.3 9.6
34	9.58 406	31	9.61 865	36	0.38 135	9.96 541	6	26	.4 12.8
35	9.58 436	30	9.61 901	35	0.38 099	9.96 535	5	25	.5 16.0
36	9.58 467	31	9.61 936	36	0.38 064	9.96 530	5	24	.6 19.2
37	9.58 497	30	9.61 972	36	0.38 028	9.96 525	5	23	.7 22.4
38	9.58 527	30	9.62 008	36	0.37 992	9.96 520	6	22	.8 25.6
39	9.58 557	31	9.62 043	36	0.37 957	9.96 514	5	21	.9 28.8
40	9.58 588	30	9.62 079	35	0.37 921	9.96 509	6	20	
41	9.58 618	30	9.62 114	35	0.37 886	9.96 504	5	19	I 3.0
42	9.58 648	30	9.62 150	36	0.37 850	9.96 498	6	18	.2 6.0
43	9.58 678	30	9.62 185	35	0.37 815	9.96 493	5	17	.3 15.0
44	9.58 709	31	9.62 221	36	0.37 779	9.96 488	5	16	.4 18.0
45	9.58 739	30	9.62 256	35	0.37 744	9.96 483	5	15	.5 21.0
46	9.58 769	30	9.62 292	36	0.37 708	9.96 477	6	14	.6 24.0
47	9.58 799	30	9.62 327	35	0.37 673	9.96 472	5	13	.7 27.0
48	9.58 829	30	9.62 362	35	0.37 638	9.96 467	5	12	.8 20.3
49	9.58 859	30	9.62 398	36	0.37 602	9.96 461	6	11	.9 23.2
50	9.58 889	30	9.62 433	35	0.37 567	9.96 456	5	10	
51	9.58 919	30	9.62 468	35	0.37 532	9.96 451	5	9	I 0.6
52	9.58 949	30	9.62 504	36	0.37 496	9.96 445	6	8	.2 1.2
53	9.58 979	30	9.62 539	35	0.37 461	9.96 440	5	7	.3 1.5
54	9.59 009	30	9.62 574	35	0.37 426	9.96 435	6	6	.4 2.0
55	9.59 039	30	9.62 609	36	0.37 391	9.96 429	5	5	.5 3.0
56	9.59 069	30	9.62 645	35	0.37 355	9.96 424	4	4	.6 3.6
57	9.59 098	29	9.62 680	35	0.37 320	9.96 419	5	3	.7 4.2
58	9.59 128	30	9.62 715	35	0.37 285	9.96 413	6	2	.8 4.8
59	9.59 158	30	9.62 750	35	0.37 250	9.96 408	5	1	.9 5.4
60	9.59 188	30	9.62 785	35	0.37 215	9.96 403	5	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	,	Prop. Pts.

23°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.59 188	30	9.62 785	35	0.37 215	9.96 403	6	60	
1	9.59 218	29	9.62 820	35	0.37 180	9.96 397	5	59	.1 36 35
2	9.59 247	30	9.62 855	35	0.37 145	9.96 392	5	58	.2 7 2 7.0
3	9.59 277	30	9.62 890	36	0.37 110	9.96 387	6	57	.3 3.6 3.5
4	9.59 307	29	9.62 926	35	0.37 074	9.96 381	5	56	.4 2 7 2 7.0
5	9.59 336	30	9.62 961	35	0.37 039	9.96 376	6	55	.5 10.8 10.5
6	9.59 366	30	9.62 996	35	0.37 004	9.96 370	5	54	.6 14.4 14.0
7	9.59 396	29	9.63 031	35	0.36 969	9.96 365	5	53	.7 18.2 17.5
8	9.59 425	30	9.63 066	35	0.36 934	9.96 360	6	52	.8 21.6 21.0
9	9.59 455	29	9.63 101	34	0.36 899	9.96 354	5	51	.9 25.2 24.5
10	9.59 484	30	9.63 135	35	0.36 865	9.96 349	6	50	.0 28.8 28.0
11	9.59 514	29	9.63 170	35	0.36 830	9.96 343	5	49	.1 32.4 31.5
12	9.59 543	30	9.63 205	35	0.36 795	9.96 338	5	48	
13	9.59 573	29	9.63 240	35	0.36 760	9.96 333	6	47	
14	9.59 602	30	9.63 275	35	0.36 725	9.96 327	5	46	
15	9.59 632	29	9.63 310	35	0.36 690	9.96 322	6	45	.1 34
16	9.59 661	29	9.63 345	34	0.36 655	9.96 316	5	44	.2 6.8
17	9.59 690	30	9.63 379	35	0.36 621	9.96 311	6	43	.3 10.2
18	9.59 720	29	9.63 414	35	0.36 586	9.96 305	5	42	.4 13.6
19	9.59 749	29	9.63 449	35	0.36 551	9.96 300	6	41	.5 17.0
20	9.59 778	30	9.63 484	35	0.36 516	9.96 294	5	40	.6 20.4
21	9.59 808	29	9.63 519	34	0.36 481	9.96 289	5	39	.7 23.8
22	9.59 837	29	9.63 553	35	0.36 447	9.96 284	6	38	.8 27.2
23	9.59 866	29	9.63 588	35	0.36 412	9.96 278	5	37	.9 30.6
24	9.59 895	29	9.63 623	34	0.36 377	9.96 273	6	36	
25	9.59 924	30	9.63 657	35	0.36 342	9.96 267	5	35	
26	9.59 954	29	9.63 692	34	0.36 308	9.96 262	6	34	.1 30 29
27	9.59 983	29	9.63 726	35	0.36 274	9.96 256	5	33	.2 6.0 5.8
28	9.60 012	29	9.63 761	35	0.36 239	9.96 251	6	32	.3 9.0 8.7
29	9.60 041	29	9.63 796	34	0.36 204	9.96 245	5	31	
30	9.60 070	29	9.63 830	34	0.36 170	9.96 240	6	30	
31	9.60 099	29	9.63 865	35	0.36 135	9.96 234	5	29	.1 3.0 2.9
32	9.60 128	29	9.63 899	34	0.36 101	9.96 229	5	28	.2 6.0 5.8
33	9.60 157	29	9.63 934	35	0.36 066	9.96 223	6	27	.3 9.0 8.7
34	9.60 186	29	9.63 968	34	0.36 032	9.96 218	5	26	
35	9.60 215	29	9.64 003	35	0.35 997	9.96 212	6	25	
36	9.60 244	29	9.64 037	34	0.35 963	9.96 207	5	24	
37	9.60 273	29	9.64 072	35	0.35 928	9.96 201	6	23	
38	9.60 302	29	9.64 106	34	0.35 894	9.96 196	5	22	
39	9.60 331	28	9.64 140	34	0.35 860	9.96 190	6	21	
40	9.60 359	29	9.64 175	35	0.35 825	9.96 185	5	20	
41	9.60 388	29	9.64 209	34	0.35 791	9.96 179	6	19	.1 28
42	9.60 417	29	9.64 243	34	0.35 757	9.96 174	5	18	.2 8.4
43	9.60 446	29	9.64 278	34	0.35 722	9.96 168	6	17	.3 11.2
44	9.60 474	28	9.64 312	34	0.35 688	9.96 162	6	16	.4 14.0
45	9.60 503	29	9.64 346	34	0.35 654	9.96 157	5	15	.5 16.8
46	9.60 532	29	9.64 381	35	0.35 619	9.96 151	6	14	.6 19.6
47	9.60 561	29	9.64 415	34	0.35 585	9.96 146	5	13	.7 22.4
48	9.60 589	28	9.64 449	34	0.35 551	9.96 140	6	12	.8 25.2
49	9.60 618	29	9.64 483	34	0.35 517	9.96 135	5	11	
50	9.60 646	28	9.64 517	34	0.35 483	9.96 129	6	10	
51	9.60 675	29	9.64 552	35	0.35 448	9.96 123	6	9	.1 0.6 0.5
52	9.60 704	28	9.64 586	34	0.35 414	9.96 118	5	8	.2 1.2 1.0
53	9.60 732	28	9.64 620	34	0.35 380	9.96 112	6	7	.3 1.8 1.5
54	9.60 761	28	9.64 654	34	0.35 346	9.96 107	5	6	.4 2.4 2.0
55	9.60 789	28	9.64 688	34	0.35 312	9.96 101	6	5	.5 3.0 2.5
56	9.60 818	28	9.64 722	34	0.35 278	9.96 095	6	4	.6 3.6 3.0
57	9.60 846	28	9.64 756	34	0.35 244	9.96 090	5	3	.7 4.2 3.5
58	9.60 875	28	9.64 790	34	0.35 210	9.96 084	6	2	.8 4.8 4.0
59	9.60 903	28	9.64 824	34	0.35 176	9.96 079	5	1	.9 5.4 4.5
60	9.60 931	28	9.64 858	34	0.35 142	9.96 073	6	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

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TABLE IV.

24°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.60 931	29	9.64 858	34	0.35 142	9.96 073	6	60	
1	9.60 960	28	9.64 892	34	0.35 108	9.96 067	5	59	
2	9.60 988	28	9.64 926	34	0.35 074	9.96 062	6	58	
3	9.61 016	29	9.64 960	34	0.35 040	9.96 056	6	57	34 33
4	9.61 045	28	9.64 994	34	0.35 006	9.96 050	5	56	3.4 3.3
5	9.61 073	28	9.65 028	34	0.34 972	9.96 045	6	55	6.8 6.6
6	9.61 101	28	9.65 062	34	0.34 938	9.96 039	5	54	10.2 9.9
7	9.61 129	29	9.65 096	34	0.34 904	9.96 034	6	53	13.6 13.2
8	9.61 158	28	9.65 130	34	0.34 870	9.96 028	6	52	17.0 16.5
9	9.61 186	28	9.65 164	33	0.34 836	9.96 022	5	51	20.4 19.8
10	9.61 214	28	9.65 197	33	0.34 803	9.96 017	5	50	23.8 23.1
11	9.61 242	28	9.65 231	34	0.34 769	9.96 011	6	49	27.2 26.4
12	9.61 270	28	9.65 265	34	0.34 735	9.96 005	5	48	30.6 29.7
13	9.61 298	28	9.65 299	34	0.34 701	9.96 000	6	47	
14	9.61 326	28	9.65 333	33	0.34 667	9.95 994	6	46	29
15	9.61 354	28	9.65 366	34	0.34 634	9.95 988	6	45	1.1 2.9
16	9.61 382	29	9.65 400	34	0.34 600	9.95 982	5	44	2.2 5.8
17	9.61 411	27	9.65 434	33	0.34 566	9.95 977	6	43	3.3 8.7
18	9.61 438	28	9.65 467	34	0.34 533	9.95 971	6	42	4.4 11.6
19	9.61 466	28	9.65 501	34	0.34 499	9.95 965	5	41	5.5 14.5
20	9.61 494	28	9.65 535	33	0.34 465	9.95 960	6	40	6.6 17.4
21	9.61 522	28	9.65 568	34	0.34 432	9.95 954	6	39	7.7 20.3
22	9.61 550	28	9.65 602	34	0.34 398	9.95 948	6	38	8.8 23.2
23	9.61 578	28	9.65 636	34	0.34 364	9.95 942	5	37	9.9 26.1
24	9.61 606	28	9.65 669	34	0.34 331	9.95 937	6	36	
25	9.61 634	28	9.65 703	33	0.34 297	9.95 931	6	35	28
26	9.61 662	27	9.65 736	34	0.34 264	9.95 925	5	34	1.1 2.8
27	9.61 689	28	9.65 770	34	0.34 230	9.95 920	6	33	2.2 5.6
28	9.61 717	28	9.65 803	33	0.34 197	9.95 914	6	32	3.3 8.4
29	9.61 745	28	9.65 837	33	0.34 163	9.95 908	6	31	4.4 11.2
30	9.61 773	27	9.65 870	34	0.34 130	9.95 902	5	30	
31	9.61 800	28	9.65 904	34	0.34 096	9.95 897	6	29	.5 14.0
32	9.61 828	28	9.65 937	33	0.34 063	9.95 891	6	28	6 16.8
33	9.61 856	27	9.65 971	34	0.34 029	9.95 885	6	27	7 19.6
34	9.61 883	28	9.66 004	33	0.33 996	9.95 879	6	26	.8 22.4
35	9.61 911	28	9.66 038	33	0.33 962	9.95 873	6	25	
36	9.61 939	27	9.66 071	33	0.33 929	9.95 868	5	24	2.7
37	9.61 966	28	9.66 104	33	0.33 896	9.95 862	6	23	3.2 5.6
38	9.61 994	27	9.66 138	34	0.33 862	9.95 856	6	22	
39	9.62 021	28	9.66 171	33	0.33 829	9.95 850	6	21	.1 2.7
40	9.62 049	27	9.66 204	34	0.33 796	9.95 844	5	20	5.4 8.1
41	9.62 076	28	9.66 238	33	0.33 762	9.95 839	6	19	10.8
42	9.62 104	27	9.66 271	33	0.33 729	9.95 833	6	18	.5 13.5
43	9.62 131	28	9.66 304	33	0.33 696	9.95 827	6	17	6 16.2
44	9.62 159	27	9.66 337	34	0.33 663	9.95 821	6	16	.7 18.9
45	9.62 186	28	9.66 371	33	0.33 629	9.95 815	5	15	.8 21.6
46	9.62 214	27	9.66 404	33	0.33 596	9.95 810	6	14	.9 24.3
47	9.62 241	27	9.66 437	33	0.33 563	9.95 804	6	13	
48	9.62 268	27	9.66 470	33	0.33 530	9.95 798	6	12	
49	9.62 296	28	9.66 503	33	0.33 497	9.95 792	6	11	6 5
50	9.62 323	27	9.66 537	34	0.33 463	9.95 786	6	10	0.6 0.5
51	9.62 350	27	9.66 570	33	0.33 430	9.95 780	6	9	.2 1.2
52	9.62 377	28	9.66 603	33	0.33 397	9.95 775	5	8	.3 1.8
53	9.62 405	28	9.66 636	33	0.33 364	9.95 769	6	7	2.4 2.0
54	9.62 432	27	9.66 669	33	0.33 331	9.95 763	6	6	3.0 2.5
55	9.62 459	27	9.66 702	33	0.33 298	9.95 757	5	5	3.6 3.0
56	9.62 486	27	9.66 735	33	0.33 265	9.95 751	6	4	4.2 3.5
57	9.62 513	28	9.66 768	33	0.33 232	9.95 745	6	3	4.8 4.0
58	9.62 541	28	9.66 801	33	0.33 199	9.95 739	6	2	5 4.5
59	9.62 568	27	9.66 834	33	0.33 166	9.95 733	5	1	
60	9.62 595	27	9.66 867	33	0.33 133	9.95 728	5	0	
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

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25°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.
0	9.62 595	27	9.66 867	33	0.33 133	9.95 728	6	60	
1	9.62 622	27	9.66 900	33	0.33 100	9.95 722	6	59	
2	9.62 649	27	9.66 933	33	0.33 067	9.95 716	6	58	
3	9.62 676	27	9.66 966	33	0.33 034	9.95 710	6	57	
4	9.62 703	27	9.66 999	33	0.33 001	9.95 704	6	56	.1 3.3 3.2
5	9.62 730	27	9.67 032	33	0.32 968	9.95 698	6	55	.2 9.9 6.4
6	9.62 757	27	9.67 065	33	0.32 935	9.95 692	6	54	.3 13.2 12.8
7	9.62 784	27	9.67 098	33	0.32 902	9.95 686	6	53	.4 16.5 16.0
8	9.62 811	27	9.67 131	33	0.32 869	9.95 680	6	52	.5 19.8 19.2
9	9.62 838	27	9.67 163	33	0.32 837	9.95 674	6	51	.6 23.1 22.4
10	9.62 865	27	9.67 196	33	0.32 804	9.95 668	5	50	.7 26.4 25.6
11	9.62 892	26	9.67 229	33	0.32 771	9.95 663	6	49	.8 29.7 28.8
12	9.62 918	27	9.67 262	33	0.32 738	9.95 657	6	48	
13	9.62 945	27	9.67 295	33	0.32 705	9.95 651	6	47	
14	9.62 972	27	9.67 327	33	0.32 673	9.95 645	6	46	
15	9.62 999	27	9.67 360	33	0.32 640	9.95 639	6	45	.1 2.7
16	9.63 026	26	9.67 393	33	0.32 607	9.95 633	6	44	.2 5.4
17	9.63 052	27	9.67 426	33	0.32 574	9.95 627	6	43	.3 8.1
18	9.63 079	27	9.67 458	33	0.32 542	9.95 621	6	42	.4 10.8
19	9.63 106	27	9.67 491	33	0.32 509	9.95 615	6	41	.5 13.5
20	9.63 133	26	9.67 524	33	0.32 476	9.95 609	6	40	.6 16.2
21	9.63 159	27	9.67 556	32	0.32 444	9.95 603	6	39	
22	9.63 186	27	9.67 589	33	0.32 411	9.95 597	6	38	.8 21.6
23	9.63 213	26	9.67 622	33	0.32 378	9.95 591	6	37	.9 24.3
24	9.63 239	27	9.67 654	33	0.32 346	9.95 585	6	36	
25	9.63 266	26	9.67 687	32	0.32 313	9.95 579	6	35	
26	9.63 292	27	9.67 719	33	0.32 281	9.95 573	6	34	.1 2.6
27	9.63 319	26	9.67 752	33	0.32 248	9.95 567	6	33	.2 5.2
28	9.63 345	27	9.67 785	33	0.32 215	9.95 561	6	32	.3 7.8
29	9.63 372	26	9.67 817	33	0.32 183	9.95 555	6	31	.4 10.4
30	9.63 398	27	9.67 850	32	0.32 150	9.95 549	6	30	.5 13.0
31	9.63 425	26	9.67 882	33	0.32 118	9.95 543	6	29	.6 15.6
32	9.63 451	27	9.67 915	33	0.32 085	9.95 537	6	28	
33	9.63 478	26	9.67 947	33	0.32 053	9.95 531	6	27	.7 18.2
34	9.63 504	27	9.67 980	33	0.32 020	9.95 525	6	26	.8 20.8
35	9.63 531	26	9.68 012	32	0.31 988	9.95 519	6	25	.9 23.4
36	9.63 557	26	9.68 044	33	0.31 956	9.95 513	6	24	
37	9.63 583	27	9.68 077	33	0.31 923	9.95 507	7	23	.1 0.7
38	9.63 610	26	9.68 109	32	0.31 891	9.95 500	6	22	.2 1.4
39	9.63 636	26	9.68 142	33	0.31 858	9.95 494	6	21	.3 2.1
40	9.63 662	27	9.68 174	32	0.31 826	9.95 488	6	20	.4 2.8
41	9.63 689	26	9.68 206	33	0.31 794	9.95 482	6	19	.5 3.5
42	9.63 715	26	9.68 239	33	0.31 761	9.95 476	6	18	.6 4.2
43	9.63 741	26	9.68 271	32	0.31 729	9.95 470	6	17	
44	9.63 767	27	9.68 303	33	0.31 697	9.95 464	6	16	.7 4.9
45	9.63 794	26	9.68 336	32	0.31 664	9.95 458	6	15	.8 5.6
46	9.63 820	26	9.68 368	33	0.31 632	9.95 452	6	14	.9 6 3
47	9.63 846	26	9.68 400	32	0.31 600	9.95 446	6	13	
48	9.63 872	26	9.68 432	33	0.31 568	9.95 440	6	12	.1 0.6 0.5
49	9.63 898	26	9.68 465	33	0.31 535	9.95 434	7	10	.2 1.2 1.0
50	9.63 924	26	9.68 497	32	0.31 503	9.95 427	6	9	.3 1.8 1.5
51	9.63 950	26	9.68 529	32	0.31 471	9.95 421	6	8	.4 2.4 2.0
52	9.63 976	26	9.68 561	32	0.31 439	9.95 415	6	7	
53	9.64 002	26	9.68 593	32	0.31 407	9.95 409	6	6	.5 3.0 2.5
54	9.64 028	26	9.68 626	33	0.31 374	9.95 403	6	6	.6 3.6 3.0
55	9.64 054	26	9.68 658	32	0.31 342	9.95 397	6	5	
56	9.64 080	26	9.68 690	32	0.31 310	9.95 391	6	4	.7 4.2 3.5
57	9.64 106	26	9.68 722	32	0.31 278	9.95 384	7	3	.8 4.8 4.0
58	9.64 132	26	9.68 754	32	0.31 246	9.95 378	6	2	.9 5.4 4.5
59	9.64 158	26	9.68 786	32	0.31 214	9.95 372	6	1	
60	9.64 184	26	9.68 818	32	0.31 182	9.95 366	6	0	

L. Cos. d. L. Cotg. c. d. L. Tang. L. Sin. d. / Prop. Pts.

64°

TABLE IV.

26°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.64 184	26	9.68 818	32	0.31 182	9.95 366	6	<b>60</b>	
1	9.64 210	26	9.68 850	32	0.31 150	9.95 360	6	59	
2	9.64 236	26	9.68 882	32	0.31 118	9.95 354	6	58	
3	9.64 262	26	9.68 914	32	0.31 086	9.95 348	6	57	
4	9.64 288	25	9.68 946	32	0.31 054	9.95 341	7	56	
5	9.64 313	26	9.68 978	32	0.31 022	9.95 335	6	55	
6	9.64 339	26	9.69 010	32	0.30 990	9.95 329	6	54	
7	9.64 365	26	9.69 042	32	0.30 958	9.95 323	6	53	
8	9.64 391	26	9.69 074	32	0.30 926	9.95 317	7	52	
9	9.64 417	25	9.69 106.	32	0.30 894	9.95 310	7	51	
10	9.64 442	26	9.69 138	32	0.30 862	9.95 304	6	<b>50</b>	
11	9.64 468	26	9.69 170	32	0.30 830	9.95 298	6	49	
12	9.64 494	25	9.69 202	32	0.30 798	9.95 292	6	48	
13	9.64 519	26	9.69 234	32	0.30 766	9.95 286	7	47	
14	9.64 545	26	9.69 266	32	0.30 734	9.95 279	7	46	
15	9.64 571	25	9.69 298	32	0.30 702	9.95 273	6	45	
16	9.64 596	26	9.69 329	32	0.30 671	9.95 267	6	44	
17	9.64 622	25	9.69 361	32	0.30 639	9.95 261	7	43	
18	9.64 647	26	9.69 393	32	0.30 607	9.95 254	6	42	
19	9.64 673	25	9.69 425	32	0.30 575	9.95 248	6	41	
20	9.64 698	26	9.69 457	32	0.30 543	9.95 242	6	<b>40</b>	
21	9.64 724	25	9.69 488	32	0.30 512	9.95 236	7	39	
22	9.64 749	26	9.69 520	32	0.30 480	9.95 229	6	38	
23	9.64 775	25	9.69 552	32	0.30 448	9.95 223	6	37	
24	9.64 800	26	9.69 584	32	0.30 416	9.95 217	6	36	
25	9.64 826	25	9.69 615	32	0.30 385	9.95 211	7	35	
26	9.64 851	26	9.69 647	32	0.30 353	9.95 204	6	34	
27	9.64 877	25	9.69 679	32	0.30 321	9.95 198	6	33	
28	9.64 902	25	9.69 710	32	0.30 290	9.95 192	7	32	
29	9.64 927	26	9.69 742	32	0.30 258	9.95 185	6	31	
30	9.64 953	25	9.69 774	32	0.30 226	9.95 179	6	<b>30</b>	
31	9.64 978	25	9.69 805	32	0.30 195	9.95 173	6	29	
32	9.65 003	26	9.69 837	32	0.30 163	9.95 167	6	28	
33	9.65 029	25	9.69 868	32	0.30 132	9.95 160	7	27	
34	9.65 054	25	9.69 900	32	0.30 100	9.95 154	6	26	
35	9.65 079	25	9.69 932	32	0.30 068	9.95 148	7	25	
36	9.65 104	26	9.69 963	32	0.30 037	9.95 141	7	24	
37	9.65 130	25	9.69 995	32	0.30 005	9.95 135	6	23	
38	9.65 155	25	9.70 026	32	0.29 974	9.95 129	6	22	
39	9.65 180	25	9.70 058	32	0.29 942	9.95 122	7	21	
40	9.65 205	25	9.70 089	32	0.29 911	9.95 116	6	<b>20</b>	
41	9.65 230	25	9.70 121	32	0.29 879	9.95 110	7	19	
42	9.65 255	26	9.70 152	32	0.29 848	9.95 103	7	18	
43	9.65 281	26	9.70 184	32	0.29 816	9.95 097	6	17	
44	9.65 306	25	9.70 215	32	0.29 785	9.95 090	7	16	
45	9.65 331	25	9.70 247	32	0.29 753	9.95 084	6	15	
46	9.65 356	25	9.70 278	32	0.29 722	9.95 078	7	14	
47	9.65 381	25	9.70 309	32	0.29 691	9.95 071	7	13	
48	9.65 406	25	9.70 341	32	0.29 659	9.95 065	6	12	
49	9.65 431	25	9.70 372	32	0.29 628	9.95 059	7	11	
50	9.65 456	25	9.70 404	32	0.29 596	9.95 052	7	<b>10</b>	
51	9.65 481	25	9.70 435	32	0.29 565	9.95 046	6	9	
52	9.65 506	25	9.70 466	32	0.29 534	9.95 039	7	8	
53	9.65 531	25	9.70 498	32	0.29 502	9.95 033	6	7	
54	9.65 556	25	9.70 529	32	0.29 471	9.95 027	6	6	
55	9.65 580	25	9.70 560	32	0.29 440	9.95 020	7	5	
56	9.65 605	25	9.70 592	32	0.29 408	9.95 014	6	4	
57	9.65 630	25	9.70 623	31	0.29 377	9.95 007	7	3	
58	9.65 655	25	9.70 654	31	0.29 346	9.95 001	6	2	
59	9.65 680	25	9.70 685	32	0.29 315	9.94 995	7	1	
60	9.65 705	25	9.70 717	32	0.29 283	9.94 988	7	<b>0</b>	
	L. Cos.	d.	I. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

27°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.65 705	24	9.70 717	3 <sup>x</sup>	0.29 283	9.94 988	6	60	
1	9.65 729	25	9.70 748	3 <sup>x</sup>	0.29 252	9.94 982	5	59	
2	9.65 754	25	9.70 779	3 <sup>x</sup>	0.29 221	9.94 975	7	58	
3	9.65 779	25	9.70 810	3 <sup>x</sup>	0.29 190	9.94 969	6	57	
4	9.65 804	24	9.70 841	3 <sup>x</sup>	0.29 159	9.94 962	7	56	.1 3.2 3.1
5	9.65 828	25	9.70 873	3 <sup>x</sup>	0.29 127	9.94 956	7	55	.2 6.4 6.2
6	9.65 853	25	9.70 904	3 <sup>x</sup>	0.29 096	9.94 949	6	54	.3 9.6 9.3
7	9.65 878	25	9.70 935	3 <sup>x</sup>	0.29 065	9.94 943	7	53	.4 12.8 12.4
8	9.65 902	24	9.70 966	3 <sup>x</sup>	0.29 034	9.94 936	6	52	.5 16.0 15.5
9	9.65 927	25	9.70 997	3 <sup>x</sup>	0.29 003	9.94 930	7	51	.6 19.2 18.6
10	9.65 952	24	9.71 028	3 <sup>x</sup>	0.28 972	9.94 923	6	50	.7 22.4 21.7
11	9.65 976	25	9.71 059	3 <sup>x</sup>	0.28 941	9.94 917	6	49	.8 25.6 24.8
12	9.66 001	25	9.71 090	3 <sup>x</sup>	0.28 910	9.94 911	7	48	.9 28.8 27.9
13	9.66 025	24	9.71 121	3 <sup>x</sup>	0.28 879	9.94 904	7	47	
14	9.66 050	25	9.71 153	3 <sup>x</sup>	0.28 847	9.94 898	6	46	
15	9.66 075	24	9.71 184	3 <sup>x</sup>	0.28 816	9.94 891	7		.1 3.0
16	9.66 099	25	9.71 215	3 <sup>x</sup>	0.28 785	9.94 885	6	45	.2 6.0
17	9.66 124	24	9.71 246	3 <sup>x</sup>	0.28 754	9.94 878	7	44	.3 9.0
18	9.66 148	24	9.71 277	3 <sup>x</sup>	0.28 723	9.94 871	7	43	.4 12.0
19	9.66 173	25	9.71 308	3 <sup>x</sup>	0.28 692	9.94 865	6	42	.5 15.0
20	9.66 197	24	9.71 339	3 <sup>x</sup>	0.28 661	9.94 858	7	41	.6 18.0
21	9.66 221	25	9.71 370	3 <sup>x</sup>	0.28 630	9.94 852	6	40	.7 21.0
22	9.66 246	24	9.71 401	3 <sup>x</sup>	0.28 599	9.94 845	7	39	.8 24.0
23	9.66 270	25	9.71 431	3 <sup>x</sup>	0.28 569	9.94 839	6	38	.9 27.0
24	9.66 295	24	9.71 462	3 <sup>x</sup>	0.28 538	9.94 832	7	37	
25	9.66 319	24	9.71 493	3 <sup>x</sup>	0.28 507	9.94 826	6	36	
26	9.66 343	25	9.71 524	3 <sup>x</sup>	0.28 476	9.94 819	7	35	
27	9.66 368	25	9.71 555	3 <sup>x</sup>	0.28 445	9.94 813	6	34	.1 2.5 2.4
28	9.66 392	24	9.71 586	3 <sup>x</sup>	0.28 414	9.94 806	7	33	.2 5.0 4.8
29	9.66 416	24	9.71 617	3 <sup>x</sup>	0.28 383	9.94 799	7	32	.3 7.5 7.2
30	9.66 441	25	9.71 648	3 <sup>x</sup>	0.28 352	9.94 793	6	31	.4 10.0 9.6
31	9.66 465	24	9.71 679	3 <sup>x</sup>	0.28 321	9.94 786	7	30	.5 12.5 12.0
32	9.66 489	24	9.71 709	3 <sup>x</sup>	0.28 291	9.94 780	6	29	.6 15.0 14.4
33	9.66 513	24	9.71 740	3 <sup>x</sup>	0.28 260	9.94 773	7	28	.7 17.5 16.8
34	9.66 537	25	9.71 771	3 <sup>x</sup>	0.28 229	9.94 767	6	27	.8 20.0 19.2
35	9.66 562	24	9.71 802	3 <sup>x</sup>	0.28 198	9.94 760	7	26	.9 22.5 21.6
36	9.66 586	24	9.71 833	3 <sup>x</sup>	0.28 167	9.94 753	7	25	
37	9.66 610	24	9.71 863	3 <sup>x</sup>	0.28 137	9.94 747	6	24	
38	9.66 634	24	9.71 894	3 <sup>x</sup>	0.28 106	9.94 740	7	23	
39	9.66 658	24	9.71 925	3 <sup>x</sup>	0.28 075	9.94 734	6	22	
40	9.66 682	24	9.71 955	3 <sup>x</sup>	0.28 045	9.94 727	7	21	
41	9.66 706	24	9.71 986	3 <sup>x</sup>	0.28 014	9.94 720	7	20	.1 2.3
42	9.66 731	25	9.72 017	3 <sup>x</sup>	0.27 983	9.94 714	6	19	.2 4.6
43	9.66 755	24	9.72 048	3 <sup>x</sup>	0.27 952	9.94 707	7	18	.3 6.9
44	9.66 779	24	9.72 078	3 <sup>x</sup>	0.27 922	9.94 700	7	17	.4 9.2
45	9.66 803	24	9.72 109	3 <sup>x</sup>	0.27 891	9.94 694	6	16	.5 11.5
46	9.66 827	24	9.72 140	3 <sup>x</sup>	0.27 860	9.94 687	7	15	.6 13.8
47	9.66 851	24	9.72 170	3 <sup>x</sup>	0.27 830	9.94 680	7	14	.7 16.1
48	9.66 875	24	9.72 201	3 <sup>x</sup>	0.27 799	9.94 674	6	13	.8 18.4
49	9.66 899	24	9.72 231	3 <sup>x</sup>	0.27 769	9.94 667	7	12	.9 20.7
50	9.66 922	23	9.72 262	3 <sup>x</sup>	0.27 738	9.94 660	7	11	
51	9.66 946	24	9.72 293	3 <sup>x</sup>	0.27 707	9.94 654	6	10	.1 0.7 0.6
52	9.66 970	24	9.72 323	3 <sup>x</sup>	0.27 677	9.94 647	7	9	.2 1.4 1.2
53	9.66 994	24	9.72 354	3 <sup>x</sup>	0.27 646	9.94 640	7	8	.3 2.1 1.8
54	9.67 018	24	9.72 384	3 <sup>x</sup>	0.27 616	9.94 634	6	7	.4 2.8 2.4
55	9.67 042	24	9.72 415	3 <sup>x</sup>	0.27 585	9.94 627	7	6	.5 3.5 3.0
56	9.67 066	24	9.72 445	3 <sup>x</sup>	0.27 555	9.94 620	7	5	.6 4.2 3.6
57	9.67 090	24	9.72 476	3 <sup>x</sup>	0.27 524	9.94 614	6	4	.7 4.9 4.2
58	9.67 113	23	9.72 506	3 <sup>x</sup>	0.27 494	9.94 607	7	3	.8 5.6 4.8
59	9.67 137	24	9.72 537	3 <sup>x</sup>	0.27 463	9.94 600	7	2	.9 6.3 5.4
60	9.67 161	24	9.72 567	3 <sup>x</sup>	0.27 433	9.94 593	7	1	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	,	Prop. Pts.

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TABLE IV.

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<i>i</i>	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.	60	Prop. Pts.
0	9.67 161	24	9.72 567	3 <sup>1</sup>	0.27 433	9.94 593	6	<b>60</b>	
1	9.67 185	23	9.72 598	30	0.27 402	9.94 587	7	59	
2	9.67 208	24	9.72 628	3 <sup>1</sup>	0.27 372	9.94 580	7	58	
3	9.67 232	24	9.72 659	30	0.27 341	9.94 573	6	57	.1   3.1   3.0
4	9.67 256	24	9.72 689	3 <sup>1</sup>	0.27 311	9.94 567	7	56	.2   6.2   6.0
5	9.67 280	23	9.72 720	30	0.27 280	9.94 560	7	55	.3   9.3   9.0
6	9.67 303	24	9.72 750	30	0.27 250	9.94 553	7	54	.4   12.4   12.0
7	9.67 327	23	9.72 780	30	0.27 220	9.94 546	6	53	.5   15.5   15.0
8	9.67 350	24	9.72 811	3 <sup>1</sup>	0.27 189	9.94 540	7	52	.6   18.6   18.0
9	9.67 374	24	9.72 841	3 <sup>1</sup>	0.27 159	9.94 533	7	51	.7   21.7   21.0
10	9.67 398	23	9.72 872	30	0.27 128	9.94 526	7	<b>50</b>	.8   24.8   24.0
11	9.67 421	24	9.72 902	30	0.27 098	9.94 519	6	49	.9   27.9   27.0
12	9.67 445	23	9.72 932	30	0.27 068	9.94 513	7	48	
13	9.67 468	24	9.72 963	3 <sup>1</sup>	0.27 037	9.94 506	7	47	
14	9.67 492	23	9.72 993	30	0.27 007	9.94 499	7	46	
15	9.67 515	24	9.73 023	3 <sup>1</sup>	0.26 977	9.94 492	7	45	.1   2.9
16	9.67 539	23	9.73 054	30	0.26 946	9.94 485	6	44	.2   5.8
17	9.67 562	24	9.73 084	30	0.26 916	9.94 479	7	43	.3   8.7
18	9.67 586	23	9.73 114	30	0.26 886	9.94 472	7	42	.4   11.6
19	9.67 609	24	9.73 144	3 <sup>1</sup>	0.26 856	9.94 465	7	41	.5   14.5
20	9.67 633	23	9.73 175	30	0.26 825	9.94 458	7	<b>40</b>	.6   17.4
21	9.67 656	24	9.73 205	30	0.26 795	9.94 451	7	39	.7   20.3
22	9.67 680	23	9.73 235	30	0.26 765	9.94 445	7	38	.8   23.2
23	9.67 703	23	9.73 265	30	0.26 735	9.94 438	7	37	.9   26.1
24	9.67 726	24	9.73 295	3 <sup>1</sup>	0.26 705	9.94 431	7	36	
25	9.67 750	23	9.73 326	30	0.26 674	9.94 424	7	35	
26	9.67 773	23	9.73 356	30	0.26 644	9.94 417	7	34	.1   2.4   2.3
27	9.67 796	24	9.73 386	30	0.26 614	9.94 410	6	33	.2   4.8   4.6
28	9.67 820	23	9.73 416	30	0.26 584	9.94 404	7	32	.3   7.2   6.9
29	9.67 843	23	9.73 446	30	0.26 554	9.94 397	7	31	.4   9.6   9.2
30	9.67 866	24	9.73 476	3 <sup>1</sup>	0.26 524	9.94 390	7	<b>30</b>	.5   12.0   11.5
31	9.67 890	23	9.73 507	30	0.26 493	9.94 383	7	29	.6   14.4   13.8
32	9.67 913	23	9.73 537	30	0.26 463	9.94 376	7	28	.7   16.8   16.1
33	9.67 936	23	9.73 567	30	0.26 433	9.94 369	7	27	.8   19.2   18.4
34	9.67 959	23	9.73 597	30	0.26 403	9.94 362	7	26	.9   21.6   20.7
35	9.67 982	24	9.73 627	30	0.26 373	9.94 355	6	25	
36	9.68 006	23	9.73 657	30	0.26 343	9.94 349	7	24	
37	9.68 029	23	9.73 687	30	0.26 313	9.94 342	7	23	
38	9.68 052	23	9.73 717	30	0.26 283	9.94 335	7	22	.1   2.2
39	9.68 075	23	9.73 747	30	0.26 253	9.94 328	7	21	.2   4.4
40	9.68 098	23	9.73 777	30	0.26 223	9.94 321	7	<b>20</b>	.3   6.6
41	9.68 121	23	9.73 807	30	0.26 193	9.94 314	7	19	.4   8.8
42	9.68 144	23	9.73 837	30	0.26 163	9.94 307	7	18	.5   11.0
43	9.68 167	23	9.73 867	30	0.26 133	9.94 300	7	17	.6   13.2
44	9.68 190	23	9.73 897	30	0.26 103	9.94 293	7	16	.7   15.4
45	9.68 213	24	9.73 927	30	0.26 073	9.94 286	7	15	.8   17.6
46	9.68 237	23	9.73 957	30	0.26 043	9.94 279	6	14	.9   19.8
47	9.68 260	23	9.73 987	30	0.26 013	9.94 273	7	13	
48	9.68 283	23	9.74 017	30	0.25 983	9.94 266	7	12	
49	9.68 305	23	9.74 047	30	0.25 953	9.94 259	7	11	
50	9.68 328	23	9.74 077	30	0.25 923	9.94 252	7	<b>10</b>	.1   0.7   0.6
51	9.68 351	23	9.74 107	30	0.25 893	9.94 245	7	9	.2   1.4   1.2
52	9.68 374	23	9.74 137	29	0.25 863	9.94 238	7	8	.3   2.1   1.8
53	9.68 397	23	9.74 166	30	0.25 834	9.94 231	7	7	.4   2.8   2.4
54	9.68 420	23	9.74 196	30	0.25 804	9.94 224	7	6	.5   3.5   3.0
55	9.68 443	23	9.74 226	30	0.25 774	9.94 217	7	5	.6   4.2   3.6
56	9.68 466	23	9.74 256	30	0.25 744	9.94 210	7	4	.7   4.9   4.2
57	9.68 489	23	9.74 286	30	0.25 714	9.94 203	7	3	.8   5.6   4.8
58	9.68 512	23	9.74 316	30	0.25 684	9.94 196	7	2	.9   6.3   5.4
59	9.68 534	23	9.74 345	29	0.25 655	9.94 189	7	1	
60	9.68 557	23	9.74 375	30	0.25 625	9.94 182	7	<b>0</b>	
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	d.		Prop. Pts.

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	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.68 557	23	9.74 375	30	0.25 625	9.94 182	7	60	
1	9.68 580	23	9.74 405	30	0.25 595	9.94 175	7	59	.1 3.0
2	9.68 603	22	9.74 435	30	0.25 565	9.94 168	7	58	.2 6.0
3	9.68 625	23	9.74 465	29	0.25 535	9.94 161	7	57	.3 9.0
4	9.68 648	23	9.74 494	30	0.25 506	9.94 154	7	56	.4 12.0
5	9.68 671	23	9.74 524	30	0.25 476	9.94 147	7	55	.5 15.0
6	9.68 694	22	9.74 554	29	0.25 446	9.94 140	7	54	.6 18.0
7	9.68 716	23	9.74 583	30	0.25 417	9.94 133	7	53	.7 21.0
8	9.68 739	23	9.74 613	30	0.25 387	9.94 126	7	52	.8 24.0
9	9.68 762	22	9.74 643	30	0.25 357	9.94 119	7	51	.9 27.0
10	9.68 784	23	9.74 673	30	0.25 327	9.94 112	7	50	29
11	9.68 807	22	9.74 702	29	0.25 298	9.94 105	7	49	.1 2.9
12	9.68 829	23	9.74 732	30	0.25 268	9.94 098	8	48	.2 5.8
13	9.68 852	23	9.74 762	30	0.25 238	9.94 090	7	47	.3 8.7
14	9.68 875	23	9.74 791	29	0.25 209	9.94 083	7	46	.4 11.6
15	9.68 897	23	9.74 821	30	0.25 179	9.94 076	7	45	.5 14.5
16	9.68 920	22	9.74 851	30	0.25 149	9.94 069	7	44	.6 17.4
17	9.68 942	23	9.74 880	29	0.25 120	9.94 062	7	43	.7 20.3
18	9.68 965	23	9.74 910	30	0.25 090	9.94 055	7	42	.8 23.2
19	9.68 987	22	9.74 939	29	0.25 061	9.94 048	7	41	.9 26.1
20	9.69 010	23	9.74 969	30	0.25 031	9.94 041	7	40	23
21	9.69 032	22	9.74 998	29	0.25 002	9.94 034	7	39	.1 2.3
22	9.69 055	23	9.75 028	30	0.24 972	9.94 027	7	38	.2 4.6
23	9.69 077	23	9.75 058	30	0.24 942	9.94 020	8	37	.3 6.9
24	9.69 100	22	9.75 087	29	0.24 913	9.94 012	7	36	.4 9.2
25	9.69 122	22	9.75 117	30	0.24 883	9.94 005	7	35	.5 11.5
26	9.69 144	23	9.75 146	29	0.24 854	9.93 998	7	34	.6 13.8
27	9.69 167	22	9.75 176	30	0.24 824	9.93 991	7	33	.7 16.1
28	9.69 189	23	9.75 205	29	0.24 795	9.93 984	7	32	.8 18.4
29	9.69 212	22	9.75 235	30	0.24 765	9.93 977	7	31	.9 20.7
30	9.69 234	22	9.75 264	30	0.24 736	9.93 970	7	30	22
31	9.69 256	23	9.75 294	30	0.24 706	9.93 963	8	29	.1 2.2
32	9.69 279	22	9.75 323	29	0.24 677	9.93 955	8	28	.2 4.4
33	9.69 301	22	9.75 353	30	0.24 647	9.93 948	7	27	.3 6.6
34	9.69 323	22	9.75 382	29	0.24 618	9.93 941	7	26	.4 9.2
35	9.69 345	23	9.75 411	29	0.24 589	9.93 934	7	25	.5 11.5
36	9.69 368	22	9.75 441	30	0.24 559	9.93 927	7	24	.6 13.8
37	9.69 390	22	9.75 470	29	0.24 530	9.93 920	8	23	.7 16.1
38	9.69 412	22	9.75 500	30	0.24 500	9.93 912	7	22	.8 18.4
39	9.69 434	22	9.75 529	29	0.24 471	9.93 905	7	21	.9 20.7
40	9.69 456	23	9.75 558	30	0.24 442	9.93 898	7	20	22
41	9.69 479	22	9.75 588	30	0.24 412	9.93 891	7	19	.1 2.2
42	9.69 501	22	9.75 617	29	0.24 383	9.93 884	7	18	.2 4.4
43	9.69 523	22	9.75 647	30	0.24 353	9.93 876	8	17	.3 6.6
44	9.69 545	22	9.75 676	29	0.24 324	9.93 869	7	16	.4 9.2
45	9.69 567	22	9.75 705	29	0.24 295	9.93 862	7	15	.5 11.5
46	9.69 589	22	9.75 735	30	0.24 265	9.93 855	7	14	.6 13.8
47	9.69 611	22	9.75 764	29	0.24 236	9.93 847	8	13	.7 16.1
48	9.69 633	22	9.75 793	29	0.24 207	9.93 840	7	12	.8 18.4
49	9.69 655	22	9.75 822	29	0.24 178	9.93 833	7	11	.9 20.7
50	9.69 677	22	9.75 852	30	0.24 148	9.93 826	7	10	8 7
51	9.69 699	22	9.75 881	29	0.24 119	9.93 819	7	9	.1 0.7
52	9.69 721	22	9.75 910	29	0.24 090	9.93 811	8	8	.2 1.6
53	9.69 743	22	9.75 939	29	0.24 061	9.93 804	7	7	.3 2.4
54	9.69 765	22	9.75 969	30	0.24 031	9.93 797	7	6	.4 3.2
55	9.69 787	22	9.75 998	29	0.24 002	9.93 789	8	5	.5 4.0
56	9.69 809	22	9.76 027	29	0.23 973	9.93 782	7	4	.6 4.8
57	9.69 831	22	9.76 056	29	0.23 944	9.93 775	7	3	.7 5.6
58	9.69 853	22	9.76 086	30	0.23 914	9.93 768	7	2	.8 6.4
59	9.69 875	22	9.76 115	29	0.23 885	9.93 760	8	1	.9 7.2
60	9.69 897	22	9.76 144	29	0.23 856	9.93 753	7	0	6.3
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

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TABLE IV.

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	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.69 897	22	9.76 144	29	0.23 856	9.93 753	7	<b>60</b>	
1	9.69 919	22	9.76 173	29	0.23 827	9.93 746	8	59	
2	9.69 941	22	9.76 202	29	0.23 798	9.93 738	7	58	
3	9.69 963	21	9.76 231	30	0.23 769	9.93 731	7	57	.1 30 .2 29
4	9.69 984	22	9.76 261	29	0.23 739	9.93 724	7	56	.2 6.0 5.8
5	9.70 006	22	9.76 290	29	0.23 710	9.93 717	8	55	.3 9.0 8.7
6	9.70 028	22	9.76 319	29	0.23 681	9.93 709	7	54	.4 12.0 11.6
7	9.70 050	22	9.76 348	29	0.23 652	9.93 702	7	53	.5 15.0 14.5
8	9.70 072	21	9.76 377	29	0.23 623	9.93 695	8	52	.6 18.0 17.4
9	9.70 093	22	9.76 406	29	0.23 594	9.93 687	7	51	.7 21.0 20.3
10	9.70 115	22	9.76 435	29	0.23 565	9.93 680	7	<b>50</b>	.8 24.0 23.2
11	9.70 137	22	9.76 464	29	0.23 536	9.93 673	8	49	.9 27.0 26.1
12	9.70 159	21	9.76 493	29	0.23 507	9.93 665	8	48	
13	9.70 180	22	9.76 522	29	0.23 478	9.93 658	7	47	
14	9.70 202	22	9.76 551	29	0.23 449	9.93 650	8	46	
15	9.70 224	21	9.76 580	29	0.23 420	9.93 643	7	45	.1 2.8
16	9.70 245	22	9.76 609	29	0.23 391	9.93 636	7	44	.2 5.6
17	9.70 267	21	9.76 639	30	0.23 361	9.93 628	8	43	.3 8.4
18	9.70 288	22	9.76 668	29	0.23 332	9.93 621	7	42	.4 11.2
19	9.70 310	22	9.76 697	28	0.23 303	9.93 614	7	41	.5 14.0
20	9.70 332	21	9.76 725	29	0.23 275	9.93 606	7	<b>40</b>	.6 16.8
21	9.70 353	22	9.76 754	29	0.23 246	9.93 599	8	39	.7 19.6
22	9.70 375	21	9.76 783	29	0.23 217	9.93 591	8	38	.8 22.4
23	9.70 396	22	9.76 812	29	0.23 188	9.93 584	7	37	.9 25.2
24	9.70 418	21	9.76 841	29	0.23 159	9.93 577	8	36	
25	9.70 439	22	9.76 870	29	0.23 130	9.93 569	7	35	
26	9.70 461	21	9.76 899	29	0.23 101	9.93 562	8	34	.1 2.2
27	9.70 482	22	9.76 928	29	0.23 072	9.93 554	7	33	.2 4.4
28	9.70 504	21	9.76 957	29	0.23 043	9.93 547	8	32	.3 6.6
29	9.70 525	22	9.76 986	29	0.23 014	9.93 539	8	31	.4 8.8
30	9.70 547	21	9.77 015	29	0.22 985	9.93 532	7	<b>30</b>	.5 11.0
31	9.70 568	22	9.77 044	29	0.22 956	9.93 525	7	29	.6 13.2
32	9.70 590	21	9.77 073	28	0.22 927	9.93 517	7	28	.7 15.4
33	9.70 611	22	9.77 101	29	0.22 897	9.93 510	7	27	.8 17.6
34	9.70 633	21	9.77 130	29	0.22 870	9.93 502	8	26	.9 19.8
35	9.70 654	21	9.77 159	29	0.22 841	9.93 495	7	25	
36	9.70 675	22	9.77 188	29	0.22 812	9.93 487	8	24	
37	9.70 697	21	9.77 217	29	0.22 783	9.93 480	7	<b>23</b>	
38	9.70 718	21	9.77 246	29	0.22 754	9.93 472	8	22	
39	9.70 739	22	9.77 274	29	0.22 726	9.93 465	7	21	.1 2.1
40	9.70 761	21	9.77 303	29	0.22 697	9.93 457	8	<b>20</b>	.2 4.2
41	9.70 782	21	9.77 332	29	0.22 668	9.93 450	7	19	.3 6.3
42	9.70 803	21	9.77 361	29	0.22 639	9.93 442	8	18	.4 8.4
43	9.70 824	22	9.77 390	28	0.22 610	9.93 435	7	17	.5 10.5
44	9.70 846	21	9.77 418	29	0.22 582	9.93 427	8	16	.6 12.6
45	9.70 867	21	9.77 447	29	0.22 553	9.93 420	7	15	.7 14.7
46	9.70 888	21	9.77 476	29	0.22 524	9.93 412	8	14	.8 16.8
47	9.70 909	22	9.77 505	28	0.22 495	9.93 405	7	<b>13</b>	.9 18.9
48	9.70 931	21	9.77 533	29	0.22 467	9.93 397	8	12	
49	9.70 952	21	9.77 562	29	0.22 438	9.93 390	7	11	
50	9.70 973	21	9.77 591	28	0.22 409	9.93 382	8	<b>10</b>	.1 0.8 0.7
51	9.70 994	21	9.77 619	29	0.22 381	9.93 375	7	9	.2 1.6 1.4
52	9.71 015	21	9.77 648	29	0.22 352	9.93 367	8	8	.3 2.4 2.1
53	9.71 036	21	9.77 677	29	0.22 323	9.93 360	7	7	.4 3.2 2.8
54	9.71 058	21	9.77 706	28	0.22 294	9.93 352	8	6	.5 4.0 3.5
55	9.71 079	21	9.77 734	29	0.22 266	9.93 344	7	5	.6 4.8 4.2
56	9.71 100	21	9.77 763	28	0.22 237	9.93 337	8	4	.7 5.6 4.9
57	9.71 121	21	9.77 791	29	0.22 209	9.93 329	7	3	.8 6.4 5.6
58	9.71 142	21	9.77 820	29	0.22 180	9.93 322	8	2	.9 7.2 6.3
59	9.71 163	21	9.77 849	28	0.22 151	9.93 314	7	<b>0</b>	
60	9.71 184	21	9.77 877	28	0.22 123	9.93 307			Prop. Pts.
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	

## 31°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.
0	9.71 184	21	9.77 877	29	0.22 123	9.93 307	8	60	
1	9.71 205	21	9.77 906	29	0.22 094	9.93 299	8	59	
2	9.71 226	21	9.77 935	28	0.22 065	9.93 291	7	58	
3	9.71 247	21	9.77 963	29	0.22 037	9.93 284	8	57	.1 2.9
4	9.71 268	21	9.77 992	28	0.22 008	9.93 276	7	56	.2 5.8
5	9.71 289	21	9.78 020	29	0.21 980	9.93 269	8	55	.3 8.7
6	9.71 310	21	9.78 049	28	0.21 951	9.93 261	8	54	.4 11.6
7	9.71 331	21	9.78 077	29	0.21 923	9.93 253	7	53	.5 14.5
8	9.71 352	21	9.78 106	29	0.21 894	9.93 246	8	52	.6 17.4
9	9.71 373	20	9.78 135	28	0.21 865	9.93 238	8	51	.7 20.3
10	9.71 393	21	9.78 163	29	0.21 837	9.93 230	7	50	.8 23.2
11	9.71 414	21	9.78 192	29	0.21 808	9.93 223	8	49	.9 26.1
12	9.71 435	21	9.78 220	28	0.21 780	9.93 215	8	48	
13	9.71 456	21	9.78 249	29	0.21 751	9.93 207	7	47	
14	9.71 477	21	9.78 277	28	0.21 723	9.93 200	7	46	
15	9.71 498	21	9.78 306	28	0.21 694	9.93 192	8	45	.1 2.8
16	9.71 519	21	9.78 334	28	0.21 666	9.93 184	8	44	.2 5.6
17	9.71 539	20	9.78 363	29	0.21 637	9.93 177	8	43	.3 8.4
18	9.71 560	21	9.78 391	28	0.21 609	9.93 169	8	42	.4 11.2
19	9.71 581	21	9.78 419	28	0.21 581	9.93 161	7	41	.5 14.0
20	9.71 602	20	9.78 448	29	0.21 552	9.93 154	8	40	.6 16.8
21	9.71 622	21	9.78 476	28	0.21 524	9.93 146	8	39	.7 19.6
22	9.71 643	21	9.78 505	29	0.21 495	9.93 138	8	38	.8 22.4
23	9.71 664	21	9.78 533	28	0.21 467	9.93 131	7	37	.9 25.2
24	9.71 685	21	9.78 562	29	0.21 438	9.93 123	8	36	
25	9.71 705	21	9.78 590	28	0.21 410	9.93 115	7	35	
26	9.71 726	21	9.78 618	28	0.21 382	9.93 108	8	34	.1 2.1
27	9.71 747	20	9.78 647	29	0.21 353	9.93 100	8	33	.2 4.2
28	9.71 767	20	9.78 675	28	0.21 325	9.93 092	8	32	.3 6.3
29	9.71 788	21	9.78 704	28	0.21 296	9.93 084	7	31	.4 8.4
30	9.71 809	20	9.78 732	28	0.21 268	9.93 077	8	30	.5 10.5
31	9.71 829	21	9.78 760	29	0.21 240	9.93 069	8	29	.6 12.6
32	9.71 850	20	9.78 789	28	0.21 211	9.93 061	8	28	.7 14.7
33	9.71 870	21	9.78 817	28	0.21 183	9.93 053	7	27	.8 16.8
34	9.71 891	20	9.78 845	29	0.21 155	9.93 046	8	26	.9 18.9
35	9.71 911	21	9.78 874	28	0.21 126	9.93 038	8	25	
36	9.71 932	20	9.78 902	28	0.21 098	9.93 030	8	24	
37	9.71 952	21	9.78 930	29	0.21 070	9.93 022	8	23	
38	9.71 973	21	9.78 959	28	0.21 041	9.93 014	8	22	.1 2.0
39	9.71 994	20	9.78 987	28	0.21 013	9.93 007	7	21	.2 4.0
40	9.72 014	20	9.79 015	28	0.20 985	9.92 999	8	20	.3 6.0
41	9.72 034	21	9.79 043	29	0.20 957	9.92 991	8	19	.4 8.0
42	9.72 055	20	9.79 072	28	0.20 928	9.92 983	8	18	.5 10.0
43	9.72 075	21	9.79 100	28	0.20 900	9.92 976	7	17	.6 12.0
44	9.72 096	20	9.79 128	28	0.20 872	9.92 968	8	16	.7 14.0
45	9.72 116	21	9.79 156	29	0.20 844	9.92 960	8	15	.8 16.0
46	9.72 137	20	9.79 185	28	0.20 815	9.92 952	8	14	.9 18.0
47	9.72 157	20	9.79 213	28	0.20 787	9.92 944	8	13	
48	9.72 177	21	9.79 241	28	0.20 759	9.92 936	8	12	
49	9.72 198	20	9.79 269	28	0.20 731	9.92 929	7	11	
50	9.72 218	20	9.79 297	29	0.20 703	9.92 921	8	10	.1 0.8 0.7
51	9.72 238	21	9.79 326	28	0.20 674	9.92 913	8	9	.2 1.6 1.4
52	9.72 259	20	9.79 354	28	0.20 646	9.92 905	8	8	.3 2.4 2.1
53	9.72 279	20	9.79 382	28	0.20 618	9.92 897	8	7	.4 3.2 2.8
54	9.72 299	21	9.79 410	28	0.20 590	9.92 889	8	6	.5 4.0 3.5
55	9.72 320	20	9.79 438	28	0.20 562	9.92 881	8	5	.6 4.8 4.2
56	9.72 340	20	9.79 466	29	0.20 534	9.92 874	7	4	.7 5.6 4.9
57	9.72 360	21	9.79 495	29	0.20 505	9.92 866	8	3	.8 6.4 5.6
58	9.72 381	21	9.79 523	28	0.20 477	9.92 858	8	2	.9 7.2 6.3
59	9.72 401	20	9.79 551	28	0.20 449	9.92 850	8	1	
60	9.72 421	20	9.79 579	28	0.20 421	9.92 842	0		
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

	L. Sln.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.72 421	20	9.79 579	28	0.20 421	9.92 842	8	60	
1	9.72 441	20	9.79 607	28	0.20 393	9.92 834	8	59	.1 29 28
2	9.72 461	21	9.79 635	28	0.20 365	9.92 826	8	58	.2 5.8 5.6
3	9.72 482	20	9.79 663	28	0.20 337	9.92 818	8	57	.3 8.7 8.4
4	9.72 502	20	9.79 691	28	0.20 309	9.92 810	7	56	.4 11.6 11.2
5	9.72 522	20	9.79 719	28	0.20 281	9.92 803	8	55	.5 14.5 14.0
6	9.72 542	20	9.79 747	29	0.20 253	9.92 795	8	54	.6 17.4 16.8
7	9.72 562	20	9.79 776	28	0.20 224	9.92 787	8	53	.7 20.3 19.6
8	9.72 582	20	9.79 804	28	0.20 196	9.92 779	8	52	.8 23.2 22.4
9	9.72 602	20	9.79 832	28	0.20 168	9.92 771	8	51	.9 26.1 25.2
10	9.72 622	21	9.79 860	28	0.20 140	9.92 763	8	50	
11	9.72 643	20	9.79 888	28	0.20 112	9.92 755	8	49	.1 2.7
12	9.72 663	20	9.79 916	28	0.20 084	9.92 747	8	48	.2 5.4
13	9.72 683	20	9.79 944	28	0.20 056	9.92 739	8	47	.3 8.1
14	9.72 703	20	9.79 972	28	0.20 028	9.92 731	8	46	.4 10.8
15	9.72 723	20	9.80 000	28	0.20 000	9.92 723	8	45	.5 13.5
16	9.72 743	20	9.80 028	28	0.19 972	9.92 715	8	44	.6 16.2
17	9.72 763	20	9.80 056	28	0.19 944	9.92 707	8	43	
18	9.72 783	20	9.80 084	28	0.19 916	9.92 699	8	42	.1 2.1
19	9.72 803	20	9.80 112	28	0.19 888	9.92 691	8	41	.2 4.2
20	9.72 823	20	9.80 140	28	0.19 860	9.92 683	8	40	.3 6.3
21	9.72 843	20	9.80 168	28	0.19 832	9.92 675	8	39	.4 8.0
22	9.72 863	20	9.80 195	27	0.19 805	9.92 667	8	38	.5 10.8
23	9.72 883	20	9.80 223	28	0.19 777	9.92 659	8	37	.6 13.5
24	9.72 902	19	9.80 251	28	0.19 749	9.92 651	8	36	
25	9.72 922	20	9.80 279	28	0.19 721	9.92 643	8	35	.1 2.0
26	9.72 942	20	9.80 307	28	0.19 693	9.92 635	8	34	.2 4.0
27	9.72 962	20	9.80 335	28	0.19 665	9.92 627	8	33	.3 6.0
28	9.72 982	20	9.80 363	28	0.19 637	9.92 619	8	32	.4 8.0
29	9.73 002	20	9.80 391	28	0.19 609	9.92 611	8	31	.5 10.0
30	9.73 022	19	9.80 419	28	0.19 581	9.92 603	8	30	.6 12.0
31	9.73 041	20	9.80 447	27	0.19 553	9.92 595	8	29	.7 14.0
32	9.73 061	20	9.80 474	28	0.19 526	9.92 587	8	28	.8 16.0
33	9.73 081	20	9.80 502	28	0.19 498	9.92 579	8	27	.9 18.0
34	9.73 101	20	9.80 530	28	0.19 470	9.92 571	8	26	
35	9.73 121	19	9.80 558	28	0.19 442	9.92 563	8	25	.1 2.1
36	9.73 140	20	9.80 586	28	0.19 414	9.92 555	8	24	.2 4.0
37	9.73 160	20	9.80 614	28	0.19 386	9.92 546	9	23	.3 6.0
38	9.73 180	20	9.80 642	28	0.19 358	9.92 538	8	22	.4 8.0
39	9.73 200	19	9.80 669	27	0.19 331	9.92 530	8	21	.5 10.0
40	9.73 219	20	9.80 697	28	0.19 303	9.92 522	8	20	.6 12.0
41	9.73 239	20	9.80 725	28	0.19 275	9.92 514	8	19	.7 14.0
42	9.73 259	20	9.80 753	28	0.19 247	9.92 506	8	18	.8 16.0
43	9.73 278	19	9.80 781	28	0.19 219	9.92 498	8	17	.9 18.0
44	9.73 298	20	9.80 808	27	0.19 192	9.92 490	8	16	
45	9.73 318	19	9.80 836	28	0.19 164	9.92 482	8	15	.1 2.0
46	9.73 337	19	9.80 864	28	0.19 136	9.92 473	9	14	.2 4.0
47	9.73 357	20	9.80 892	28	0.19 108	9.92 465	8	13	.3 6.0
48	9.73 377	20	9.80 919	27	0.19 081	9.92 457	8	12	.4 8.0
49	9.73 396	19	9.80 947	28	0.19 053	9.92 449	8	11	.5 10.0
50	9.73 416	20	9.80 975	28	0.19 025	9.92 441	8	10	.6 12.0
51	9.73 435	19	9.81 003	27	0.18 997	9.92 433	8	9	.7 14.0
52	9.73 455	20	9.81 030	28	0.18 970	9.92 425	8	8	.8 2.4
53	9.73 474	19	9.81 058	28	0.18 942	9.92 416	9	7	.9 2.8
54	9.73 494	20	9.81 086	28	0.18 914	9.92 408	8	6	
55	9.73 513	19	9.81 113	27	0.18 887	9.92 400	8	5	.1 0.8
56	9.73 533	20	9.81 141	28	0.18 859	9.92 392	8	4	.2 1.6
57	9.73 552	19	9.81 169	28	0.18 831	9.92 384	8	3	.3 4.0
58	9.73 572	20	9.81 196	27	0.18 804	9.92 376	8	2	.4 6.0
59	9.73 591	19	9.81 224	28	0.18 776	9.92 367	9	1	.5 8.0
60	9.73 611	20	9.81 252	28	0.18 748	9.92 359	8	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	,	Prop. Pts.

## 33°

	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.73 611	19	9.81 252	27	0.18 748	9.92 359	8	60	
1	9.73 630	20	9.81 279	28	0.18 721	9.92 351	8	59	
2	9.73 650	19	9.81 307	28	0.18 693	9.92 343	8	58	
3	9.73 669	20	9.81 335	27	0.18 665	9.92 335	9	57	.1 2.8 2.7
4	9.73 689	19	9.81 362	28	0.18 638	9.92 326	8	56	.2 5.6 5.4
5	9.73 708	19	9.81 390	28	0.18 610	9.92 318	8	55	.3 8.4 8.1
6	9.73 727	20	9.81 418	27	0.18 582	9.92 310	8	54	.4 11.2 10.8
7	9.73 747	19	9.81 445	28	0.18 555	9.92 302	9	53	.5 14.0 13.5
8	9.73 766	19	9.81 473	27	0.18 527	9.92 293	8	52	.6 16.8 16.2
9	9.73 785	20	9.81 500	28	0.18 500	9.92 285	8	51	.7 19.6 18.9
10	9.73 805	19	9.81 528	28	0.18 472	9.92 277	8	50	.8 22.4 21.6
11	9.73 824	19	9.81 556	27	0.18 444	9.92 269	9	49	.9 25.2 24.3
12	9.73 843	20	9.81 583	28	0.18 417	9.92 260	8	48	
13	9.73 863	19	9.81 611	27	0.18 389	9.92 252	8	47	
14	9.73 882	19	9.81 638	28	0.18 362	9.92 244	9	46	
15	9.73 901	20	9.81 666	27	0.18 334	9.92 235	8	45	.1 2.0
16	9.73 921	19	9.81 693	28	0.18 307	9.92 227	8	44	.2 4.0
17	9.73 940	19	9.81 721	28	0.18 279	9.92 219	8	43	.3 6.0
18	9.73 959	19	9.81 748	27	0.18 252	9.92 211	8	42	.4 8.0
19	9.73 978	19	9.81 776	28	0.18 224	9.92 202	9	41	.5 10.0
20	9.73 997	20	9.81 803	27	0.18 197	9.92 194	8	40	.6 12.0
21	9.74 017	19	9.81 831	28	0.18 169	9.92 186	8	39	.7 14.0
22	9.74 036	19	9.81 858	27	0.18 142	9.92 177	8	38	.8 16.0
23	9.74 055	19	9.81 886	28	0.18 114	9.92 169	8	37	.9 18.0
24	9.74 074	19	9.81 913	27	0.18 087	9.92 161	8	36	
25	9.74 093	20	9.81 941	28	0.18 059	9.92 152	9	35	
26	9.74 113	19	9.81 968	27	0.18 032	9.92 144	8	34	.1 1.9
27	9.74 132	19	9.81 996	28	0.18 004	9.92 136	9	33	.2 3.8
28	9.74 151	19	9.82 023	27	0.17 977	9.92 127	8	32	.3 5.7
29	9.74 170	19	9.82 051	28	0.17 949	9.92 119	8	31	.4 7.6
30	9.74 189	19	9.82 078	28	0.17 922	9.92 111	8	30	.5 9.5
31	9.74 208	19	9.82 106	27	0.17 894	9.92 102	9	29	.6 11.4
32	9.74 227	19	9.82 133	28	0.17 867	9.92 094	8	28	.7 13.3
33	9.74 246	19	9.82 161	27	0.17 839	9.92 086	9	27	.8 15.2
34	9.74 265	19	9.82 188	27	0.17 812	9.92 077	9	26	.9 17.1
35	9.74 284	19	9.82 215	28	0.17 785	9.92 069	8	25	
36	9.74 303	19	9.82 243	27	0.17 757	9.92 060	9	24	
37	9.74 322	19	9.82 270	28	0.17 730	9.92 052	8	23	
38	9.74 341	19	9.82 298	27	0.17 702	9.92 044	8	22	
39	9.74 360	19	9.82 325	27	0.17 675	9.92 035	9	21	.1 1.8
40	9.74 379	19	9.82 352	28	0.17 648	9.92 027	8	20	.2 3.6
41	9.74 398	19	9.82 380	27	0.17 620	9.92 018	9	19	.3 5.4
42	9.74 417	19	9.82 407	28	0.17 593	9.92 010	8	18	.4 7.2
43	9.74 436	19	9.82 435	27	0.17 565	9.92 002	8	17	.5 9.0
44	9.74 455	19	9.82 462	27	0.17 538	9.91 993	9	16	.6 10.8
45	9.74 474	19	9.82 489	28	0.17 511	9.91 985	8	15	.7 12.6
46	9.74 493	19	9.82 517	27	0.17 483	9.91 976	9	14	.8 14.4
47	9.74 512	19	9.82 544	27	0.17 456	9.91 968	8	13	.9 16.2
48	9.74 531	18	9.82 571	28	0.17 429	9.91 959	9	12	
49	9.74 549	19	9.82 599	27	0.17 401	9.91 951	8	11	
50	9.74 568	19	9.82 626	27	0.17 374	9.91 942	9	10	.1 0.9 0.8
51	9.74 587	19	9.82 653	28	0.17 347	9.91 934	8	9	.2 1.8 1.6
52	9.74 606	19	9.82 681	28	0.17 319	9.91 925	8	8	.3 2.7 2.4
53	9.74 625	19	9.82 708	27	0.17 292	9.91 917	8	7	.4 3.6 3.2
54	9.74 644	18	9.82 735	27	0.17 265	9.91 908	9	6	.5 4.5 4.0
55	9.74 662	19	9.82 762	28	0.17 238	9.91 900	8	5	.6 5.4 4.8
56	9.74 681	19	9.82 790	27	0.17 210	9.91 891	9	4	.7 6.3 5.6
57	9.74 700	19	9.82 817	27	0.17 183	9.91 883	8	3	.8 7.2 6.4
58	9.74 719	18	9.82 844	27	0.17 156	9.91 874	9	2	.9 8.1 7.2
59	9.74 737	19	9.82 871	27	0.17 129	9.91 866	8	1	
60	9.74 756	19	9.82 899	28	0.17 101	9.91 857	9	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	,	Prop. Pts.

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TABLE LV.

34°

/	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.	
0	9.74 756	19	9.82 899	27	0.17 101	9.91 857	8	<b>60</b>	
1	9.74 775	19	9.82 926	27	0.17 074	9.91 849	9	59	
2	9.74 794	18	9.82 953	27	0.17 047	9.91 840	8	58	
3	9.74 812	19	9.82 980	28	0.17 020	9.91 832	9	57	
4	9.74 831	19	9.83 008	27	0.16 992	9.91 823	8	56	.1 28 .2 2.8 .3 5.6 .4 5.4
5	9.74 850	18	9.83 035	27	0.16 965	9.91 815	9	55	.3 8.4 .4 8.1
6	9.74 868	19	9.83 062	27	0.16 938	9.91 806	8	54	.4 11.2 .5 10.8
7	9.74 887	19	9.83 089	28	0.16 911	9.91 798	9	53	.5 14.0 .6 13.5
8	9.74 906	18	9.83 117	27	0.16 883	9.91 789	8	52	.6 16.8 .7 16.2
9	9.74 924	19	9.83 144	27	0.16 856	9.91 781	9	51	.7 19.6 .8 18.9
10	9.74 943	18	9.83 171	27	0.16 829	9.91 772	9	<b>50</b>	.8 22.4 .9 21.6
11	9.74 961	19	9.83 198	27	0.16 802	9.91 763	8	49	
12	9.74 980	19	9.83 225	27	0.16 775	9.91 755	9	48	
13	9.74 999	18	9.83 252	27	0.16 748	9.91 746	8	47	
14	9.75 017	19	9.83 280	28	0.16 720	9.91 738	9	46	
15	9.75 036	18	9.83 307	27	0.16 693	9.91 729	9	45	.1 2.6
16	9.75 054	19	9.83 334	27	0.16 666	9.91 720	8	44	.2 5.2
17	9.75 073	18	9.83 361	27	0.16 639	9.91 712	9	43	.3 7.8
18	9.75 091	19	9.83 388	27	0.16 612	9.91 703	8	42	.4 10.4
19	9.75 110	18	9.83 415	27	0.16 585	9.91 695	9	41	.5 13.0
20	9.75 128	19	9.83 442	28	0.16 558	9.91 686	9	<b>40</b>	.6 15.6
21	9.75 147	18	9.83 470	27	0.16 530	9.91 677	8	39	.7 18.2
22	9.75 165	18	9.83 497	27	0.16 503	9.91 669	9	38	.8 20.8
23	9.75 184	19	9.83 524	27	0.16 476	9.91 660	9	37	.9 23.4
24	9.75 202	19	9.83 551	27	0.16 449	9.91 651	9	36	
25	9.75 221	18	9.83 578	27	0.16 422	9.91 643	8	35	
26	9.75 239	19	9.83 605	27	0.16 395	9.91 634	9	34	.1 1.9
27	9.75 258	19	9.83 632	27	0.16 368	9.91 625	8	33	.2 3.8
28	9.75 276	18	9.83 659	27	0.16 341	9.91 617	9	32	.3 5.7
29	9.75 294	19	9.83 686	27	0.16 314	9.91 608	9	31	.4 7.6
30	9.75 313	18	9.83 713	27	0.16 287	9.91 599	8	<b>30</b>	.5 9.5
31	9.75 331	19	9.83 740	28	0.16 260	9.91 591	8	29	.6 11.4
32	9.75 350	18	9.83 768	28	0.16 232	9.91 582	9	28	.7 13.3
33	9.75 368	18	9.83 795	27	0.16 205	9.91 573	8	27	.8 15.2
34	9.75 386	19	9.83 822	27	0.16 178	9.91 565	9	26	.9 17.1
35	9.75 405	18	9.83 849	27	0.16 151	9.91 556	9	25	
36	9.75 423	18	9.83 876	27	0.16 124	9.91 547	9	24	
37	9.75 441	18	9.83 903	27	0.16 097	9.91 538	8	23	
38	9.75 459	18	9.83 930	27	0.16 070	9.91 530	8	22	
39	9.75 478	18	9.83 957	27	0.16 043	9.91 521	9	21	
40	9.75 496	18	9.83 984	27	0.16 016	9.91 512	9	<b>20</b>	
41	9.75 514	19	9.84 011	27	0.15 989	9.91 504	8	19	.1 1.8
42	9.75 533	18	9.84 038	27	0.15 962	9.91 495	9	18	.2 3.6
43	9.75 551	18	9.84 065	27	0.15 935	9.91 486	9	17	.3 5.4
44	9.75 569	18	9.84 092	27	0.15 908	9.91 477	9	16	.4 7.2
45	9.75 587	18	9.84 119	27	0.15 881	9.91 469	8	15	.5 9.0
46	9.75 605	18	9.84 146	27	0.15 854	9.91 460	9	14	.6 10.8
47	9.75 624	19	9.84 173	27	0.15 827	9.91 451	9	13	.7 12.6
48	9.75 642	18	9.84 200	27	0.15 800	9.91 442	9	12	.8 14.4
49	9.75 660	18	9.84 227	27	0.15 773	9.91 433	8	11	.9 16.2
50	9.75 678	18	9.84 254	26	0.15 746	9.91 425	8	<b>10</b>	
51	9.75 696	18	9.84 280	26	0.15 720	9.91 410	9	9	
52	9.75 714	19	9.84 307	27	0.15 693	9.91 407	9	8	.1 2.7
53	9.75 733	18	9.84 334	27	0.15 666	9.91 398	9	7	.2 3.6
54	9.75 751	18	9.84 361	27	0.15 639	9.91 389	8	6	.3 4.5
55	9.75 769	18	9.84 388	27	0.15 612	9.91 381	9	5	.4 4.6
56	9.75 787	18	9.84 415	27	0.15 585	9.91 372	9	4	.5 5.4
57	9.75 805	18	9.84 442	27	0.15 558	9.91 363	9	3	.6 5.6
58	9.75 823	18	9.84 469	27	0.15 531	9.91 354	9	2	.7 6.4
59	9.75 841	18	9.84 496	27	0.15 504	9.91 345	9	1	.8 7.2
60	9.75 859	18	9.84 523	27	0.15 477	9.91 336	9	<b>0</b>	
L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.	

35°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
<b>0</b>	9.75 859	18	9.84 523	27	0.15 477	9.91 336	8	<b>60</b>	
<b>1</b>	9.75 877	18	9.84 550	26	0.15 450	9.91 328	9	59	
<b>2</b>	9.75 895	18	9.84 576	27	0.15 424	9.91 319	9	58	
<b>3</b>	9.75 913	18	9.84 603	27	0.15 397	9.91 310	9	57	.1 2.7 2.6
<b>4</b>	9.75 931	18	9.84 630	27	0.15 370	9.91 301	9	56	.2 5.4 5.2
<b>5</b>	9.75 949	18	9.84 657	27	0.15 343	9.91 292	9	55	.3 8.1 7.8
<b>6</b>	9.75 967	18	9.84 684	27	0.15 316	9.91 283	9	54	.4 10.8 10.4
<b>7</b>	9.75 985	18	9.84 711	27	0.15 289	9.91 274	8	53	.5 13.5 13.0
<b>8</b>	9.76 003	18	9.84 738	26	0.15 262	9.91 266	9	52	.6 16.2 15.6
<b>9</b>	9.76 021	18	9.84 764	26	0.15 236	9.91 257	9	51	.7 18.9 18.2
<b>10</b>	9.76 039	18	9.84 791	27	0.15 209	9.91 248	9	<b>50</b>	.8 21.6 20.8
<b>11</b>	9.76 057	18	9.84 818	27	0.15 182	9.91 239	9	49	.9 24.3 23.4
<b>12</b>	9.76 075	18	9.84 845	27	0.15 155	9.91 230	9	48	
<b>13</b>	9.76 093	18	9.84 872	27	0.15 128	9.91 221	9	47	
<b>14</b>	9.76 111	18	9.84 899	27	0.15 101	9.91 212	9	46	
<b>15</b>	9.76 129	17	9.84 925	27	0.15 075	9.91 203	9	45	.1 1.8
<b>16</b>	9.76 146	18	9.84 952	27	0.15 048	9.91 194	9	44	.2 3.6
<b>17</b>	9.76 164	18	9.84 979	27	0.15 021	9.91 185	9	43	.3 5.4
<b>18</b>	9.76 182	18	9.85 006	27	0.14 994	9.91 176	9	42	.4 7.2
<b>19</b>	9.76 200	18	9.85 033	27	0.14 967	9.91 167	9	41	.5 9.0
<b>20</b>	9.76 218	18	9.85 059	27	0.14 941	9.91 158	9	<b>40</b>	.6 10.8
<b>21</b>	9.76 236	17	9.85 086	27	0.14 914	9.91 149	9	39	.7 12.6
<b>22</b>	9.76 253	18	9.85 113	27	0.14 887	9.91 141	9	38	.8 14.4
<b>23</b>	9.76 271	18	9.85 140	26	0.14 860	9.91 132	9	37	.9 16.2
<b>24</b>	9.76 289	18	9.85 166	27	0.14 834	9.91 123	9	36	
<b>25</b>	9.76 307	17	9.85 193	27	0.14 807	9.91 114	9	35	
<b>26</b>	9.76 324	18	9.85 220	27	0.14 780	9.91 105	9	34	.1 1.7
<b>27</b>	9.76 342	18	9.85 247	27	0.14 753	9.91 096	9	33	.2 3.4
<b>28</b>	9.76 360	18	9.85 273	27	0.14 727	9.91 087	9	32	.3 5.1
<b>29</b>	9.76 378	18	9.85 300	27	0.14 700	9.91 078	9	31	.4 6.8
<b>30</b>	9.76 395	18	9.85 327	27	0.14 673	9.91 069	9	<b>30</b>	.5 8.5
<b>31</b>	9.76 413	18	9.85 354	26	0.14 646	9.91 060	9	29	.6 10.2
<b>32</b>	9.76 431	17	9.85 380	26	0.14 620	9.91 051	9	28	.7 11.9
<b>33</b>	9.76 448	17	9.85 407	27	0.14 593	9.91 042	9	27	.8 13.6
<b>34</b>	9.76 466	18	9.85 434	27	0.14 566	9.91 033	10	26	.9 15.3
<b>35</b>	9.76 484	17	9.85 460	27	0.14 540	9.91 023	9	25	
<b>36</b>	9.76 501	18	9.85 487	27	0.14 513	9.91 014	9	24	
<b>37</b>	9.76 519	18	9.85 514	27	0.14 486	9.91 005	9	23	
<b>38</b>	9.76 537	18	9.85 540	26	0.14 460	9.90 996	9	22	
<b>39</b>	9.76 554	17	9.85 567	27	0.14 433	9.90 987	9	21	.1 1.0
<b>40</b>	9.76 572	18	9.85 594	27	0.14 406	9.90 978	9	<b>20</b>	.2 2.0
<b>41</b>	9.76 590	18	9.85 620	26	0.14 380	9.90 969	9	19	.3 3.0
<b>42</b>	9.76 607	17	9.85 647	27	0.14 353	9.90 960	9	18	.4 4.0
<b>43</b>	9.76 625	18	9.85 674	27	0.14 326	9.90 951	9	17	.5 5.0
<b>44</b>	9.76 642	17	9.85 700	26	0.14 300	9.90 942	9	16	.6 6.0
<b>45</b>	9.76 660	17	9.85 727	27	0.14 273	9.90 933	9	15	.7 7.0
<b>46</b>	9.76 677	18	9.85 754	27	0.14 246	9.90 924	9	14	.8 8.0
<b>47</b>	9.76 695	18	9.85 780	26	0.14 220	9.90 915	9	13	.9 9.0
<b>48</b>	9.76 712	17	9.85 807	27	0.14 193	9.90 906	9	12	
<b>49</b>	9.76 730	18	9.85 834	27	0.14 166	9.90 896	10	<b>11</b>	.1 0.9 0.8
<b>50</b>	9.76 747	17	9.85 860	26	0.14 140	9.90 887	9	<b>10</b>	.2 1.8 1.6
<b>51</b>	9.76 765	18	9.85 887	26	0.14 113	9.90 878	9	9	.3 2.7 2.4
<b>52</b>	9.76 782	17	9.85 913	27	0.14 087	9.90 869	9	8	.4 3.6 3.2
<b>53</b>	9.76 800	18	9.85 940	27	0.14 060	9.90 860	9	7	.5 4.5 4.0
<b>54</b>	9.76 817	17	9.85 967	26	0.14 033	9.90 851	9	6	.6 5.4 4.8
<b>55</b>	9.76 835	18	9.85 993	27	0.14 007	9.90 842	10	5	.7 6.3 5.6
<b>56</b>	9.76 852	17	9.86 020	26	0.13 980	9.90 832	10	4	.8 7.2 6.4
<b>57</b>	9.76 870	18	9.86 046	26	0.13 954	9.90 823	9	3	
<b>58</b>	9.76 887	17	9.86 073	27	0.13 927	9.90 814	9	2	.9 8.1 7.2
<b>59</b>	9.76 904	17	9.86 100	27	0.13 900	9.90 805	9	1	
<b>60</b>	9.76 922	18	9.86 126	26	0.13 874	9.90 796	9	<b>0</b>	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

TABLE IV.

36°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.
0	9.76 922	17	9.86 126	27	0.13 874	9.90 796	9	60	
1	9.76 939	18	9.86 153	26	0.13 847	9.90 787	10	59	
2	9.76 957	17	9.86 179	27	0.13 821	9.90 777	9	58	
3	9.76 974	17	9.86 206	26	0.13 794	9.90 768	9	57	
4	9.76 991	18	9.86 232	27	0.13 768	9.90 759	9	56	
5	9.77 009	17	9.86 259	26	0.13 741	9.90 750	9	55	.1 2.7 2.6
6	9.77 026	17	9.86 285	27	0.13 715	9.90 741	10	54	.2 5.4 5.2
7	9.77 043	18	9.86 312	26	0.13 688	9.90 731	9	53	.3 8.1 7.8
8	9.77 061	17	9.86 338	26	0.13 662	9.90 722	9	52	.4 10.8 10.4
9	9.77 078	17	9.86 365	27	0.13 635	9.90 713	9	51	.5 13.5 13.0
10	9.77 095	17	9.86 392	27	0.13 608	9.90 704	9	50	.6 16.2 15.6
11	9.77 112	18	9.86 418	26	0.13 582	9.90 694	10	49	.7 18.2 18.2
12	9.77 130	17	9.86 445	27	0.13 555	9.90 685	9	48	.8 21.6 20.8
13	9.77 147	17	9.86 471	27	0.13 529	9.90 676	9	47	.9 24.3 23.4
14	9.77 164	17	9.86 498	26	0.13 502	9.90 667	10	46	
15	9.77 181	18	9.86 524	27	0.13 470	9.90 657	9	45	.1 1.8
16	9.77 199	17	9.86 551	26	0.13 449	9.90 648	9	44	.2 3.6
17	9.77 216	17	9.86 577	26	0.13 423	9.90 639	9	43	.3 5.4
18	9.77 233	17	9.86 603	27	0.13 397	9.90 630	10	42	.4 7.2
19	9.77 250	18	9.86 630	26	0.13 370	9.90 620	10	41	.5 9.0
20	9.77 268	17	9.86 656	27	0.13 344	9.90 611	9	40	.6 10.8
21	9.77 285	17	9.86 683	26	0.13 317	9.90 602	9	39	.7 12.6
22	9.77 302	17	9.86 709	27	0.13 291	9.90 592	10	38	.8 14.4
23	9.77 319	17	9.86 736	27	0.13 264	9.90 583	9	37	.9 16.2
24	9.77 336	17	9.86 762	27	0.13 238	9.90 574	9	36	
25	9.77 353	17	9.86 789	26	0.13 211	9.90 565		35	
26	9.77 370	17	9.86 815	27	0.13 185	9.90 555	10	34	.1 1.7
27	9.77 387	18	9.86 842	27	0.13 158	9.90 546	9	33	.2 3.4
28	9.77 405	17	9.86 868	26	0.13 132	9.90 537	9	32	.3 5.1
29	9.77 422	17	9.86 894	27	0.13 106	9.90 527	10	31	.4 6.8
30	9.77 439	17	9.86 921	26	0.13 079	9.90 518		30	
31	9.77 456	17	9.86 947	27	0.13 053	9.90 509	9	29	.5 8.5
32	9.77 473	17	9.86 974	26	0.13 026	9.90 499	10	28	.6 10.2
33	9.77 490	17	9.87 000	27	0.13 000	9.90 490	9	27	.7 11.9
34	9.77 507	17	9.87 027	26	0.12 973	9.90 480	10	26	.8 13.6
35	9.77 524	17	9.87 053	26	0.12 947	9.90 471	9	25	.9 15.3
36	9.77 541	17	9.87 079	26	0.12 921	9.90 462	9	24	
37	9.77 558	17	9.87 106	27	0.12 894	9.90 452	10	23	
38	9.77 575	17	9.87 132	26	0.12 868	9.90 443	9	22	
39	9.77 592	17	9.87 158	26	0.12 842	9.90 434	9	21	
40	9.77 609	17	9.87 185	27	0.12 815	9.90 424	10	20	
41	9.77 626	17	9.87 211	26	0.12 789	9.90 415	9	19	.1 1.6
42	9.77 643	17	9.87 238	27	0.12 762	9.90 405	10	18	.2 3.2
43	9.77 660	17	9.87 264	26	0.12 736	9.90 396	9	17	.3 4.8
44	9.77 677	17	9.87 290	27	0.12 710	9.90 386	10	16	.4 6.4
45	9.77 694	17	9.87 317	26	0.12 683	9.90 377	9	15	.5 8.0
46	9.77 711	17	9.87 343	26	0.12 657	9.90 368	9	14	.6 9.6
47	9.77 728	16	9.87 369	27	0.12 631	9.90 358	10	13	.7 11.2
48	9.77 744	17	9.87 396	26	0.12 604	9.90 349	9	12	.8 12.8
49	9.77 761	17	9.87 422	26	0.12 578	9.90 339	10	11	.9 14.4
50	9.77 778	17	9.87 448	27	0.12 552	9.90 330	9	10	
51	9.77 795	17	9.87 475	26	0.12 525	9.90 320	10	9	.1 1.0 0.9
52	9.77 812	17	9.87 501	26	0.12 499	9.90 311	9	8	.2 2.0 1.8
53	9.77 829	17	9.87 527	27	0.12 473	9.90 301	10	7	.3 3.0 2.7
54	9.77 846	16	9.87 554	26	0.12 446	9.90 292	9	6	.4 4.0 3.6
55	9.77 862	17	9.87 580	26	0.12 420	9.90 282	10	5	.5 5.0 4.5
56	9.77 879	17	9.87 606	27	0.12 394	9.90 273	9	4	.6 6.0 5.4
57	9.77 896	17	9.87 633	27	0.12 367	9.90 263	10	3	.7 7.0 6.3
58	9.77 913	17	9.87 659	26	0.12 341	9.90 254	9	2	.8 8.0 7.2
59	9.77 930	17	9.87 685	26	0.12 315	9.90 244	10	1	.9 9.0 8.1
60	9.77 946	16	9.87 711	26	0.12 289	9.90 235	9	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

## 37°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.77 946	17	9.87 711	27	0.12 289	9.90 235	10	60	
1	9.77 963	17	9.87 738	26	0.12 262	9.90 225	9	59	.1 2.7
2	9.77 980	17	9.87 764	26	0.12 236	9.90 216	10	58	.2 5.4
3	9.77 997	16	9.87 790	27	0.12 210	9.90 206	9	57	.3 8.1
4	9.78 013	17	9.87 817	26	0.12 183	9.90 197	10	56	.4 10.8
5	9.78 030	17	9.87 843	26	0.12 157	9.90 187	9	55	.5 13.5
6	9.78 047	16	9.87 869	26	0.12 131	9.90 178	10	54	.6 16.2
7	9.78 063	17	9.87 895	27	0.12 105	9.90 168	9	53	.7 18.9
8	9.78 080	17	9.87 922	26	0.12 078	9.90 159	10	52	.8 21.6
9	9.78 097	16	9.87 948	26	0.12 052	9.90 149	10	51	.9 24.3
10	9.78 113	17	9.87 974	26	0.12 026	9.90 139	9	50	
11	9.78 130	17	9.88 000	27	0.12 000	9.90 130	10	49	.1 2.6
12	9.78 147	16	9.88 027	27	0.11 973	9.90 120	9	48	.2 5.2
13	9.78 163	16	9.88 053	26	0.11 947	9.90 111	10	47	.3 7.8
14	9.78 180	17	9.88 079	26	0.11 921	9.90 101	10	46	.4 10.4
15	9.78 197	16	9.88 105	26	0.11 895	9.90 091	9	45	.5 13.0
16	9.78 213	16	9.88 131	26	0.11 869	9.90 082	10	44	.6 15.6
17	9.78 230	17	9.88 158	26	0.11 842	9.90 072	9	43	.7 18.2
18	9.78 246	16	9.88 184	26	0.11 816	9.90 063	10	42	.8 20.8
19	9.78 263	17	9.88 210	26	0.11 790	9.90 053	10	41	.9 23.4
20	9.78 280	16	9.88 236	26	0.11 764	9.90 043	9	40	
21	9.78 296	16	9.88 262	26	0.11 738	9.90 034	10	39	.1 1.7
22	9.78 313	17	9.88 289	27	0.11 711	9.90 024	10	38	.2 3.4
23	9.78 329	16	9.88 315	26	0.11 685	9.90 014	9	37	.3 5.1
24	9.78 346	16	9.88 341	26	0.11 659	9.90 005	10	36	.4 6.8
25	9.78 362	17	9.88 367	26	0.11 633	9.89 995	10	35	.5 8.5
26	9.78 379	16	9.88 393	26	0.11 607	9.89 985	9	34	.6 10.2
27	9.78 395	17	9.88 420	27	0.11 580	9.89 976	10	33	.7 11.9
28	9.78 412	16	9.88 446	26	0.11 554	9.89 966	10	32	.8 13.6
29	9.78 428	17	9.88 472	26	0.11 528	9.89 956	9	31	.9 15.3
30	9.78 445	16	9.88 498	26	0.11 502	9.89 947	10	30	
31	9.78 461	16	9.88 524	26	0.11 476	9.89 937	10	29	.1 1.7
32	9.78 478	16	9.88 550	26	0.11 450	9.89 927	10	28	.2 3.4
33	9.78 494	16	9.88 577	27	0.11 423	9.89 918	9	27	.3 5.1
34	9.78 510	17	9.88 603	26	0.11 397	9.89 908	10	26	.4 6.8
35	9.78 527	16	9.88 629	26	0.11 371	9.89 898	10	25	.5 8.5
36	9.78 543	17	9.88 655	26	0.11 345	9.89 888	9	24	.6 10.2
37	9.78 560	16	9.88 681	26	0.11 319	9.89 879	10	23	.7 11.9
38	9.78 576	16	9.88 707	26	0.11 293	9.89 869	10	22	.8 13.6
39	9.78 592	17	9.88 733	26	0.11 267	9.89 859	10	21	.9 15.3
40	9.78 609	16	9.88 759	27	0.11 241	9.89 849	9	20	
41	9.78 625	16	9.88 786	27	0.11 214	9.89 840	10	19	.1 4.8
42	9.78 642	17	9.88 812	26	0.11 188	9.89 830	10	18	.2 6.4
43	9.78 658	16	9.88 838	26	0.11 162	9.89 820	10	17	.3 8.0
44	9.78 674	17	9.88 864	26	0.11 136	9.89 810	10	16	.4 9.6
45	9.78 691	16	9.88 890	26	0.11 110	9.89 801	9	15	.5 11.2
46	9.78 707	16	9.88 916	26	0.11 084	9.89 791	10	14	.6 12.8
47	9.78 723	16	9.88 942	26	0.11 058	9.89 781	10	13	.7 14.4
48	9.78 739	16	9.88 968	26	0.11 032	9.89 771	10	12	
49	9.78 756	17	9.88 994	26	0.11 006	9.89 761	10	11	.1 9
50	9.78 772	16	9.89 020	26	0.10 980	9.89 752	10	10	.2 2.0
51	9.78 788	16	9.89 046	26	0.10 954	9.89 742	10	9	.3 2.7
52	9.78 805	17	9.89 073	27	0.10 927	9.89 732	10	8	.4 3.6
53	9.78 821	16	9.89 099	26	0.10 901	9.89 722	10	7	.5 4.5
54	9.78 837	16	9.89 125	26	0.10 875	9.89 712	10	6	.6 5.4
55	9.78 853	16	9.89 151	26	0.10 849	9.89 702	9	5	.7 6.0
56	9.78 869	17	9.89 177	26	0.10 823	9.89 693	10	4	.8 7.0
57	9.78 886	16	9.89 203	26	0.10 797	9.89 683	10	3	.9 8.0
58	9.78 902	16	9.89 229	26	0.10 771	9.89 673	10	2	
59	9.78 918	16	9.89 255	26	0.10 745	9.89 663	10	1	.1 8.1
60	9.78 934	16	9.89 281	26	0.10 719	9.89 653	10	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	'	Prop. Pts.

TABLE IV.

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	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	d.		Prop. Pts.
0	9.78 934	16	9.89 281	26	0.10 719	9.89 653	10	<b>60</b>	
1	9.78 950	17	9.89 307	26	0.10 693	9.89 643	10	59	
2	9.78 967	16	9.89 333	26	0.10 667	9.89 633	10	58	
3	9.78 983	16	9.89 359	26	0.10 641	9.89 624	10	57	.1 2.6 2.5
4	9.78 999	16	9.89 385	26	0.10 615	9.89 614	10	56	.2 5.2 5.0
5	9.79 015	16	9.89 411	26	0.10 589	9.89 604	10	55	.3 7.8 7.5
6	9.79 031	16	9.89 437	26	0.10 563	9.89 594	10	54	.4 10.4 10.0
7	9.79 047	16	9.89 463	26	0.10 537	9.89 584	10	53	.5 13.0 12.5
8	9.79 063	16	9.89 489	26	0.10 511	9.89 574	10	52	.6 15.6 15.0
9	9.79 079	16	9.89 515	26	0.10 485	9.89 564	10	51	.7 18.2 17.5
10	9.79 095	16	9.89 541	26	0.10 459	9.89 554	10	<b>50</b>	.8 20.8 20.0
11	9.79 111	17	9.89 567	26	0.10 433	9.89 544	10	49	.9 23.4 22.5
12	9.79 128	16	9.89 593	26	0.10 407	9.89 534	10	48	
13	9.79 144	16	9.89 619	26	0.10 381	9.89 524	10	47	
14	9.79 160	16	9.89 645	26	0.10 355	9.89 514	10	46	
15	9.79 176	16	9.89 671	26	0.10 329	9.89 504	9	45	.1 1.7
16	9.79 192	16	9.89 697	26	0.10 303	9.89 495	10	44	.2 3.4
17	9.79 208	16	9.89 723	26	0.10 277	9.89 485	10	43	.3 5.1
18	9.79 224	16	9.89 749	26	0.10 251	9.89 475	10	42	.4 6.8
19	9.79 240	16	9.89 775	26	0.10 225	9.89 465	10	41	.5 8.5
20	9.79 256	16	9.89 801	26	0.10 199	9.89 455	10	<b>40</b>	.6 10.2
21	9.79 272	16	9.89 827	26	0.10 173	9.89 445	10	39	.7 11.9
22	9.79 288	16	9.89 853	26	0.10 147	9.89 435	10	38	.8 13.6
23	9.79 304	15	9.89 879	26	0.10 121	9.89 425	10	37	.9 15.3
24	9.79 319	16	9.89 905	26	0.10 095	9.89 415	10	36	
25	9.79 335	16	9.89 931	26	0.10 069	9.89 405	10	35	
26	9.79 351	16	9.89 957	26	0.10 043	9.89 395	10	34	.1 1.6 1.5
27	9.79 367	16	9.89 983	26	0.10 017	9.89 385	10	33	.2 3.2 3.0
28	9.79 383	16	9.90 009	26	0.09 991	9.89 375	10	32	.3 4.8 4.5
29	9.79 399	16	9.90 035	26	0.09 965	9.89 364	10	31	.4 6.4 6.0
30	9.79 415	16	9.90 061	25	0.09 939	9.89 354	10	<b>30</b>	.5 8.0 7.5
31	9.79 431	16	9.90 086	26	0.09 914	9.89 344	10	29	.6 9.6 9.0
32	9.79 447	16	9.90 112	26	0.09 888	9.89 334	10	28	.7 11.2 10.5
33	9.79 463	16	9.90 138	26	0.09 862	9.89 324	10	27	.8 12.8 12.0
34	9.79 478	15	9.90 164	26	0.09 836	9.89 314	10	26	.9 14.4 13.5
35	9.79 494	16	9.90 190	26	0.09 810	9.89 304	10	25	
36	9.79 510	16	9.90 216	26	0.09 784	9.89 294	10	24	
37	9.79 526	16	9.90 242	26	0.09 758	9.89 284	10	23	
38	9.79 542	16	9.90 268	26	0.09 732	9.89 274	10	22	
39	9.79 558	16	9.90 294	26	0.09 706	9.89 264	10	21	
40	9.79 573	15	9.90 320	26	0.09 680	9.89 254	10	<b>20</b>	
41	9.79 589	16	9.90 346	26	0.09 654	9.89 244	10	19	.1 3.3
42	9.79 605	16	9.90 371	25	0.09 629	9.89 233	10	18	.4 4.4
43	9.79 621	16	9.90 397	26	0.09 603	9.89 223	10	17	.5 5.5
44	9.79 636	15	9.90 423	26	0.09 577	9.89 213	10	16	.6 6.6
45	9.79 652	16	9.90 449	26	0.09 551	9.89 203	10	15	.7 7.7
46	9.79 668	16	9.90 475	26	0.09 525	9.89 193	10	14	.8 8.8
47	9.79 684	16	9.90 501	26	0.09 499	9.89 183	10	13	.9 9.9
48	9.79 699	16	9.90 527	26	0.09 473	9.89 173	10	12	
49	9.79 715	16	9.90 553	26	0.09 447	9.89 162	10	11	
50	9.79 731	16	9.90 578	25	0.09 422	9.89 152	10	<b>10</b>	.1 1.0 0.9
51	9.79 746	15	9.90 604	26	0.09 396	9.89 142	10	9	.2 2.0 1.8
52	9.79 762	16	9.90 630	26	0.09 370	9.89 132	10	8	.3 3.0 2.7
53	9.79 778	16	9.90 656	26	0.09 344	9.89 122	10	7	.4 4.0 3.6
54	9.79 793	16	9.90 682	26	0.09 318	9.89 112	10	6	.5 5.0 4.5
55	9.79 809	16	9.90 708	26	0.09 292	9.89 101	10	5	.6 6.0 5.4
56	9.79 825	16	9.90 734	26	0.09 266	9.89 091	10	4	.7 7.0 6.3
57	9.79 840	15	9.90 759	25	0.09 241	9.89 081	10	3	.8 8.0 7.2
58	9.79 856	16	9.90 785	26	0.09 215	9.89 071	10	2	.9 9.0
59	9.79 872	16	9.90 811	26	0.09 189	9.89 060	10	1	
60	9.79 887	15	9.90 837	26	0.09 163	9.89 050	10	<b>0</b>	

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	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.79 887	16	9.90 837	26	0.09 163	9.89 050	10	60	
1	9.79 993	15	9.90 863	26	0.09 137	9.89 040	10	59	
2	9.79 918	16	9.90 889	25	0.09 111	9.89 030	10	58	
3	9.79 934	16	9.90 914	26	0.09 086	9.89 020	11	57	
4	9.79 950	15	9.90 940	26	0.09 060	9.89 009	10	56	.1 2.6
5	9.79 965	16	9.90 966	26	0.09 034	9.88 999	10	55	.2 5.4
6	9.79 981	15	9.90 992	26	0.09 008	9.88 989	11	54	.3 7.8
7	9.79 996	16	9.91 018	25	0.08 982	9.88 978	10	53	.4 10.4
8	9.80 012	15	9.91 043	26	0.08 957	9.88 968	10	52	.5 13.0
9	9.80 027	16	9.91 069	26	0.08 931	9.88 958	10	51	.6 15.6
10	9.80 043	15	9.91 095	26	0.08 905	9.88 948	11	50	.7 18.2
11	9.80 058	16	9.91 121	26	0.08 879	9.88 937	10	49	.8 20.8
12	9.80 074	15	9.91 147	25	0.08 853	9.88 927	10	48	.9 23.4
13	9.80 089	16	9.91 172	26	0.08 828	9.88 917	11	47	
14	9.80 105	15	9.91 198	26	0.08 802	9.88 906	10	46	25
15	9.80 120	16	9.91 224	26	0.08 776	9.88 896	10	45	.1 2.5
16	9.80 136	15	9.91 250	26	0.08 750	9.88 886	11	44	.2 5.0
17	9.80 151	15	9.91 276	25	0.08 724	9.88 875	10	43	.3 7.5
18	9.80 166	16	9.91 301	26	0.08 699	9.88 865	10	42	.4 10.0
19	9.80 182	15	9.91 327	26	0.08 673	9.88 855	11	41	.5 12.5
20	9.80 197	16	9.91 353	26	0.08 647	9.88 844	10	40	.6 15.0
21	9.80 213	15	9.91 379	25	0.08 621	9.88 834	10	39	.7 17.5
22	9.80 228	16	9.91 404	26	0.08 596	9.88 824	10	38	.8 20.0
23	9.80 244	15	9.91 430	26	0.08 570	9.88 813	11	37	.9 22.5
24	9.80 259	15	9.91 456	26	0.08 544	9.88 803	10	36	
25	9.80 274	16	9.91 482	25	0.08 518	9.88 793	11	35	16
26	9.80 290	15	9.91 507	26	0.08 493	9.88 782	10	34	.1 1.6
27	9.80 305	15	9.91 533	26	0.08 467	9.88 772	11	33	.2 3.2
28	9.80 320	16	9.91 559	26	0.08 441	9.88 761	10	32	.3 4.8
29	9.80 336	15	9.91 585	25	0.08 415	9.88 751	10	31	.4 6.4
30	9.80 351	15	9.91 610	26	0.08 390	9.88 741	11	30	.5 8.0
31	9.80 366	16	9.91 636	26	0.08 364	9.88 730	10	29	.6 9.6
32	9.80 382	15	9.91 662	26	0.08 338	9.88 720	10	28	.7 11.2
33	9.80 397	15	9.91 688	25	0.08 312	9.88 709	11	27	.8 12.8
34	9.80 412	16	9.91 713	26	0.08 287	9.88 699	11	26	.9 14.4
35	9.80 428	15	9.91 739	26	0.08 261	9.88 688	10	25	
36	9.80 443	15	9.91 765	26	0.08 235	9.88 678	10	24	
37	9.80 458	15	9.91 791	26	0.08 209	9.88 668	10	23	
38	9.80 473	16	9.91 816	25	0.08 184	9.88 657	11	22	
39	9.80 489	15	9.91 842	26	0.08 158	9.88 647	10	21	
40	9.80 504	15	9.91 868	25	0.08 132	9.88 636	10	20	15
41	9.80 519	15	9.91 893	25	0.08 107	9.88 626	10	19	.1 1.5
42	9.80 534	16	9.91 919	26	0.08 081	9.88 615	11	18	.2 3.0
43	9.80 550	15	9.91 945	26	0.08 055	9.88 605	10	17	.3 4.8
44	9.80 565	15	9.91 971	25	0.08 029	9.88 594	10	16	.4 6.4
45	9.80 580	15	9.91 996	26	0.08 004	9.88 584	11	15	.5 8.0
46	9.80 595	15	9.92 022	26	0.07 978	9.88 573	11	14	.6 9.6
47	9.80 610	15	9.92 048	26	0.07 952	9.88 563	10	13	.7 11.2
48	9.80 625	15	9.92 073	25	0.07 927	9.88 552	11	12	.8 12.8
49	9.80 641	16	9.92 099	26	0.07 901	9.88 542	10	11	.9 14.4
50	9.80 656	15	9.92 125	26	0.07 875	9.88 531	10	10	10
51	9.80 671	15	9.92 150	25	0.07 850	9.88 521	10	9	.1 1.1
52	9.80 686	15	9.92 176	26	0.07 824	9.88 510	11	8	.2 2.2
53	9.80 701	15	9.92 202	25	0.07 798	9.88 499	11	7	.3 3.3
54	9.80 716	15	9.92 227	26	0.07 773	9.88 489	10	6	.4 4.4
55	9.80 731	15	9.92 253	26	0.07 747	9.88 478	11	5	.5 5.5
56	9.80 746	16	9.92 279	26	0.07 721	9.88 468	10	4	.6 6.0
57	9.80 762	15	9.92 304	25	0.07 696	9.88 457	11	3	.7 7.7
58	9.80 777	15	9.92 330	26	0.07 670	9.88 447	10	2	.8 8.8
59	9.80 792	15	9.92 356	25	0.07 644	9.88 436	11	1	.9 9.9
60	9.80 807	15	9.92 381	25	0.07 619	9.88 425	10	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	,	Prop. Pts.

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TABLE IV.

40°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.80 807	15	9.92 381	26	0.07 619	9.88 425	10	60	
1	9.80 822	15	9.92 407	26	0.07 593	9.88 415	11	59	.1 26
2	9.80 837	15	9.92 433	25	0.07 567	9.88 404	10	58	.2 5.2
3	9.80 852	15	9.92 458	26	0.07 542	9.88 394	11	57	.3 7.8
4	9.80 867	15	9.92 484	26	0.07 516	9.88 383	11	56	.4 10.4
5	9.80 882	15	9.92 510	25	0.07 490	9.88 372	10	55	.5 13.0
6	9.80 897	15	9.92 535	26	0.07 465	9.88 362	11	54	.6 15.6
7	9.80 912	15	9.92 561	26	0.07 439	9.88 351	11	53	.7 18.2
8	9.80 927	15	9.92 587	25	0.07 413	9.88 340	10	52	.8 20.8
9	9.80 942	15	9.92 612	26	0.07 388	9.88 330	11	51	.9 23.4
10	9.80 957	15	9.92 638	25	0.07 362	9.88 319	11	50	
11	9.80 972	15	9.92 663	26	0.07 337	9.88 308	10	49	.1 2.5
12	9.80 987	15	9.92 689	26	0.07 311	9.88 298	11	48	.2 5.0
13	9.81 002	15	9.92 715	25	0.07 285	9.88 287	11	47	.3 7.5
14	9.81 017	15	9.92 740	26	0.07 260	9.88 276	10	46	.4 10.0
15	9.81 032	15	9.92 766	26	0.07 234	9.88 266	11	45	.5 12.5
16	9.81 047	14	9.92 792	25	0.07 208	9.88 255	11	44	.6 15.0
17	9.81 061	15	9.92 817	25	0.07 183	9.88 244	10	43	.7 17.5
18	9.81 076	15	9.92 843	26	0.07 157	9.88 234	11	42	.8 20.0
19	9.81 091	15	9.92 868	25	0.07 132	9.88 223	11	41	.9 22.5
20	9.81 106	15	9.92 894	26	0.07 106	9.88 212	11	40	
21	9.81 121	15	9.92 920	25	0.07 080	9.88 201	10	39	.1 1.5
22	9.81 136	15	9.92 945	25	0.07 055	9.88 191	10	38	.2 3.0
23	9.81 151	15	9.92 971	26	0.07 029	9.88 180	11	37	.3 4.5
24	9.81 166	15	9.92 996	25	0.07 004	9.88 169	11	36	.4 6.0
25	9.81 180	15	9.93 022	26	0.06 978	9.88 158	10	35	.5 7.5
26	9.81 195	15	9.93 048	26	0.06 952	9.88 148	11	34	.6 9.0
27	9.81 210	15	9.93 073	25	0.06 927	9.88 137	11	33	.7 10.5
28	9.81 225	15	9.93 099	26	0.06 901	9.88 126	11	32	.8 12.0
29	9.81 240	15	9.93 124	25	0.06 876	9.88 115	10	31	.9 13.5
30	9.81 254	15	9.93 150	26	0.06 850	9.88 105	11	30	
31	9.81 269	15	9.93 175	25	0.06 825	9.88 094	11	29	.1 1.4
32	9.81 284	15	9.93 201	26	0.06 799	9.88 083	11	28	.2 2.8
33	9.81 299	15	9.93 227	26	0.06 773	9.88 072	11	27	.3 4.2
34	9.81 314	15	9.93 252	25	0.06 748	9.88 061	10	26	.4 5.6
35	9.81 328	15	9.93 278	26	0.06 722	9.88 051	11	25	.5 7.0
36	9.81 343	15	9.93 303	25	0.06 697	9.88 040	11	24	.6 8.4
37	9.81 358	15	9.93 329	26	0.06 671	9.88 029	11	23	.7 10.0
38	9.81 372	14	9.93 354	25	0.06 646	9.88 018	11	22	.8 11.4
39	9.81 387	15	9.93 380	26	0.06 620	9.88 007	11	21	.9 12.8
40	9.81 402	15	9.93 406	26	0.06 594	9.87 996	11	20	
41	9.81 417	15	9.93 431	25	0.06 569	9.87 985	11	19	.1 1.5
42	9.81 431	14	9.93 457	25	0.06 543	9.87 975	10	18	.2 3.0
43	9.81 446	15	9.93 482	26	0.06 518	9.87 964	11	17	.3 4.4
44	9.81 461	15	9.93 508	25	0.06 492	9.87 953	11	16	.4 5.8
45	9.81 475	14	9.93 533	25	0.06 467	9.87 942	11	15	.5 7.2
46	9.81 490	15	9.93 559	26	0.06 441	9.87 931	11	14	.6 8.6
47	9.81 505	15	9.93 584	25	0.06 416	9.87 920	11	13	.7 10.0
48	9.81 519	14	9.93 610	26	0.06 390	9.87 909	11	12	.8 11.4
49	9.81 534	15	9.93 636	25	0.06 364	9.87 898	11	11	.9 12.8
50	9.81 549	15	9.93 661	25	0.06 339	9.87 887	10	10	
51	9.81 563	14	9.93 687	26	0.06 313	9.87 877	10	9	.1 1.1
52	9.81 578	15	9.93 712	25	0.06 288	9.87 866	11	8	.2 2.2
53	9.81 592	14	9.93 738	26	0.06 262	9.87 855	11	7	.3 3.6
54	9.81 607	15	9.93 763	25	0.06 237	9.87 844	11	6	.4 4.4
55	9.81 622	14	9.93 789	26	0.06 211	9.87 833	11	5	.5 5.0
56	9.81 636	14	9.93 814	25	0.06 186	9.87 822	11	4	.6 6.0
57	9.81 651	15	9.93 840	26	0.06 160	9.87 811	11	3	.7 7.0
58	9.81 665	14	9.93 865	25	0.06 135	9.87 800	11	2	.8 8.0
59	9.81 680	15	9.93 891	26	0.06 109	9.87 789	11	1	.9 9.0
60	9.81 694	14	9.93 916	25	0.06 084	9.87 778	11	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

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41°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.81 694	15	9.93 916	26	0.06 084	9.87 778	11	60	
1	9.81 709	14	9.93 942	25	0.06 058	9.87 767	11	59	
2	9.81 723	15	9.93 967	26	0.06 033	9.87 756	11	58	
3	9.81 738	14	9.93 993	25	0.06 007	9.87 745	11	57	.1 2.6
4	9.81 752	15	9.94 018	26	0.05 982	9.87 734	11	56	.2 5.2
5	9.81 767	14	9.94 044	25	0.05 956	9.87 723	11	55	.3 7.8
6	9.81 781	15	9.94 069	26	0.05 931	9.87 712	11	54	.4 10.4
7	9.81 796	14	9.94 095	25	0.05 905	9.87 701	11	53	.5 13.0
8	9.81 810	15	9.94 120	26	0.05 880	9.87 690	11	52	.6 15.6
9	9.81 825	14	9.94 146	25	0.05 854	9.87 679	11	51	.7 18.2
10	9.81 839	15	9.94 171	26	0.05 829	9.87 668	11	50	.8 20.8
11	9.81 854	14	9.94 197	25	0.05 803	9.87 657	11	49	.9 23.4
12	9.81 868	14	9.94 222	26	0.05 778	9.87 646	11	48	
13	9.81 882	15	9.94 248	25	0.05 752	9.87 635	11	47	
14	9.81 897	14	9.94 273	26	0.05 727	9.87 624	11	46	
15	9.81 911	15	9.94 299	25	0.05 701	9.87 613	12	45	.1 2.5
16	9.81 926	14	9.94 324	26	0.05 676	9.87 601	11	44	.2 5.0
17	9.81 940	15	9.94 350	25	0.05 650	9.87 590	11	43	.3 7.5
18	9.81 955	14	9.94 375	26	0.05 625	9.87 579	11	42	.4 10.0
19	9.81 969	14	9.94 401	25	0.05 599	9.87 568	11	41	.5 12.5
20	9.81 983	15	9.94 426	26	0.05 574	9.87 557	11	40	.6 15.0
21	9.81 998	14	9.94 452	25	0.05 548	9.87 546	11	39	.7 17.5
22	9.82 012	14	9.94 477	26	0.05 523	9.87 535	11	38	.8 20.0
23	9.82 026	15	9.94 502	25	0.05 497	9.87 524	11	37	.9 22.5
24	9.82 041	14	9.94 528	26	0.05 472	9.87 513	12	36	
25	9.82 055	14	9.94 554	25	0.05 446	9.87 501	11	35	
26	9.82 069	15	9.94 579	25	0.05 421	9.87 490	11	34	I 1.5
27	9.82 084	14	9.94 604	26	0.05 396	9.87 479	11	33	.2 3.0
28	9.82 098	14	9.94 630	25	0.05 370	9.87 468	11	32	.3 4.5
29	9.82 112	14	9.94 655	26	0.05 345	9.87 457	11	31	.4 6.0
30	9.82 126	14	9.94 681	25	0.05 319	9.87 446	12	30	.5 7.5
31	9.82 141	15	9.94 706	26	0.05 294	9.87 434	11	29	.6 9.0
32	9.82 155	14	9.94 732	25	0.05 268	9.87 423	11	28	.7 10.5
33	9.82 169	14	9.94 757	26	0.05 243	9.87 412	11	27	.8 12.0
34	9.82 184	15	9.94 783	25	0.05 217	9.87 401	11	26	.9 13.5
35	9.82 198	14	9.94 808	26	0.05 192	9.87 390	12	25	
36	9.82 212	14	9.94 834	25	0.05 166	9.87 378	11	24	
37	9.82 226	14	9.94 859	25	0.05 141	9.87 367	11	23	
38	9.82 240	15	9.94 884	26	0.05 116	9.87 356	11	22	
39	9.82 255	14	9.94 910	25	0.05 090	9.87 345	11	21	
40	9.82 269	14	9.94 935	26	0.05 065	9.87 334	12	20	
41	9.82 283	14	9.94 961	25	0.05 039	9.87 322	11	19	
42	9.82 297	14	9.94 986	26	0.05 014	9.87 311	11	18	
43	9.82 311	15	9.95 012	25	0.04 988	9.87 300	11	17	
44	9.82 326	14	9.95 037	25	0.04 963	9.87 288	11	16	
45	9.82 340	14	9.95 062	26	0.04 938	9.87 277	11	15	
46	9.82 354	14	9.95 088	25	0.04 912	9.87 266	11	14	
47	9.82 368	14	9.95 113	25	0.04 887	9.87 255	12	13	
48	9.82 382	14	9.95 139	26	0.04 861	9.87 243	11	12	
49	9.82 396	14	9.95 164	26	0.04 836	9.87 232	11	11	
50	9.82 410	14	9.95 190	25	0.04 810	9.87 221	12	10	.1 1.2
51	9.82 424	15	9.95 215	25	0.04 785	9.87 209	11	9	.2 2.4
52	9.82 439	14	9.95 240	26	0.04 760	9.87 198	11	8	.3 3.6
53	9.82 453	14	9.95 266	25	0.04 734	9.87 187	11	7	.4 4.8
54	9.82 467	14	9.95 291	26	0.04 709	9.87 175	12	6	.5 6.0
55	9.82 481	14	9.95 317	25	0.04 683	9.87 164	11	5	.6 7.2
56	9.82 495	14	9.95 342	26	0.04 658	9.87 153	11	4	.7 8.4
57	9.82 509	14	9.95 368	26	0.04 632	9.87 141	12	3	.8 9.6
58	9.82 523	14	9.95 393	25	0.04 607	9.87 130	11	2	.9 10.8
59	9.82 537	14	9.95 418	26	0.04 582	9.87 119	12	1	
60	9.82 551	14	9.95 444	26	0.04 556	9.87 107	12	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	'	Prop. Pts.

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TABLE IV.

42°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.82 551	14	9.95 444	25	0.04 556	9.87 107	11	<b>60</b>	
1	9.82 565	14	9.95 469	26	0.04 531	9.87 096	11	59	.1 2.6
2	9.82 579	14	9.95 495	25	0.04 505	9.87 085	12	58	.2 5.2
3	9.82 593	14	9.95 520	25	0.04 480	9.87 073	11	57	.3 7.8
4	9.82 607	14	9.95 545	26	0.04 455	9.87 062	12	56	.4 10.4
5	9.82 621	14	9.95 571	25	0.04 429	9.87 050	11	55	.5 13.0
6	9.82 635	14	9.95 596	26	0.04 404	9.87 039	11	54	.6 15.6
7	9.82 649	14	9.95 622	25	0.04 378	9.87 028	12	53	.7 18.2
8	9.82 663	14	9.95 647	25	0.04 353	9.87 016	11	52	.8 20.8
9	9.82 677	14	9.95 672	26	0.04 328	9.87 005	12	51	.9 23.4
10	9.82 691	14	9.95 698	25	0.04 302	9.86 993	11	<b>50</b>	
11	9.82 705	14	9.95 723	25	0.04 277	9.86 982	12	49	.1 2.5
12	9.82 719	14	9.95 748	25	0.04 252	9.86 970	11	48	.2 5.0
13	9.82 733	14	9.95 774	25	0.04 226	9.86 959	12	47	.3 7.5
14	9.82 747	14	9.95 799	26	0.04 201	9.86 947	11	46	.4 10.0
15	9.82 761	14	9.95 825	25	0.04 175	9.86 936	12	45	.5 12.5
16	9.82 775	14	9.95 850	25	0.04 150	9.86 924	11	44	.6 15.0
17	9.82 788	13	9.95 875	25	0.04 125	9.86 913	11	43	.7 17.5
18	9.82 802	14	9.95 901	25	0.04 099	9.86 902	12	42	.8 20.0
19	9.82 816	14	9.95 926	26	0.04 074	9.86 890	11	41	.9 22.5
20	9.82 830	14	9.95 952	25	0.04 048	9.86 879	12	<b>40</b>	
21	9.82 844	14	9.95 977	25	0.04 023	9.86 867	12	39	.1 2.5
22	9.82 858	14	9.96 002	25	0.03 998	9.86 855	11	38	.2 5.0
23	9.82 872	13	9.96 028	26	0.03 972	9.86 844	12	37	.3 7.5
24	9.82 885	14	9.96 053	25	0.03 947	9.86 832	11	36	.4 10.0
25	9.82 899	14	9.96 078	26	0.03 922	9.86 821	12	35	.5 12.5
26	9.82 913	14	9.96 104	26	0.03 896	9.86 809	11	34	.6 14.0
27	9.82 927	14	9.96 129	25	0.03 871	9.86 798	12	33	.7 16.5
28	9.82 941	14	9.96 155	26	0.03 845	9.86 786	11	32	.8 19.0
29	9.82 955	13	9.96 180	25	0.03 820	9.86 775	12	31	.9 21.5
30	9.82 968	14	9.96 205	25	0.03 795	9.86 763	11	<b>30</b>	
31	9.82 982	14	9.96 231	25	0.03 769	9.86 752	12	29	.1 2.5
32	9.82 996	14	9.96 256	25	0.03 744	9.86 740	12	28	.2 5.0
33	9.83 010	14	9.96 281	25	0.03 719	9.86 728	11	27	.3 7.5
34	9.83 023	13	9.96 307	25	0.03 693	9.86 717	12	26	.4 10.0
35	9.83 037	14	9.96 332	25	0.03 668	9.86 705	11	25	.5 12.5
36	9.83 051	14	9.96 357	25	0.03 643	9.86 694	12	24	.6 14.0
37	9.83 065	14	9.96 383	26	0.03 617	9.86 682	12	23	.7 16.5
38	9.83 078	13	9.96 408	25	0.03 592	9.86 670	11	22	.8 19.0
39	9.83 092	14	9.96 433	25	0.03 567	9.86 659	12	21	.9 21.5
40	9.83 106	14	9.96 459	25	0.03 541	9.86 647	12	<b>20</b>	
41	9.83 120	13	9.96 484	25	0.03 516	9.86 635	11	19	.1 2.5
42	9.83 133	14	9.96 510	26	0.03 490	9.86 624	11	18	.2 5.0
43	9.83 147	14	9.96 535	25	0.03 465	9.86 612	12	17	.3 7.5
44	9.83 161	13	9.96 560	25	0.03 440	9.86 600	11	16	.4 10.0
45	9.83 174	14	9.96 586	25	0.03 414	9.86 589	12	15	.5 12.5
46	9.83 188	14	9.96 611	25	0.03 389	9.86 577	12	14	.6 14.0
47	9.83 202	14	9.96 636	25	0.03 364	9.86 565	12	13	.7 16.5
48	9.83 215	13	9.96 662	26	0.03 338	9.86 554	11	12	.8 19.0
49	9.83 229	13	9.96 687	25	0.03 313	9.86 542	12	11	.9 21.5
50	9.83 242	13	9.96 712	25	0.03 288	9.86 530	12	<b>10</b>	.1 1.2 1.1
51	9.83 256	14	9.96 738	26	0.03 262	9.86 518	12	9	.2 2.4 2.2
52	9.83 270	14	9.96 763	25	0.03 237	9.86 507	11	8	.3 3.6 3.3
53	9.83 283	13	9.96 788	25	0.03 212	9.86 495	12	7	.4 4.8 4.4
54	9.83 297	14	9.96 814	26	0.03 186	9.86 483	11	6	.5 6.0 5.5
55	9.83 310	14	9.96 839	25	0.03 161	9.86 472	11	5	.6 7.2 6.6
56	9.83 324	14	9.96 864	25	0.03 136	9.86 460	12	4	.7 8.4 7.7
57	9.83 338	13	9.96 890	26	0.03 110	9.86 448	12	3	.8 9.6 8.8
58	9.83 351	13	9.96 915	25	0.03 085	9.86 436	12	2	.9 10.8 9.9
59	9.83 365	14	9.96 940	25	0.03 060	9.86 425	11	1	
60	9.83 378	13	9.96 966	26	0.03 034	9.86 413	12	<b>0</b>	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

## 43°

/	L. Sin.	d.	L. Tang.	e. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.83 378	14	9.96 966	25	0.03 034	9.86 413	12	<b>60</b>	
1	9.83 392	13	9.96 991	25	0.03 009	9.86 401	12	59	
2	9.83 405	14	9.97 016	26	0.02 984	9.86 389	12	58	
3	9.83 419	13	9.97 042	25	0.02 958	9.86 377	12	57	
4	9.83 432	14	9.97 067	25	0.02 933	9.86 366	12	56	.1 2.6
5	9.83 446	13	9.97 092	26	0.02 908	9.86 354	12	55	.2 5.2
6	9.83 459	14	9.97 118	25	0.02 882	9.86 342	12	54	.3 7.8
7	9.83 473	13	9.97 143	25	0.02 857	9.86 330	12	53	4 10.4
8	9.83 486	14	9.97 168	25	0.02 832	9.86 318	12	52	5 13.0
9	9.83 500	13	9.97 193	26	0.02 807	9.86 306	12	51	.6 15.6
10	9.83 513	14	9.97 219	25	0.02 781	9.86 295	12	<b>50</b>	.7 18.2
11	9.83 527	13	9.97 244	25	0.02 756	9.86 283	12	49	.8 20.8
12	9.83 540	14	9.97 269	26	0.02 731	9.86 271	12	48	.9 23.4
13	9.83 554	13	9.97 295	25	0.02 705	9.86 259	12	47	
14	9.83 567	14	9.97 320	25	0.02 680	9.86 247	12	46	
15	9.83 581	13	9.97 345	26	0.02 655	9.86 235	12	45	.1 2.5
16	9.83 594	14	9.97 371	25	0.02 629	9.86 223	12	44	.2 5.0
17	9.83 608	13	9.97 396	25	0.02 604	9.86 211	12	43	.3 7.5
18	9.83 621	13	9.97 421	26	0.02 579	9.86 200	12	42	4 10.0
19	9.83 634	14	9.97 447	25	0.02 553	9.86 188	12	41	.5 12.5
20	9.83 648	13	9.97 472	25	0.02 528	9.86 176	12	<b>40</b>	.6 15.0
21	9.83 661	13	9.97 497	26	0.02 503	9.86 164	12	39	.7 17.5
22	9.83 674	14	9.97 523	25	0.02 477	9.86 152	12	38	.8 20.0
23	9.83 688	13	9.97 548	25	0.02 452	9.86 140	12	37	.9 22.5
24	9.83 701	14	9.97 573	25	0.02 427	9.86 128	12	36	
25	9.83 715	13	9.97 598	26	0.02 402	9.86 116	12	35	
26	9.83 728	13	9.97 624	25	0.02 376	9.86 104	12	34	.1 1.4
27	9.83 741	14	9.97 649	25	0.02 351	9.86 092	12	33	.2 2.8
28	9.83 755	13	9.97 674	26	0.02 326	9.86 080	12	32	.3 4.2
29	9.83 768	13	9.97 700	25	0.02 300	9.86 068	12	31	.4 5.6
30	9.83 781	14	9.97 725	25	0.02 275	9.86 056	12	<b>30</b>	.5 7.0
31	9.83 795	13	9.97 750	26	0.02 250	9.86 044	12	29	.6 8.4
32	9.83 808	13	9.97 776	26	0.02 224	9.86 032	12	28	.7 9.8
33	9.83 821	13	9.97 801	25	0.02 199	9.86 020	12	27	.8 11.2
34	9.83 834	14	9.97 826	25	0.02 174	9.86 008	12	26	.9 12.6
35	9.83 848	13	9.97 851	26	0.02 149	9.85 996	12	25	
36	9.83 861	13	9.97 877	25	0.02 123	9.85 984	12	24	
37	9.83 874	13	9.97 902	25	0.02 098	9.85 972	12	23	
38	9.83 887	14	9.97 927	26	0.02 073	9.85 960	12	22	
39	9.83 901	13	9.97 953	25	0.02 047	9.85 948	12	21	
40	9.83 914	13	9.97 978	25	0.02 022	9.85 936	12	<b>20</b>	
41	9.83 927	13	9.98 003	26	0.01 997	9.85 924	12	19	.1 3.9
42	9.83 940	13	9.98 029	25	0.01 971	9.85 912	12	18	.2 5.2
43	9.83 954	13	9.98 054	25	0.01 946	9.85 900	12	17	.3 6.5
44	9.83 967	13	9.98 079	25	0.01 921	9.85 888	12	16	.4 7.8
45	9.83 980	13	9.98 104	26	0.01 896	9.85 876	12	15	.5 9.1
46	9.83 993	13	9.98 130	25	0.01 870	9.85 864	12	14	.6 10.4
47	9.84 006	13	9.98 155	25	0.01 845	9.85 851	13	13	.7 11.7
48	9.84 020	14	9.98 180	25	0.01 820	9.85 839	12	12	
49	9.84 033	13	9.98 206	26	0.01 794	9.85 827	12	<b>11</b>	
50	9.84 046	13	9.98 231	25	0.01 769	9.85 815	12	<b>10</b>	
51	9.84 059	13	9.98 256	25	0.01 744	9.85 803	12	9	.1 1.1
52	9.84 072	13	9.98 281	25	0.01 719	9.85 791	12	8	.2 2.2
53	9.84 085	13	9.98 307	26	0.01 693	9.85 779	12	7	.3 3.3
54	9.84 098	14	9.98 332	25	0.01 668	9.85 766	13	6	.4 4.4
55	9.84 112	13	9.98 357	26	0.01 643	9.85 754	12	5	.5 5.5
56	9.84 125	13	9.98 383	25	0.01 617	9.85 742	12	4	.6 6.6
57	9.84 138	13	9.98 408	25	0.01 592	9.85 730	12	3	.7 7.7
58	9.84 151	13	9.98 433	25	0.01 567	9.85 718	12	2	.8 8.8
59	9.84 164	13	9.98 458	26	0.01 542	9.85 706	13	<b>1</b>	.9 9.9
60	9.84 177	13	9.98 484	26	0.01 516	9.85 693	13	<b>0</b>	
	L. Cos.	d.	L. Cotg.	e. d.	L. Tang.	L. Sin.	d.	/	Prop. Pts.

## 46°

44°

	L. Sin.	d.	L. Tang.	c. d.	L. Cotg.	L. Cos.	d.		Prop. Pts.
0	9.84 177	13	9.98 484	25	0.01 516	9.85 693	12	60	
1	9.84 190	13	9.98 509	25	0.01 491	9.85 681	12	59	.1 2.6
2	9.84 203	13	9.98 534	26	0.01 466	9.85 669	12	58	.2 5.2
3	9.84 216	13	9.98 560	25	0.01 440	9.85 657	12	57	.3 7.8
4	9.84 229	13	9.98 585	25	0.01 415	9.85 645	13	56	.4 10.4
5	9.84 242	13	9.98 610	25	0.01 390	9.85 632	12	55	.5 13.0
6	9.84 255	14	9.98 635	26	0.01 365	9.85 620	12	54	.6 15.6
7	9.84 269	13	9.98 661	25	0.01 339	9.85 608	12	53	.7 18.2
8	9.84 282	13	9.98 686	25	0.01 314	9.85 596	13	52	.8 20.8
9	9.84 295	13	9.98 711	26	0.01 289	9.85 583	12	51	.9 23.4
10	9.84 308	13	9.98 737	25	0.01 263	9.85 571	12	50	
11	9.84 321	13	9.98 762	25	0.01 238	9.85 559	12	49	
12	9.84 334	13	9.98 787	25	0.01 213	9.85 547	12	48	
13	9.84 347	13	9.98 812	26	0.01 188	9.85 534	13	47	
14	9.84 360	13	9.98 838	25	0.01 162	9.85 522	12	46	
15	9.84 373	12	9.98 863	25	0.01 137	9.85 510	13	45	.1 2.5
16	9.84 385	12	9.98 888	25	0.01 112	9.85 497	12	44	.2 5.0
17	9.84 398	13	9.98 913	25	0.01 087	9.85 485	12	43	.3 7.5
18	9.84 411	13	9.98 939	25	0.01 061	9.85 473	13	42	.4 10.0
19	9.84 424	13	9.98 964	25	0.01 036	9.85 460	12	41	.5 12.5
20	9.84 437	13	9.98 989	26	0.01 011	9.85 448	12	40	.6 15.0
21	9.84 450	13	9.99 015	26	0.00 985	9.85 436	12	39	.7 17.5
22	9.84 463	13	9.99 040	25	0.00 960	9.85 423	13	38	.8 20.0
23	9.84 476	13	9.99 065	25	0.00 935	9.85 411	12	37	.9 22.5
24	9.84 489	13	9.99 090	25	0.00 910	9.85 399	13	36	
25	9.84 502	13	9.99 116	25	0.00 884	9.85 386	12	35	
26	9.84 515	13	9.99 141	25	0.00 859	9.85 374	13	34	.1 1.4
27	9.84 528	12	9.99 166	25	0.00 834	9.85 361	12	33	.2 2.8
28	9.84 540	13	9.99 191	25	0.00 809	9.85 349	12	32	.3 4.2
29	9.84 553	13	9.99 217	26	0.00 783	9.85 337	13	31	.4 5.6
30	9.84 566	13	9.99 242	25	0.00 758	9.85 324	12	30	.5 7.0
31	9.84 579	13	9.99 267	25	0.00 733	9.85 312	13	29	.6 8.4
32	9.84 592	13	9.99 293	25	0.00 707	9.85 299	12	28	.7 9.8
33	9.84 605	13	9.99 318	25	0.00 682	9.85 287	13	27	.8 11.2
34	9.84 618	13	9.99 343	25	0.00 657	9.85 274	13	26	.9 12.6
35	9.84 630	13	9.99 368	26	0.00 632	9.85 262	12	25	
36	9.84 643	13	9.99 394	26	0.00 606	9.85 250	13	24	
37	9.84 656	13	9.99 419	25	0.00 581	9.85 237	12	23	
38	9.84 669	13	9.99 444	25	0.00 556	9.85 225	12	22	
39	9.84 682	12	9.99 469	25	0.00 531	9.85 212	13	21	
40	9.84 694	13	9.99 495	25	0.00 505	9.85 200	13	20	
41	9.84 707	13	9.99 520	25	0.00 480	9.85 187	12	19	.1 3.9
42	9.84 720	13	9.99 545	25	0.00 455	9.85 175	12	18	.2 5.2
43	9.84 733	13	9.99 570	26	0.00 430	9.85 162	13	17	.3 6.5
44	9.84 745	13	9.99 596	25	0.00 404	9.85 150	12	16	.4 7.8
45	9.84 758	13	9.99 621	25	0.00 379	9.85 137	12	15	.5 9.1
46	9.84 771	13	9.99 646	25	0.00 354	9.85 125	13	14	.6 10.4
47	9.84 784	13	9.99 672	26	0.00 328	9.85 112	13	13	.7 11.7
48	9.84 796	12	9.99 697	25	0.00 303	9.85 100	12	12	
49	9.84 809	13	9.99 722	25	0.00 278	9.85 087	13	11	
50	9.84 822	13	9.99 747	25	0.00 253	9.85 074	12	10	.1 1.2
51	9.84 835	12	9.99 773	26	0.00 227	9.85 062	13	9	.2 2.4
52	9.84 847	13	9.99 798	25	0.00 202	9.85 049	13	8	.3 3.6
53	9.84 860	13	9.99 823	25	0.00 177	9.85 037	12	7	.4 4.8
54	9.84 873	12	9.99 848	25	0.00 152	9.85 024	13	6	.5 6.0
55	9.84 885	13	9.99 874	26	0.00 126	9.85 012	13	5	.6 7.2
56	9.84 898	13	9.99 899	25	0.00 101	9.84 999	13	4	.7 8.4
57	9.84 911	13	9.99 924	25	0.00 076	9.84 986	13	3	.8 9.6
58	9.84 923	12	9.99 949	26	0.00 051	9.84 974	12	2	.9 10.8
59	9.84 936	13	9.99 975	25	0.00 025	9.84 961	13	1	
60	9.84 949	13	0.00 000	25	0.00 000	9.84 949	12	0	
	L. Cos.	d.	L. Cotg.	c. d.	L. Tang.	L. Sin.	d.		Prop. Pts.

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**TABLE V.****NATURAL****SINES AND COSINES.**

TABLE V.

	0°		1°		2°		3°		4°		
	N. sine	N. cos.									
0	.00000	1.00000	.01745	.99985	.03490	.99939	.05234	.99863	.06976	.99756	60
1	.00029	1.00000	.01774	.99984	.03519	.99938	.05263	.99861	.07005	.99754	59
2	.00058	1.00000	.01803	.99984	.03548	.99937	.05292	.99860	.07034	.99752	58
3	.00087	1.00000	.01832	.99983	.03577	.99936	.05321	.99858	.07063	.99750	57
4	.00116	1.00000	.01862	.99983	.03606	.99935	.05350	.99857	.07092	.99748	56
5	.00145	1.00000	.01891	.99982	.03635	.99934	.05379	.99855	.07121	.99746	55
6	.00175	1.00000	.01920	.99982	.03664	.99933	.05408	.99854	.07150	.99744	54
7	.00204	1.00000	.01949	.99981	.03693	.99932	.05437	.99852	.07179	.99742	53
8	.00233	1.00000	.01978	.99980	.03723	.99931	.05466	.99851	.07208	.99740	52
9	.00262	1.00000	.02007	.99980	.03752	.99930	.05495	.99849	.07237	.99738	51
10	.00291	1.00000	.02036	.99979	.03781	.99929	.05524	.99847	.07266	.99736	50
11	.00320	.99999	.02065	.99979	.03810	.99927	.05553	.99846	.07295	.99734	49
12	.00349	.99999	.02094	.99978	.03839	.99926	.05582	.99844	.07324	.99731	48
13	.00378	.99999	.02123	.99977	.03868	.99925	.05611	.99842	.07353	.99729	47
14	.00407	.99999	.02152	.99977	.03897	.99924	.05640	.99841	.07382	.99727	46
15	.00436	.99999	.02181	.99976	.03926	.99923	.05669	.99839	.07411	.99725	45
16	.00465	.99999	.02211	.99976	.03955	.99922	.05698	.99838	.07440	.99723	44
17	.00495	.99999	.02240	.99975	.03984	.99921	.05727	.99836	.07469	.99721	43
18	.00524	.99999	.02269	.99974	.04013	.99919	.05756	.99834	.07498	.99719	42
19	.00553	.99998	.02298	.99974	.04042	.99918	.05785	.99833	.07527	.99716	41
20	.00582	.99998	.02327	.99973	.04071	.99917	.05814	.99831	.07556	.99714	40
21	.00611	.99998	.02356	.99972	.04100	.99916	.05844	.99829	.07585	.99712	39
22	.00640	.99998	.02385	.99972	.04129	.99915	.05873	.99827	.07614	.99710	38
23	.00669	.99998	.02414	.99971	.04159	.99913	.05902	.99826	.07643	.99708	37
24	.00698	.99998	.02443	.99970	.04188	.99912	.05931	.99824	.07672	.99705	36
25	.00727	.99997	.02472	.99969	.04217	.99911	.05960	.99822	.07701	.99703	35
26	.00756	.99997	.02501	.99969	.04246	.99910	.05989	.99821	.07730	.99701	34
27	.00785	.99997	.02530	.99968	.04275	.99909	.06018	.99819	.07759	.99699	33
28	.00814	.99997	.02560	.99967	.04304	.99907	.06047	.99817	.07788	.99696	32
29	.00844	.99996	.02589	.99966	.04333	.99906	.06076	.99815	.07817	.99694	31
30	.00873	.99996	.02618	.99966	.04362	.99905	.06105	.99813	.07846	.99692	30
31	.00902	.99996	.02647	.99965	.04391	.99904	.06134	.99812	.07875	.99689	29
32	.00931	.99996	.02676	.99964	.04420	.99902	.06163	.99810	.07904	.99687	28
33	.00960	.99995	.02705	.99963	.04449	.99901	.06192	.99808	.07933	.99685	27
34	.00989	.99995	.02734	.99963	.04478	.99900	.06221	.99806	.07962	.99683	26
35	.01018	.99995	.02763	.99962	.04507	.99898	.06250	.99804	.07991	.99680	25
36	.01047	.99995	.02792	.99961	.04536	.99897	.06279	.99803	.08020	.99678	24
37	.01076	.99994	.02821	.99960	.04565	.99896	.06308	.99801	.08049	.99676	23
38	.01105	.99994	.02850	.99959	.04594	.99894	.06337	.99799	.08078	.99673	22
39	.01134	.99994	.02879	.99959	.04623	.99893	.06366	.99797	.08107	.99671	21
40	.01164	.99993	.02908	.99958	.04653	.99892	.06395	.99795	.08136	.99668	20
41	.01193	.99993	.02938	.99957	.04682	.99890	.06424	.99793	.08165	.99666	19
42	.01222	.99993	.02967	.99956	.04711	.99889	.06453	.99792	.08194	.99664	18
43	.01251	.99992	.02996	.99955	.04740	.99888	.06482	.99790	.08223	.99661	17
44	.01280	.99992	.03025	.99954	.04760	.99886	.06511	.99788	.08252	.99659	16
45	.01309	.99991	.03054	.99953	.04798	.99885	.06540	.99786	.08281	.99657	15
46	.01338	.99991	.03083	.99952	.04827	.99883	.06569	.99784	.08310	.99654	14
47	.01367	.99991	.03112	.99952	.04856	.99882	.06598	.99782	.08339	.99652	13
48	.01396	.99990	.03141	.99951	.04885	.99881	.06627	.99780	.08368	.99649	12
49	.01425	.99990	.03170	.99950	.04914	.99879	.06656	.99778	.08397	.99647	11
50	.01454	.99989	.03199	.99949	.04943	.99878	.06685	.99776	.08426	.99644	10
51	.01483	.99989	.03228	.99948	.04972	.99876	.06714	.99774	.08455	.99642	9
52	.01513	.99989	.03257	.99947	.05001	.99875	.06743	.99772	.08484	.99639	8
53	.01542	.99988	.03286	.99946	.05030	.99873	.06773	.99770	.08513	.99637	7
54	.01571	.99988	.03316	.99945	.05059	.99872	.06802	.99768	.08542	.99635	6
55	.01600	.99987	.03345	.99944	.05088	.99870	.06831	.99766	.08571	.99632	5
56	.01629	.99987	.03374	.99943	.05117	.99869	.06860	.99764	.08600	.99630	4
57	.01658	.99986	.03403	.99942	.05146	.99867	.06889	.99762	.08620	.99627	3
58	.01687	.99986	.03432	.99941	.05175	.99865	.06918	.99760	.08655	.99625	2
59	.01716	.99985	.03461	.99940	.05205	.99864	.06947	.99758	.08687	.99622	1
60	.01745	.99985	.03490	.99939	.05234	.99863	.06976	.99756	.08716	.99619	0
	N. cos.	N. sine	,								
	89°	88°	87°	86°	85°						

## NATURAL SINES AND COSINES.

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	5°		6°		7°		8°		9°		
	N. sine	N. cos.									
0	.08716	.99619	.10453	.99452	.12187	.99255	.13917	.99027	.15643	.98769	60
1	.08745	.99617	.10482	.99449	.12216	.99251	.13946	.99023	.15072	.98764	59
2	.08774	.99614	.10511	.99446	.12245	.99248	.13975	.99019	.15701	.98760	58
3	.08803	.99612	.10540	.99443	.12274	.99244	.14004	.99015	.15730	.98755	57
4	.08831	.99609	.10569	.99440	.12302	.99240	.14033	.99011	.15758	.98751	56
5	.08860	.99607	.10597	.99437	.12331	.99237	.14061	.99006	.15787	.98746	55
6	.08889	.99604	.10626	.99434	.12360	.99233	.14090	.99002	.15816	.98741	54
7	.08918	.99602	.10655	.99431	.12389	.99230	.14119	.98998	.15845	.98737	53
8	.08947	.99599	.10684	.99428	.12418	.99226	.14148	.98994	.15873	.98732	52
9	.08976	.99596	.10713	.99424	.12447	.99222	.14177	.98990	.15902	.98728	51
10	.09005	.99594	.10742	.99421	.12476	.99219	.14205	.98986	.15931	.98723	50
11	.09034	.99591	.10771	.99418	.12504	.99215	.14234	.98982	.15959	.98718	49
12	.09063	.99588	.10800	.99415	.12533	.99211	.14263	.98978	.15988	.98714	48
13	.09092	.99586	.10829	.99412	.12562	.99208	.14292	.98973	.16017	.98709	47
14	.09121	.99583	.10858	.99409	.12591	.99204	.14320	.98969	.16046	.98704	46
15	.09150	.99580	.10887	.99406	.12620	.99200	.14349	.98965	.16074	.98700	45
16	.09179	.99578	.10916	.99402	.12649	.99197	.14378	.98961	.16103	.98695	44
17	.09208	.99575	.10945	.99399	.12678	.99193	.14407	.98957	.16132	.98690	43
18	.09237	.99572	.10973	.99396	.12706	.99189	.14436	.98953	.16160	.98686	42
19	.09266	.99570	.11002	.99393	.12735	.99186	.14464	.98948	.16189	.98681	41
20	.09295	.99567	.11031	.99390	.12764	.99182	.14493	.98944	.16218	.98676	40
21	.09324	.99564	.11060	.99386	.12793	.99178	.14522	.98940	.16246	.98671	39
22	.09353	.99562	.11089	.99383	.12822	.99175	.14551	.98936	.16275	.98667	38
23	.09382	.99559	.11118	.99380	.12851	.99171	.14580	.98931	.16304	.98662	37
24	.09411	.99556	.11147	.99377	.12880	.99167	.14608	.98927	.16333	.98657	36
25	.09440	.99553	.11176	.99374	.12908	.99163	.14637	.98923	.16361	.98652	35
26	.09469	.99551	.11205	.99370	.12937	.99160	.14666	.98919	.16390	.98648	34
27	.09498	.99548	.11234	.99367	.12966	.99156	.14695	.98914	.16419	.98643	33
28	.09527	.99545	.11263	.99364	.12995	.99152	.14723	.98910	.16447	.98638	32
29	.09556	.99542	.11291	.99360	.13024	.99148	.14752	.98906	.16476	.98633	31
30	.09585	.99540	.11320	.99357	.13053	.99144	.14781	.98902	.16505	.98629	30
31	.09614	.99537	.11349	.99354	.13081	.99141	.14810	.98897	.16533	.98624	29
32	.09642	.99534	.11378	.99351	.13110	.99137	.14838	.98893	.16562	.98619	28
33	.09671	.99531	.11407	.99347	.13139	.99133	.14867	.98889	.16591	.98614	27
34	.09700	.99528	.11436	.99344	.13168	.99129	.14896	.98884	.16620	.98609	26
35	.09729	.99526	.11465	.99341	.13197	.99125	.14925	.98880	.16648	.98604	25
36	.09758	.99523	.11494	.99337	.13226	.99122	.14954	.98876	.16677	.98600	24
37	.09787	.99520	.11523	.99334	.13254	.99118	.14982	.98871	.16706	.98595	23
38	.09816	.99517	.11552	.99331	.13283	.99114	.15011	.98867	.16734	.98590	22
39	.09845	.99514	.11580	.99327	.13312	.99110	.15040	.98863	.16763	.98585	21
40	.09874	.99511	.11609	.99324	.13341	.99106	.15069	.98858	.16792	.98580	20
41	.09903	.99508	.11638	.99320	.13370	.99102	.15097	.98854	.16820	.98575	19
42	.09932	.99506	.11667	.99317	.13399	.99098	.15126	.98849	.16849	.98570	18
43	.09961	.99503	.11696	.99314	.13427	.99094	.15155	.98845	.16878	.98565	17
44	.09990	.99500	.11725	.99310	.13456	.99091	.15184	.98841	.16906	.98561	16
45	.10019	.99497	.11754	.99307	.13485	.99087	.15212	.98836	.16935	.98556	15
46	.10048	.99494	.11783	.99303	.13514	.99083	.15241	.98832	.16964	.98551	14
47	.10077	.99491	.11812	.99300	.13543	.99079	.15270	.98827	.16992	.98546	13
48	.10106	.99488	.11840	.99297	.13572	.99075	.15299	.98823	.17021	.98541	12
49	.10135	.99485	.11869	.99293	.13600	.99071	.15327	.98818	.17050	.98536	11
50	.10164	.99482	.11898	.99290	.13629	.99067	.15356	.98814	.17078	.98531	10
51	.10192	.99479	.11927	.99286	.13658	.99063	.15385	.98809	.17107	.98526	9
52	.10221	.99476	.11956	.99283	.13687	.99059	.15414	.98805	.17136	.98521	8
53	.10250	.99473	.11985	.99279	.13716	.99055	.15442	.98800	.17164	.98516	7
54	.10279	.99470	.12014	.99276	.13744	.99051	.15471	.98796	.17193	.98511	6
55	.10308	.99467	.12043	.99272	.13773	.99047	.15500	.98791	.17222	.98506	5
56	.10337	.99464	.12071	.99269	.13802	.99043	.15529	.98787	.17250	.98501	4
57	.10366	.99461	.12100	.99265	.13831	.99039	.15557	.98782	.17279	.98496	3
58	.10395	.99458	.12129	.99262	.13860	.99035	.15586	.98778	.17308	.98491	2
59	.10424	.99455	.12158	.99258	.13889	.99031	.15615	.98773	.17336	.98486	1
60	.10453	.99452	.12187	.99255	.13917	.99027	.15643	.98769	.17365	.98481	0
	N. cos.	N. sine	/								
	84°	83°	82°	81°	80°						

TABLE V.

	10°		11°		12°		13°		14°		
	N. sine	N. cos.									
0	.17365	.98481	.19081	.98163	.20791	.97815	.22495	.97437	.24192	.97030	60
1	.17393	.98476	.19109	.98157	.20820	.97809	.22523	.97430	.24220	.97023	59
2	.17422	.98471	.19138	.98152	.20848	.97803	.22552	.97424	.24249	.97015	58
3	.17451	.98466	.19167	.98146	.20877	.97797	.22580	.97417	.24277	.97008	57
4	.17479	.98461	.19195	.98140	.20905	.97791	.22608	.97411	.24305	.97001	56
5	.17508	.98455	.19224	.98135	.20933	.97784	.22637	.97404	.24333	.96994	55
6	.17537	.98450	.19252	.98129	.20962	.97778	.22665	.97398	.24362	.96987	54
7	.17565	.98445	.19281	.98124	.20990	.97772	.22693	.97391	.24390	.96980	53
8	.17594	.98440	.19309	.98118	.21019	.97766	.22722	.97384	.24418	.96973	52
9	.17623	.98435	.19338	.98112	.21047	.97760	.22750	.97378	.24446	.96966	51
10	.17651	.98430	.19366	.98107	.21076	.97754	.22778	.97371	.24474	.96959	50
11	.17680	.98425	.19395	.98101	.21104	.97748	.22807	.97365	.24503	.96952	49
12	.17708	.98420	.19423	.98096	.21132	.97742	.22835	.97358	.24531	.96945	48
13	.17737	.98414	.19452	.98090	.21161	.97735	.22863	.97351	.24559	.96937	47
14	.17766	.98409	.19481	.98084	.21189	.97729	.22892	.97345	.24587	.96930	46
15	.17794	.98404	.19509	.98079	.21218	.97723	.22920	.97338	.24615	.96923	45
16	.17823	.98399	.19538	.98073	.21246	.97717	.22948	.97331	.24644	.96916	44
17	.17852	.98394	.19566	.98067	.21275	.97711	.22977	.97325	.24672	.96909	43
18	.17880	.98389	.19595	.98061	.21303	.97705	.23005	.97318	.24700	.96902	42
19	.17909	.98383	.19623	.98056	.21331	.97698	.23033	.97311	.24728	.96894	41
20	.17937	.98378	.19652	.98050	.21360	.97692	.23062	.97304	.24756	.96887	40
21	.17966	.98373	.19680	.98044	.21388	.97686	.23090	.97298	.24784	.96880	39
22	.17995	.98368	.19709	.98039	.21417	.97680	.23118	.97291	.24813	.96873	38
23	.18023	.98362	.19737	.98033	.21445	.97673	.23146	.97284	.24841	.96866	37
24	.18052	.98357	.19766	.98027	.21474	.97667	.23175	.97278	.24869	.96858	36
25	.18081	.98352	.19794	.98021	.21502	.97661	.23203	.97271	.24897	.96851	35
26	.18109	.98347	.19823	.98016	.21530	.97655	.23231	.97264	.24925	.96844	34
27	.18138	.98341	.19851	.98010	.21559	.97648	.23260	.97257	.24954	.96837	33
28	.18166	.98336	.19880	.98004	.21587	.97642	.23288	.97251	.24982	.96829	32
29	.18195	.98331	.19908	.97998	.21616	.97636	.23316	.97244	.25010	.96822	31
30	.18224	.98325	.19937	.97992	.21644	.97630	.23345	.97237	.25038	.96815	30
31	.18252	.98320	.19965	.97987	.21672	.97623	.23373	.97230	.25066	.96807	29
32	.18281	.98315	.19994	.97981	.21701	.97617	.23401	.97223	.25094	.96800	28
33	.18309	.98310	.20022	.97975	.21729	.97611	.23429	.97217	.25122	.96793	27
34	.18338	.98304	.20051	.97969	.21758	.97604	.23458	.97210	.25151	.96786	26
35	.18367	.98309	.20079	.97963	.21786	.97598	.23486	.97203	.25179	.96778	25
36	.18395	.98294	.20108	.97958	.21814	.97592	.23514	.97196	.25207	.96771	24
37	.18424	.98288	.20136	.97952	.21843	.97585	.23542	.97189	.25235	.96764	23
38	.18452	.98283	.20165	.97946	.21871	.97579	.23571	.97182	.25263	.96756	22
39	.18481	.98277	.20193	.97940	.21899	.97573	.23599	.97176	.25291	.96749	21
40	.18509	.98272	.20222	.97934	.21928	.97566	.23627	.97169	.25320	.96742	20
41	.18538	.98267	.20250	.97928	.21956	.97560	.23656	.97162	.25348	.96734	19
42	.18567	.98261	.20279	.97922	.21985	.97553	.23684	.97155	.25376	.96727	18
43	.18595	.98256	.20307	.97916	.22013	.97547	.23712	.97148	.25404	.96719	17
44	.18624	.98250	.20336	.97910	.22041	.97541	.23740	.97141	.25432	.96712	16
45	.18652	.98245	.20364	.97905	.22070	.97534	.23769	.97134	.25460	.96705	15
46	.18681	.98240	.20393	.97899	.22098	.97528	.23797	.97127	.25488	.96697	14
47	.18710	.98234	.20421	.97893	.22126	.97521	.23825	.97120	.25516	.96690	13
48	.18738	.98220	.20450	.97887	.22155	.97515	.23853	.97113	.25545	.96682	12
49	.18767	.98223	.20478	.97881	.22183	.97508	.23882	.97106	.25573	.96675	11
50	.18795	.98218	.20507	.97875	.22212	.97502	.23910	.97100	.25601	.96667	10
51	.18824	.98212	.20535	.97869	.22240	.97496	.23938	.97093	.25620	.96660	9
52	.18852	.98207	.20563	.97863	.22268	.97489	.23966	.97086	.25657	.96653	8
53	.18881	.98201	.20592	.97857	.22297	.97483	.23995	.97079	.25685	.96645	7
54	.18910	.98196	.20620	.97851	.22325	.97476	.24023	.97072	.25713	.96638	6
55	.18938	.98190	.20649	.97845	.22353	.97470	.24051	.97065	.25741	.96630	5
56	.18967	.98185	.20677	.97839	.22382	.97463	.24079	.97058	.25760	.96623	4
57	.18995	.98179	.20706	.97833	.22410	.97457	.24108	.97051	.25798	.96615	3
58	.19024	.98174	.20734	.97827	.22438	.97450	.24136	.97044	.25826	.96608	2
59	.19052	.98168	.20763	.97821	.22467	.97444	.24164	.97037	.25854	.96600	1
60	.19081	.98163	.20791	.97815	.22495	.97437	.24192	.97030	.25882	.96593	0
	N. cos.	N. sine	/								
	79°	78°	77°	76°	75°						

## NATURAL SINES AND COSINES.

79

	15°		16°		17°		18°		19°		
/	N. sine	N. cos.									
0	.25882	.96593	.27564	.96126	.29237	.95630	.30902	.95106	.32557	.94552	60
1	.25910	.96585	.27592	.96118	.29265	.95622	.30929	.95097	.32584	.94542	59
2	.25938	.96578	.27620	.96110	.29293	.95613	.30957	.95088	.32612	.94533	58
3	.25966	.96570	.27648	.96102	.29321	.95605	.30985	.95079	.32639	.94523	57
4	.25994	.96562	.27676	.96094	.29348	.95596	.31012	.95070	.32667	.94514	56
5	.26022	.96555	.27704	.96086	.29376	.95588	.31040	.95061	.32694	.94504	55
6	.26050	.96547	.27731	.96078	.29404	.95579	.31068	.95052	.32722	.94495	54
7	.26079	.96540	.27759	.96070	.29432	.95571	.31095	.95043	.32749	.94485	53
8	.26107	.96532	.27787	.96062	.29460	.95562	.31123	.95033	.32777	.94476	52
9	.26135	.96524	.27815	.96054	.29487	.95554	.31151	.95024	.32804	.94466	51
10	.26163	.96517	.27843	.96046	.29515	.95545	.31178	.95015	.32832	.94457	50
11	.26191	.96500	.27871	.96037	.29543	.95536	.31206	.95006	.32859	.94447	49
12	.26219	.96502	.27899	.96029	.29571	.95528	.31233	.94997	.32887	.94438	48
13	.26247	.96494	.27927	.96021	.29599	.95519	.31261	.94988	.32914	.94428	47
14	.26275	.96486	.27955	.96013	.29626	.95511	.31289	.94979	.32942	.94418	46
15	.26303	.96479	.27983	.96005	.29654	.95502	.31316	.94970	.32969	.94409	45
16	.26331	.96471	.28011	.95997	.29682	.95493	.31344	.94961	.32997	.94399	44
17	.26359	.96463	.28039	.95980	.29710	.95485	.31372	.94952	.33024	.94390	43
18	.26387	.96450	.28067	.95981	.29737	.95470	.31399	.94943	.33051	.94380	42
19	.26415	.96448	.28095	.95972	.29765	.95467	.31427	.94933	.33079	.94370	41
20	.26443	.96440	.28123	.95964	.29793	.95459	.31454	.94924	.33106	.94361	40
21	.26471	.96433	.28150	.95956	.29821	.95450	.31482	.94915	.33134	.94351	39
22	.26500	.96425	.28178	.95948	.29849	.95441	.31510	.94906	.33161	.94342	38
23	.26528	.96417	.28206	.95940	.29876	.95433	.31537	.94897	.33189	.94332	37
24	.26556	.96410	.28234	.95931	.29904	.95424	.31565	.94888	.33216	.94322	36
25	.26584	.96402	.28262	.95923	.29932	.95415	.31593	.94878	.33244	.94313	35
26	.26612	.96394	.28290	.95915	.29960	.95407	.31620	.94869	.33271	.94303	34
27	.26640	.96386	.28318	.95907	.29987	.95398	.31648	.94860	.33298	.94293	33
28	.26668	.96379	.28346	.95898	.30015	.95389	.31675	.94851	.33326	.94284	32
29	.26696	.96371	.28374	.95890	.30043	.95380	.31703	.94842	.33353	.94274	31
30	.26724	.96363	.28402	.95882	.30071	.95372	.31730	.94832	.33381	.94264	30
31	.26752	.96355	.28429	.95874	.30098	.95363	.31758	.94823	.33408	.94254	29
32	.26780	.96347	.28457	.95865	.30126	.95354	.31786	.94814	.33430	.94245	28
33	.26808	.96340	.28485	.95857	.30154	.95345	.31813	.94805	.33463	.94235	27
34	.26836	.96332	.28513	.95849	.30182	.95337	.31841	.94795	.33490	.94225	26
35	.26864	.96324	.28541	.95841	.30209	.95328	.31868	.94786	.33518	.94215	25
36	.26892	.96316	.28569	.95832	.30237	.95319	.31896	.94777	.33545	.94206	24
37	.26920	.96308	.28597	.95824	.30265	.95310	.31923	.94768	.33573	.94196	23
38	.26948	.96301	.28625	.95816	.30292	.95301	.31951	.94758	.33600	.94186	22
39	.26976	.96293	.28652	.95807	.30320	.95293	.31979	.94749	.33627	.94176	21
40	.27004	.96285	.28680	.95799	.30348	.95284	.32006	.94740	.33655	.94167	20
41	.27032	.96277	.28708	.95791	.30376	.95275	.32034	.94730	.33682	.94157	19
42	.27060	.96269	.28736	.95782	.30403	.95266	.32061	.94721	.33710	.94147	18
43	.27088	.96261	.28764	.95774	.30431	.95257	.32089	.94712	.33737	.94137	17
44	.27116	.96253	.28792	.95766	.30459	.95248	.32116	.94702	.33764	.94127	16
45	.27144	.96246	.28820	.95757	.30486	.95240	.32144	.94693	.33792	.94118	15
46	.27172	.96238	.28847	.95749	.30514	.95231	.32171	.94684	.33819	.94108	14
47	.27200	.96230	.28875	.95740	.30542	.95222	.32199	.94674	.33846	.94098	13
48	.27228	.96222	.28903	.95732	.30570	.95213	.32227	.94655	.33874	.94088	12
49	.27256	.96214	.28931	.95724	.30597	.95204	.32254	.94656	.33901	.94078	11
50	.27284	.96206	.28959	.95715	.30625	.95195	.32282	.94646	.33929	.94068	10
51	.27312	.96198	.28987	.95707	.30653	.95186	.32309	.94637	.33956	.94058	9
52	.27340	.96190	.29015	.95698	.30680	.95177	.32337	.94627	.33983	.94049	8
53	.27368	.96182	.29042	.95690	.30708	.95168	.32364	.94618	.34011	.94039	7
54	.27396	.96174	.29070	.95681	.30736	.95159	.32392	.94609	.34038	.94029	6
55	.27424	.96166	.29098	.95673	.30763	.95150	.32419	.94599	.34065	.94019	5
56	.27452	.96158	.29126	.95664	.30791	.95142	.32447	.94590	.34093	.94009	4
57	.27480	.96150	.29154	.95656	.30819	.95133	.32474	.94580	.34120	.93999	3
58	.27508	.96142	.29182	.95647	.30846	.95124	.32502	.94571	.34147	.93989	2
59	.27536	.96134	.29209	.95639	.30874	.95115	.32529	.94561	.34175	.93979	1
60	.27564	.96126	.29237	.95630	.30902	.95106	.32557	.94552	.34202	.93969	0
	N. cos.	N. sine	#								
	74°	73°	72°	71°	70°						

TABLE V.

	20°		21°		22°		23°		24°		
/	N. sine	N. cos.									
0	.34202	.93969	.35837	.93358	.37461	.92718	.39073	.92050	.40674	.91355	60
1	.34229	.93959	.35864	.93348	.37488	.92707	.39100	.92039	.40700	.91343	59
2	.34257	.93949	.35891	.93337	.37515	.92697	.39127	.92028	.40727	.91331	58
3	.34284	.93939	.35918	.93327	.37542	.92686	.39153	.92016	.40753	.91319	57
4	.34311	.93929	.35945	.93316	.37569	.92675	.39180	.92005	.40780	.91307	56
5	.34339	.93919	.35973	.93306	.37595	.92664	.39207	.91994	.40806	.91295	55
6	.34366	.93909	.36000	.93295	.37622	.92653	.39234	.91982	.40833	.91283	54
7	.34393	.93899	.36027	.93285	.37649	.92642	.39260	.91971	.40860	.91272	53
8	.34421	.93889	.36054	.93274	.37676	.92631	.39287	.91959	.40886	.91260	52
9	.34448	.93879	.36081	.93264	.37703	.92620	.39314	.91948	.40913	.91248	51
10	.34475	.93869	.36108	.93253	.37730	.92600	.39341	.91936	.40939	.91236	50
11	.34503	.93859	.36135	.93243	.37757	.92598	.39367	.91925	.40966	.91224	49
12	.34530	.93849	.36162	.93232	.37784	.92587	.39394	.91914	.40992	.91212	48
13	.34557	.93839	.36190	.93222	.37811	.92576	.39421	.91902	.41019	.91200	47
14	.34584	.93829	.36217	.93211	.37838	.92565	.39448	.91891	.41045	.91188	46
15	.34612	.93819	.36244	.93201	.37865	.92554	.39474	.91879	.41072	.91176	45
16	.34639	.93809	.36271	.93190	.37892	.92543	.39501	.91868	.41098	.91164	44
17	.34666	.93799	.36298	.93180	.37919	.92532	.39528	.91856	.41125	.91152	43
18	.34694	.93789	.36325	.93169	.37946	.92521	.39555	.91845	.41151	.91140	42
19	.34721	.93779	.36352	.93159	.37973	.92510	.39581	.91833	.41178	.91128	41
20	.34748	.93769	.36379	.93148	.37999	.92499	.39608	.91822	.41204	.91116	40
21	.34775	.93759	.36406	.93137	.38026	.92488	.39635	.91810	.41231	.91104	39
22	.34803	.93748	.36434	.93127	.38053	.92477	.39661	.91799	.41257	.91092	38
23	.34830	.93738	.36461	.93116	.38080	.92466	.39688	.91787	.41284	.91080	37
24	.34857	.93728	.36488	.93106	.38107	.92455	.39715	.91775	.41310	.91068	36
25	.34884	.93718	.36515	.93095	.38134	.92444	.39741	.91764	.41337	.91056	35
26	.34912	.93708	.36542	.93084	.38161	.92432	.39768	.91752	.41363	.91044	34
27	.34939	.93698	.36569	.93074	.38188	.92421	.39795	.91741	.41390	.91032	33
28	.34966	.93688	.36596	.93063	.38215	.92410	.39822	.91729	.41416	.91020	32
29	.34993	.93677	.36623	.93052	.38241	.92399	.39848	.91718	.41443	.91008	31
30	.35021	.93667	.36650	.93040	.38268	.92388	.39875	.91706	.41469	.90996	30
31	.35048	.93657	.36677	.93031	.38295	.92377	.39902	.91694	.41496	.90984	29
32	.35075	.93647	.36704	.93020	.38322	.92366	.39928	.91683	.41522	.90972	28
33	.35102	.93637	.36731	.93010	.38349	.92355	.39955	.91671	.41549	.90960	27
34	.35130	.93626	.36758	.92999	.38376	.92343	.39982	.91660	.41575	.90948	26
35	.35157	.93616	.36785	.92988	.38403	.92332	.40008	.91648	.41602	.90936	25
36	.35184	.93606	.36812	.92978	.38430	.92321	.40035	.91636	.41628	.90924	24
37	.35211	.93596	.36839	.92967	.38456	.92310	.40062	.91625	.41655	.90911	23
38	.35239	.93585	.36867	.92956	.38483	.92299	.40088	.91613	.41681	.90899	22
39	.35266	.93575	.36894	.92945	.38510	.92287	.40115	.91601	.41707	.90887	21
40	.35293	.93565	.36921	.92935	.38537	.92276	.40141	.91590	.41734	.90875	20
41	.35320	.93555	.36948	.92924	.38564	.92265	.40168	.91578	.41760	.90863	19
42	.35347	.93544	.36975	.92913	.38591	.92254	.40195	.91566	.41787	.90851	18
43	.35375	.93534	.37002	.92902	.38617	.92243	.40221	.91555	.41813	.90839	17
44	.35402	.93524	.37029	.92892	.38644	.92231	.40248	.91543	.41840	.90826	16
45	.35429	.93514	.37056	.92881	.38671	.92220	.40275	.91531	.41866	.90814	15
46	.35456	.93503	.37083	.92870	.38698	.92209	.40301	.91519	.41892	.90802	14
47	.35484	.93493	.37110	.92859	.38725	.92198	.40328	.91508	.41919	.90790	13
48	.35511	.93483	.37137	.92849	.38752	.92186	.40355	.91496	.41945	.90778	12
49	.35538	.93474	.37164	.92838	.38778	.92175	.40381	.91484	.41972	.90766	11
50	.35565	.93462	.37191	.92827	.38805	.92164	.40408	.91472	.41998	.90753	10
51	.35592	.93452	.37218	.92816	.38832	.92152	.40434	.91461	.42024	.90741	9
52	.35619	.93441	.37245	.92805	.38859	.92141	.40461	.91449	.42051	.90729	8
53	.35647	.93431	.37272	.92794	.38886	.92130	.40488	.91437	.42077	.90717	7
54	.35674	.93420	.37299	.92784	.38912	.92119	.40514	.91425	.42104	.90704	6
55	.35701	.93410	.37326	.92773	.38939	.92107	.40541	.91414	.42130	.90692	5
56	.35728	.93400	.37353	.92762	.38966	.92096	.40567	.91402	.42156	.90680	4
57	.35755	.93389	.37380	.92751	.38993	.92085	.40594	.91390	.42183	.90668	3
58	.35782	.93379	.37407	.92740	.39020	.92073	.40621	.91378	.42209	.90655	2
59	.35810	.93368	.37434	.92729	.39046	.92062	.40647	.91366	.42235	.90643	1
60	.35837	.93358	.37461	.92718	.39073	.92050	.40674	.91355	.42262	.90631	0
	N. cos.	N. sine	/								
	69°		68°		67°		66°		65°		

	25°		26°		27°		28°		29°		
	N. sine	N. cos.									
0	.42262	.90631	.43837	.89879	.45399	.89101	.46947	.88295	.48481	.87462	60
1	.42288	.90618	.43863	.89867	.45425	.89087	.46973	.88281	.48506	.87448	59
2	.42315	.90606	.43889	.89854	.45451	.89074	.46999	.88267	.48532	.87434	58
3	.42341	.90594	.43916	.89841	.45477	.89061	.47024	.88254	.48557	.87420	57
4	.42367	.90582	.43942	.89828	.45503	.89048	.47050	.88240	.48583	.87406	50
5	.42394	.90569	.43968	.89816	.45529	.89035	.47076	.88226	.48608	.87391	55
6	.42420	.90557	.43994	.89803	.45554	.89021	.47101	.88213	.48634	.87377	54
7	.42446	.90545	.44020	.89790	.45580	.89008	.47127	.88199	.48659	.87363	53
8	.42473	.90532	.44046	.89777	.45606	.88995	.47153	.88185	.48684	.87349	52
9	.42499	.90520	.44072	.89764	.45632	.88981	.47178	.88172	.48710	.87335	51
10	.42525	.90507	.44098	.89752	.45658	.88968	.47204	.88158	.48735	.87321	50
11	.42552	.90495	.44124	.89739	.45684	.88955	.47229	.88144	.48761	.87306	49
12	.42578	.90483	.44151	.89726	.45710	.88942	.47255	.88130	.48786	.87292	48
13	.42604	.90470	.44177	.89713	.45736	.88928	.47281	.88117	.48811	.87278	47
14	.42631	.90458	.44203	.89700	.45762	.88915	.47306	.88103	.48837	.87264	46
15	.42657	.90446	.44229	.89687	.45787	.88902	.47332	.88089	.48862	.87250	45
16	.42683	.90433	.44255	.89674	.45813	.88888	.47358	.88075	.48888	.87235	44
17	.42709	.90421	.44281	.89662	.45839	.88875	.47383	.88062	.48913	.87221	43
18	.42736	.90408	.44307	.89649	.45865	.88860	.47409	.88048	.48938	.87207	42
19	.42762	.90396	.44333	.89630	.45891	.88848	.47434	.88034	.48964	.87193	41
20	.42788	.90383	.44359	.89623	.45917	.88835	.47460	.88020	.48989	.87178	40
21	.42815	.90371	.44385	.89610	.45942	.88822	.47486	.88006	.49014	.87164	39
22	.42841	.90358	.44411	.89597	.45968	.88808	.47511	.87993	.49040	.87150	38
23	.42867	.90346	.44437	.89584	.45994	.88795	.47537	.87979	.49065	.87136	37
24	.42894	.90334	.44464	.89571	.46020	.88782	.47562	.87965	.49090	.87121	36
25	.42920	.90321	.44490	.89558	.46046	.88768	.47588	.87951	.49116	.87107	35
26	.42946	.90309	.44516	.89545	.46072	.88755	.47614	.87937	.49141	.87093	34
27	.42972	.90296	.44542	.89532	.46097	.88741	.47639	.87923	.49166	.87079	33
28	.42999	.90284	.44568	.89519	.46123	.88728	.47665	.87999	.49192	.87064	32
29	.43025	.90271	.44594	.89506	.46149	.88715	.47690	.87896	.49217	.87050	31
30	.43051	.90259	.44620	.89493	.46175	.88701	.47716	.87882	.49242	.87036	30
31	.43077	.90246	.44646	.89480	.46201	.88688	.47741	.87868	.49268	.87021	29
32	.43104	.90233	.44672	.89467	.46226	.88674	.47767	.87854	.49293	.87007	28
33	.43130	.90221	.44688	.89454	.46252	.88661	.47793	.87840	.49318	.86993	27
34	.43156	.90208	.44724	.89441	.46278	.88647	.47818	.87826	.49344	.86978	26
35	.43182	.90196	.44750	.89428	.46304	.88634	.47844	.87812	.49369	.86964	25
36	.43209	.90183	.44776	.89415	.46330	.88620	.47869	.87798	.49394	.86949	24
37	.43235	.90171	.44802	.89402	.46355	.88607	.47895	.87784	.49419	.86935	23
38	.43261	.90158	.44828	.89380	.46381	.88593	.47920	.87770	.49445	.86921	22
39	.43287	.90146	.44854	.89376	.46407	.88580	.47946	.87756	.49470	.86906	21
40	.43313	.90133	.44880	.89363	.46433	.88566	.47971	.87743	.49495	.86892	20
41	.43340	.90120	.44906	.89350	.46458	.88553	.47997	.87729	.49521	.86878	19
42	.43366	.90108	.44932	.89337	.46484	.88539	.48022	.87715	.49546	.86863	18
43	.43392	.90095	.44958	.89324	.46510	.88526	.48048	.87701	.49571	.86849	17
44	.43418	.90082	.44984	.89311	.46536	.88512	.48073	.87687	.49596	.86834	16
45	.43445	.90070	.45010	.89298	.46561	.88499	.48099	.87673	.49622	.86820	15
46	.43471	.90057	.45036	.89285	.46587	.88485	.48124	.87659	.49647	.86805	14
47	.43497	.90045	.45062	.89272	.46613	.88472	.48150	.87645	.49672	.86791	13
48	.43523	.90032	.45088	.89259	.46639	.88458	.48175	.87631	.49697	.86777	12
49	.43549	.90019	.45114	.89245	.46664	.88445	.48201	.87617	.49723	.86762	11
50	.43575	.90007	.45140	.89232	.46690	.88431	.48226	.87603	.49748	.86748	10
51	.43602	.89994	.45166	.89219	.46716	.88417	.48252	.87589	.49773	.86733	9
52	.43628	.89981	.45192	.89206	.46742	.88404	.48277	.87575	.49798	.86719	8
53	.43654	.89968	.45218	.89193	.46767	.88390	.48303	.87561	.49824	.86704	7
54	.43680	.89956	.45243	.89180	.46793	.88377	.48328	.87546	.49849	.86690	6
55	.43706	.89943	.45269	.89167	.46819	.88363	.48354	.87532	.49874	.86675	5
56	.43733	.89930	.45295	.89153	.46844	.88349	.48379	.87518	.49899	.86661	4
57	.43759	.89918	.45321	.89140	.46870	.88336	.48405	.87504	.49924	.86646	3
58	.43785	.89905	.45347	.89127	.46896	.88322	.48430	.87490	.49950	.86632	2
59	.43811	.89892	.45373	.89114	.46921	.88308	.48450	.87476	.49975	.86617	1
60	.43837	.89879	.45399	.89101	.46947	.88295	.48481	.87462	.50000	.86603	0
	N. cos.	N. sine									
	64°		63°		62°		61°		60°		

TABLE V.

	30°		31°		32°		33°		34°		
,	N. sine	N. cos.									
0	.50000	.86603	.51504	.85717	.52992	.84805	.54464	.83867	.55919	.82904	60
1	.50025	.86588	.51529	.85702	.53017	.84789	.54488	.83851	.55943	.82887	59
2	.50050	.86573	.51554	.85687	.53041	.84774	.54513	.83835	.55968	.82871	58
3	.50076	.86559	.51579	.85672	.53066	.84759	.54537	.83819	.55992	.82855	57
4	.50101	.86544	.51604	.85657	.53091	.84743	.54561	.83804	.56016	.82839	56
5	.50126	.86530	.51628	.85642	.53115	.84728	.54586	.83788	.56040	.82822	55
6	.50151	.86515	.51653	.85627	.53140	.84712	.54610	.83772	.56064	.82806	54
7	.50176	.86501	.51678	.85612	.53164	.84697	.54635	.83756	.56088	.82790	53
8	.50201	.86486	.51703	.85597	.53189	.84681	.54659	.83740	.56112	.82773	52
9	.50227	.86471	.51728	.85582	.53214	.84666	.54683	.83724	.56136	.82757	51
10	.50252	.86457	.51753	.85567	.53238	.84650	.54708	.83708	.56160	.82741	50
11	.50277	.86442	.51778	.85551	.53263	.84635	.54732	.83692	.56184	.82724	49
12	.50302	.86427	.51803	.85536	.53288	.84619	.54756	.83676	.56208	.82708	48
13	.50327	.86413	.51828	.85521	.53312	.84604	.54781	.83660	.56232	.82692	47
14	.50352	.86398	.51852	.85506	.53337	.84588	.54805	.83645	.56256	.82675	46
15	.50377	.86384	.51877	.85491	.53361	.84573	.54829	.83629	.56280	.82659	45
16	.50403	.86369	.51902	.85476	.53386	.84557	.54854	.83613	.56305	.82643	44
17	.50428	.86354	.51927	.85461	.53411	.84542	.54878	.83597	.56329	.82626	43
18	.50453	.86340	.51952	.85446	.53435	.84526	.54902	.83581	.56353	.82610	42
19	.50478	.86325	.51977	.85431	.53460	.84511	.54927	.83565	.56377	.82593	41
20	.50503	.86310	.52002	.85416	.53484	.84495	.54951	.83549	.56401	.82577	40
21	.50528	.86295	.52026	.85401	.53509	.84480	.54975	.83533	.56425	.82561	39
22	.50553	.86281	.52051	.85385	.53534	.84464	.54999	.83517	.56449	.82544	38
23	.50578	.86266	.52076	.85370	.53558	.84448	.55024	.83501	.56473	.82528	37
24	.50603	.86251	.52101	.85355	.53583	.84433	.55048	.83485	.56497	.82511	36
25	.50628	.86237	.52126	.85340	.53607	.84417	.55072	.83469	.56521	.82495	35
26	.50654	.86222	.52151	.85325	.53632	.84402	.55097	.83453	.56545	.82478	34
27	.50679	.86207	.52175	.85310	.53656	.84386	.55121	.83437	.56569	.82462	33
28	.50704	.86192	.52200	.85294	.53681	.84370	.55145	.83421	.56593	.82446	32
29	.50729	.86178	.52225	.85279	.53705	.84355	.55169	.83405	.56617	.82429	31
30	.50754	.86163	.52250	.85264	.53730	.84339	.55194	.83389	.56641	.82413	30
31	.50779	.86148	.52275	.85249	.53754	.84324	.55218	.83373	.56665	.82396	29
32	.50804	.86133	.52299	.85234	.53779	.84308	.55242	.83356	.56689	.82380	28
33	.50829	.86119	.52324	.85218	.53804	.84292	.55266	.83340	.56713	.82363	27
34	.50854	.86104	.52349	.85203	.53828	.84277	.55291	.83324	.56736	.82347	26
35	.50879	.86089	.52374	.85188	.53853	.84261	.55315	.83308	.56760	.82330	25
36	.50904	.86074	.52399	.85173	.53877	.84245	.55339	.83292	.56784	.82314	24
37	.50929	.86059	.52423	.85157	.53902	.84230	.55363	.83276	.56808	.82297	23
38	.50954	.86045	.52448	.85142	.53926	.84214	.55388	.83260	.56832	.82281	22
39	.50979	.86030	.52473	.85127	.53951	.84198	.55412	.83244	.56856	.82264	21
40	.51004	.86015	.52498	.85112	.53975	.84182	.55436	.83228	.56880	.82248	20
41	.51029	.86000	.52522	.85096	.54000	.84167	.55460	.83212	.56904	.82231	19
42	.51054	.85985	.52547	.85081	.54024	.84151	.55484	.83195	.56928	.82214	18
43	.51079	.85970	.52572	.85066	.54049	.84135	.55509	.83179	.56952	.82198	17
44	.51104	.85956	.52597	.85051	.54073	.84120	.55533	.83163	.56976	.82181	16
45	.51129	.85941	.52621	.85035	.54097	.84104	.55557	.83147	.57000	.82165	15
46	.51154	.85926	.52646	.85020	.54122	.84088	.55581	.83131	.57024	.82148	14
47	.51179	.85911	.52671	.85005	.54146	.84072	.55605	.83115	.57047	.82132	13
48	.51204	.85896	.52696	.84989	.54171	.84057	.55630	.83098	.57071	.82115	12
49	.51229	.85881	.52720	.84974	.54195	.84041	.55654	.83082	.57095	.82098	11
50	.51254	.85866	.52745	.84959	.54220	.84025	.55678	.83060	.57119	.82082	10
51	.51279	.85851	.52770	.84943	.54244	.84009	.55702	.83050	.57143	.82065	9
52	.51304	.85836	.52794	.84928	.54269	.83994	.55726	.83034	.57167	.82048	8
53	.51329	.85821	.52819	.84913	.54293	.83978	.55750	.83017	.57191	.82032	7
54	.51354	.85806	.52844	.84897	.54317	.83962	.55775	.83001	.57215	.82015	6
55	.51379	.85792	.52869	.84882	.54342	.83946	.55799	.82985	.57238	.81999	5
56	.51404	.85777	.52893	.84866	.54366	.83930	.55823	.82969	.57262	.81982	4
57	.51429	.85762	.52918	.84851	.54391	.83915	.55847	.82953	.57286	.81965	3
58	.51454	.85747	.52943	.84836	.54415	.83899	.55871	.82936	.57310	.81949	2
59	.51479	.85732	.52967	.84820	.54440	.83883	.55895	.82920	.57334	.81932	1
60	.51504	.85717	.52992	.84805	.54464	.83867	.55919	.82904	.57358	.81915	0
	N. cos.	N. sine	/								
	59°		58°		57°		56°		55°		

	35°		36°		37°		38°		39°		
	N. sine	N. cos.									
0	.57358	.81915	.58779	.80902	.60182	.79864	.61566	.78801	.62932	.77715	60
1	.57381	.81899	.58802	.80885	.60205	.79846	.61589	.78783	.62955	.77696	59
2	.57405	.81882	.58826	.80867	.60228	.79829	.61612	.78765	.62977	.77678	58
3	.57429	.81865	.58849	.80850	.60251	.79811	.61635	.78747	.63000	.77660	57
4	.57453	.81848	.58873	.80833	.60274	.79793	.61658	.78729	.63022	.77641	56
5	.57477	.81832	.58896	.80816	.60298	.79776	.61681	.78711	.63045	.77623	55
6	.57501	.81815	.58920	.80799	.60321	.79758	.61704	.78694	.63068	.77605	54
7	.57524	.81798	.58943	.80782	.60344	.79741	.61726	.78676	.63090	.77586	53
8	.57548	.81782	.58967	.80765	.60367	.79723	.61749	.78658	.63113	.77568	52
9	.57572	.81765	.58990	.80748	.60390	.79706	.61772	.78640	.63135	.77550	51
10	.57596	.81748	.59014	.80730	.60414	.79688	.61795	.78622	.63158	.77531	50
11	.57619	.81731	.59037	.80713	.60437	.79671	.61818	.78604	.63180	.77513	49
12	.57643	.81714	.59060	.80696	.60460	.79653	.61841	.78586	.63203	.77494	48
13	.57667	.81698	.59084	.80679	.60483	.79635	.61864	.78568	.63225	.77476	47
14	.57691	.81681	.59108	.80662	.60506	.79618	.61887	.78550	.63248	.77458	46
15	.57715	.81664	.59131	.80644	.60529	.79600	.61909	.78532	.63271	.77439	45
16	.57738	.81647	.59154	.80627	.60553	.79583	.61932	.78514	.63293	.77421	44
17	.57762	.81631	.59178	.80610	.60576	.79565	.61955	.78496	.63316	.77402	43
18	.57786	.81614	.59201	.80593	.60599	.79547	.61978	.78478	.63338	.77384	42
19	.57810	.81597	.59225	.80576	.60622	.79530	.62001	.78460	.63361	.77366	41
20	.57833	.81580	.59248	.80558	.60645	.79512	.62024	.78442	.63383	.77347	40
21	.57857	.81563	.59272	.80541	.60668	.79494	.62046	.78424	.63406	.77329	39
22	.57881	.81546	.59295	.80524	.60691	.79477	.62069	.78405	.63428	.77310	38
23	.57904	.81530	.59318	.80507	.60714	.79459	.62092	.78387	.63451	.77292	37
24	.57928	.81513	.59342	.80489	.60738	.79441	.62115	.78369	.63473	.77273	36
25	.57952	.81496	.59365	.80472	.60761	.79424	.62138	.78351	.63496	.77255	35
26	.57976	.81479	.59389	.80455	.60784	.79406	.62160	.78333	.63518	.77236	34
27	.57999	.81462	.59412	.80438	.60807	.79388	.62183	.78315	.63540	.77218	33
28	.58023	.81445	.59436	.80420	.60830	.79371	.62206	.78297	.63563	.77199	32
29	.58047	.81428	.59459	.80403	.60853	.79353	.62229	.78279	.63585	.77181	31
30	.58070	.81412	.59482	.80386	.60876	.79335	.62251	.78261	.63608	.77162	30
31	.58094	.81395	.59506	.80368	.60899	.79318	.62274	.78243	.63630	.77144	29
32	.58118	.81378	.59529	.80351	.60922	.79300	.62297	.78225	.63653	.77125	28
33	.58141	.81361	.59552	.80334	.60945	.79282	.62320	.78206	.63675	.77107	27
34	.58165	.81344	.59576	.80316	.60968	.79264	.62342	.78188	.63698	.77088	26
35	.58189	.81327	.59599	.80299	.60991	.79247	.62365	.78170	.63720	.77070	25
36	.58212	.81310	.59622	.80282	.61015	.79229	.62388	.78152	.63742	.77051	24
37	.58236	.81293	.59646	.80264	.61038	.79211	.62411	.78134	.63765	.77033	23
38	.58260	.81276	.59669	.80247	.61061	.79193	.62433	.78116	.63787	.77014	22
39	.58283	.81259	.59693	.80230	.61084	.79176	.62456	.78098	.63810	.76996	21
40	.58307	.81242	.59716	.80212	.61107	.79158	.62479	.78079	.63832	.76977	20
41	.58330	.81225	.59739	.80195	.61130	.79140	.62502	.78061	.63854	.76959	19
42	.58354	.81208	.59763	.80178	.61153	.79122	.62524	.78043	.63877	.76940	18
43	.58378	.81191	.59786	.80160	.61176	.79105	.62547	.78025	.63899	.76921	17
44	.58401	.81174	.59809	.80143	.61199	.79079	.62570	.78007	.63920	.76903	16
45	.58425	.81157	.59832	.80125	.61222	.79069	.62592	.77988	.63944	.76884	15
46	.58449	.81140	.59856	.80108	.61245	.79051	.62615	.77970	.63966	.76866	14
47	.58472	.81123	.59879	.80091	.61268	.79033	.62638	.77952	.63989	.76847	13
48	.58496	.81106	.59902	.80073	.61291	.79016	.62660	.77934	.64011	.76828	12
49	.58519	.81089	.59926	.80056	.61314	.78998	.62683	.77916	.64033	.76810	11
50	.58543	.81072	.59949	.80038	.61337	.78980	.62706	.77897	.64056	.76791	10
51	.58567	.81055	.59972	.80021	.61360	.78962	.62728	.77879	.64078	.76772	9
52	.58590	.81038	.59995	.80003	.61383	.78944	.62751	.77861	.64100	.76754	8
53	.58614	.81021	.60019	.79980	.61406	.78926	.62774	.77843	.64123	.76735	7
54	.58637	.81004	.60042	.79968	.61429	.78908	.62796	.77824	.64145	.76717	6
55	.58661	.80987	.60065	.79951	.61451	.78891	.62819	.77806	.64167	.76698	5
56	.58684	.80970	.60089	.79934	.61474	.78873	.62842	.77788	.64190	.76679	4
57	.58708	.80953	.60112	.79916	.61497	.78855	.62864	.77769	.64212	.76661	3
58	.58731	.80936	.60135	.79899	.61520	.78837	.62887	.77751	.64234	.76642	2
59	.58755	.80919	.60158	.79881	.61543	.78819	.62909	.77733	.64256	.76623	1
60	.58779	.80902	.60182	.79864	.61566	.78801	.62932	.77715	.64279	.76604	0
	N. cos.	N. sine									
	54°	53°	52°	51°	50°						

TABLE V.

	40°		41°		42°		43°		44°		
	N. sine	N. cos.									
0	.64279	.76604	.65606	.75471	.66913	.74314	.68200	.73135	.69466	.71934	60
1	.64301	.76586	.65628	.75452	.66935	.74295	.68221	.73116	.69487	.71914	59
2	.64323	.76567	.65650	.75433	.66956	.74276	.68242	.73096	.69508	.71894	58
3	.64346	.76548	.65672	.75414	.66978	.74256	.68264	.73076	.69529	.71873	57
4	.64368	.76530	.65694	.75395	.66999	.74237	.68285	.73056	.69549	.71853	56
5	.64390	.76511	.65716	.75375	.67021	.74217	.68306	.73036	.69570	.71833	55
6	.64412	.76492	.65738	.75356	.67043	.74198	.68327	.73016	.69591	.71813	54
7	.64435	.76473	.65759	.75337	.67064	.74178	.68349	.72996	.69612	.71792	53
8	.64457	.76455	.65781	.75318	.67086	.74159	.68370	.72976	.69633	.71772	52
9	.64479	.76436	.65803	.75299	.67107	.74139	.68391	.72957	.69654	.71752	51
10	.64501	.76417	.65825	.75280	.67129	.74120	.68412	.72937	.69675	.71732	50
11	.64524	.76398	.65847	.75261	.67151	.74100	.68434	.72917	.69696	.71711	49
12	.64546	.76380	.65869	.75241	.67172	.74080	.68455	.72897	.69717	.71691	48
13	.64568	.76361	.65891	.75222	.67194	.74061	.68476	.72877	.69737	.71671	47
14	.64590	.76342	.65913	.75203	.67215	.74041	.68497	.72857	.69758	.71650	46
15	.64612	.76323	.65935	.75184	.67237	.74022	.68518	.72837	.69779	.71630	45
16	.64635	.76304	.65956	.75165	.67258	.74002	.68539	.72817	.69800	.71610	44
17	.64657	.76286	.65978	.75146	.67280	.73983	.68561	.72797	.69821	.71590	43
18	.64679	.76267	.66000	.75126	.67301	.73963	.68582	.72777	.69842	.71569	42
19	.64701	.76248	.66022	.75107	.67323	.73944	.68603	.72757	.69862	.71549	41
20	.64723	.76229	.66044	.75088	.67344	.73924	.68624	.72737	.69883	.71529	40
21	.64746	.76210	.66066	.75069	.67366	.73904	.68645	.72717	.69904	.71508	39
22	.64768	.76192	.66088	.75050	.67387	.73885	.68666	.72697	.69925	.71488	38
23	.64790	.76173	.66109	.75030	.67409	.73865	.68688	.72677	.69946	.71468	37
24	.64812	.76154	.66131	.75011	.67430	.73846	.68709	.72657	.69966	.71447	36
25	.64834	.76135	.66153	.74992	.67452	.73826	.68730	.72637	.69987	.71427	35
26	.64856	.76116	.66175	.74973	.67473	.73806	.68751	.72617	.70000	.71407	34
27	.64878	.76097	.66197	.74953	.67495	.73787	.68772	.72597	.70029	.71386	33
28	.64901	.76078	.66218	.74934	.67516	.73767	.68793	.72577	.70049	.71366	32
29	.64923	.76059	.66240	.74915	.67538	.73747	.68814	.72557	.70070	.71345	31
30	.64945	.76041	.66262	.74896	.67559	.73728	.68835	.72537	.70091	.71325	30
31	.64967	.76022	.66284	.74876	.67580	.73708	.68857	.72517	.70112	.71305	29
32	.64989	.76003	.66306	.74857	.67602	.73688	.68878	.72497	.70132	.71284	28
33	.65011	.75984	.66327	.74838	.67623	.73669	.68899	.72477	.70153	.71264	27
34	.65033	.75965	.66349	.74818	.67645	.73649	.68920	.72457	.70174	.71243	26
35	.65055	.75946	.66371	.74799	.67666	.73629	.68941	.72437	.70195	.71223	25
36	.65077	.75927	.66393	.74780	.67688	.73610	.68962	.72417	.70215	.71203	24
37	.65100	.75908	.66414	.74760	.67709	.73590	.68983	.72397	.70236	.71182	23
38	.65122	.75889	.66436	.74741	.67730	.73570	.69004	.72377	.70257	.71162	22
39	.65144	.75870	.66458	.74722	.67752	.73551	.69025	.72357	.70277	.71141	21
40	.65166	.75851	.66480	.74703	.67773	.73531	.69046	.72337	.70298	.71121	20
41	.65188	.75832	.66501	.74683	.67795	.73511	.69067	.72317	.70319	.71100	19
42	.65210	.75813	.66523	.74664	.67816	.73491	.69088	.72297	.70339	.71080	18
43	.65232	.75794	.66545	.74644	.67837	.73472	.69109	.72277	.70360	.71059	17
44	.65254	.75775	.66566	.74625	.67859	.73452	.69130	.72257	.70381	.71039	16
45	.65276	.75756	.66588	.74606	.67880	.73432	.69151	.72236	.70401	.71019	15
46	.65298	.75738	.66610	.74586	.67901	.73413	.69172	.72216	.70422	.70998	14
47	.65320	.75719	.66632	.74567	.67923	.73393	.69193	.72196	.70443	.70978	13
48	.65342	.75700	.66653	.74548	.67944	.73373	.69214	.72176	.70463	.70957	12
49	.65364	.75680	.66675	.74528	.67965	.73353	.69235	.72150	.70484	.70937	11
50	.65386	.75661	.66699	.74509	.67987	.73333	.69256	.72136	.70505	.70910	10
51	.65408	.75642	.66718	.74480	.68008	.73314	.69277	.72116	.70525	.70896	9
52	.65430	.75623	.66740	.74470	.68029	.73294	.69298	.72095	.70540	.70875	8
53	.65452	.75604	.66762	.74451	.68051	.73274	.69319	.72075	.70557	.70855	7
54	.65474	.75585	.66783	.74431	.68072	.73254	.69340	.72055	.70587	.70834	6
55	.65496	.75566	.66805	.74412	.68093	.73234	.69361	.72035	.70605	.70813	5
56	.65518	.75547	.66827	.74392	.68115	.73215	.69382	.72015	.70628	.70793	4
57	.65540	.75528	.66848	.74373	.68136	.73195	.69403	.71995	.70649	.70772	3
58	.65562	.75509	.66869	.74353	.68157	.73175	.69424	.71974	.70670	.70752	2
59	.65584	.75490	.66891	.74334	.68179	.73155	.69445	.71954	.70690	.70731	1
60	.65606	.75471	.66913	.74314	.68200	.73135	.69466	.71934	.70711	.70711	0
	N. cos.	N. sine	/								
	49°	48°	47°	46°	45°						

## TABLE VI.

## ADDITION AND SUBTRACTION LOGARITHMS.

## PRECEPTS.

## I. When difference of given logarithms is less than 2.00.

ADDITION.—Enter table with difference between logarithms as Arg. A, and take out B.

Add B to subtracted logarithm.

SUBTRACTION.—Subtract lesser from greater logarithm; enter with the difference as B, and take out A.

Add A to the subtracted logarithm.

## II. When difference of given logarithms exceeds 2.00.

Subtract lesser from greater.

ADDITION.—Enter table with difference as Arg. A, take out B-A and add it to the greater logarithm.

SUBTRACTION.—Enter column B with difference of logarithms; take out B-A, and subtract it from greater logarithm.

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
5.	0.00	000	001	001	001	001	001	002	002	003	003	
6.0	004	004	005	005	005	005	005	005	005	005	005	
6.1	005	006	006	006	006	006	006	006	007	007	007	3 4 5 6
6.2	007	007	007	007	008	008	008	008	008	008	008	1 0.3 0.4 0.5 0.6
6.3	009	009	009	009	010	010	010	010	010	011	011	2 0.6 0.8 1.0 1.2
6.4	011	011	011	012	012	012	013	013	013	013	013	3 0.9 1.2 1.5 1.8
6.5	014	014	014	015	015	015	016	016	017	017	017	4 1.2 1.6 2.0 2.4
6.6	017	018	018	019	019	019	020	020	021	021	021	5 1.5 2.0 2.5 3.0
6.7	022	022	023	023	024	024	025	026	026	027	027	6 1.8 2.4 3.0 3.6
6.8	027	028	029	029	030	031	031	032	033	034	034	7 2.1 2.8 3.5 4.2
6.9	034	035	036	037	038	039	040	041	041	042	042	8 2.4 3.2 4.0 4.8
7.0	043	044	045	047	048	049	050	051	052	053	053	9 2.7 3.6 4.5 5.4
7.1	055	056	057	059	060	061	063	064	066	067	067	10 3 4 5 6
7.2	069	070	072	074	075	077	079	081	083	085	085	1 0.7 0.8 0.9 1.0
7.3	087	089	091	093	095	097	099	102	104	106	106	2 1.4 1.6 1.8 2.0
7.4	109	111	114	117	119	122	125	128	131	134	134	3 2.1 2.4 2.7 3.0
7.5	137	140	144	147	150	154	157	161	165	169	169	4 2.8 3.2 3.6 4.0
7.6	173	177	181	185	189	194	198	203	207	212	212	5 3.5 4.0 4.5 5.0
7.7	217	222	227	233	238	244	249	255	261	267	267	6 4.2 4.8 5.4 6.0
7.8	273	280	286	293	299	306	313	321	328	336	336	7 4.9 5.6 6.3 7.0
7.9	344	352	360	368	377	385	394	403	413	422	422	8 5.6 6.4 7.2 8.0
8.0	432	442	452	463	474	485	496	507	519	531	531	9 6.3 7.2 8.1 9.0
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

ADD.  $\left\{ \begin{array}{l} \log b - \log a = A \\ \log(a+b) = \log a + B \end{array} \right.$

SUB.  $\left\{ \begin{array}{l} \log a - \log b = B \\ \log(a-b) = \log b + A \end{array} \right.$

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
8.00	0.00	432	433	434	435	436	437	438	439	440	441	
8.01		442	443	444	445	446	447	448	449	450	451	
8.02		452	453	454	456	457	458	459	460	461	462	
8.03		463	464	465	466	467	468	469	470	471	473	
8.04		474	475	476	477	478	479	480	481	482	483	
8.05		485	486	487	488	489	490	491	492	494	495	
8.06		496	497	498	499	500	502	503	504	505	506	
8.07		507	508	510	511	512	513	514	515	517	518	
8.08		519	520	521	523	524	525	526	527	529	530	
8.09		531	532	533	535	536	537	538	540	541	542	
8.10		543	545	546	547	548	550	551	552	553	555	
8.11		556	557	558	560	561	562	564	565	566	567	I 8
8.12		569	570	571	573	574	575	577	578	579	581	I 0.2
8.13		582	583	585	586	587	589	590	591	593	594	I 0.4
8.14		595	597	598	599	601	602	604	605	606	608	I 0.6
8.15		609	611	612	613	615	616	618	619	620	622	I 0.8
8.16		623	625	626	628	629	630	632	633	635	636	I 1.0
8.17		638	639	641	642	644	645	646	648	649	651	I 1.2
8.18		652	654	655	657	658	660	661	663	664	666	I 1.4
8.19		667	669	671	672	674	675	677	678	680	681	I 1.6
8.20		683	684	686	688	689	691	692	694	696	697	I 1.8
8.21		699	700	702	703	705	707	708	710	712	713	I 2.0
8.22		715	716	718	720	721	723	725	726	728	730	I 2.2
8.23		731	733	735	736	738	740	741	743	745	747	I 2.4
8.24		748	750	752	753	755	757	759	760	762	764	I 2.6
8.25		766	767	769	771	773	774	776	778	780	781	I 2.8
8.26		783	785	787	789	790	792	794	796	798	799	I 3.0
8.27		801	803	805	807	809	810	812	814	816	818	I 3.2
8.28		820	822	823	825	827	829	831	833	835	837	I 3.4
8.29		839	841	842	844	846	848	850	852	854	856	I 3.6
8.30		858	860	862	864	866	868	870	872	874	876	
8.31		878	880	882	884	886	888	890	892	894	896	
8.32		898	900	902	904	906	908	910	912	915	917	
8.33		919	921	923	925	927	929	931	933	936	938	
8.34		940	942	944	946	948	951	953	955	957	959	
8.35		962	964	966	968	970	973	975	977	979	981	
8.36		984	986	988	990	993	995	997	999	*002	*004	
8.37	0.01	006	009	011	013	016	018	020	022	025	027	I 4
8.38		030	032	034	037	039	041	044	046	048	051	I 0.4
8.39		053	056	058	060	063	065	068	070	073	075	I 0.6
8.40		077	080	082	085	087	090	092	095	097	100	I 2.0
8.41		102	105	107	110	112	115	117	120	122	125	I 2.4
8.42		128	130	133	135	138	140	143	146	148	151	I 2.8
8.43		153	156	159	161	164	167	169	172	175	177	I 3.2
8.44		180	183	185	188	191	193	196	199	202	204	I 3.6
8.45		207	210	213	215	218	221	224	226	229	232	
8.46		235	238	240	243	246	249	252	255	257	260	
8.47		263	266	269	272	275	278	280	283	286	289	
8.48		292	295	298	301	304	307	310	313	316	319	
8.49		322	325	328	331	334	337	340	343	346	349	
8.50		352	355	358	361	364	368	371	374	377	380	
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

ADD.  $\begin{cases} \log b - \log a = A. \\ \log(a + b) = \log a + B. \end{cases}$

SUB.  $\begin{cases} \log a - \log b = B. \\ \log(a - b) = \log b + A. \end{cases}$

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
8.50	0.01	352	355	358	361	364	368	371	374	377	380	
8.51		383	386	389	393	396	399	402	405	408	412	
8.52		415	418	421	424	428	431	434	437	441	444	
8.53		447	450	454	457	460	464	467	470	474	477	
8.54		480	484	487	490	494	497	501	504	507	511	
8.55		514	518	521	525	528	531	535	538	542	545	I 3 4
8.56		549	552	556	559	563	566	570	574	577	581	I 0.3 0.4
8.57		584	588	591	595	599	602	606	610	613	617	2 0.6 0.8
8.58		621	624	628	632	635	639	643	646	650	654	3 0.9 1.2
8.59		658	661	665	669	673	676	680	684	688	692	4 1.2 1.6
8.60		695	699	703	707	711	715	719	722	726	730	5 1.5 2.0
8.61		734	738	742	746	750	754	758	762	766	770	6 1.8 2.4
8.62		774	778	782	786	790	794	798	802	806	810	7 2.1 2.8
8.63		814	818	822	827	831	835	839	843	847	851	8 2.4 3.2
8.64		856	860	864	868	872	877	881	885	889	894	9 2.7 3.6
8.65		898	902	906	911	915	919	924	928	932	937	
8.66		941	945	950	954	959	963	967	972	976	981	
8.67		985	990	994	999	*003	*008	*012	*017	*021	*026	I 5 6
8.68	0.02	030	035	040	044	049	053	058	063	067	072	I 0.5 0.6
8.69		077	081	086	091	095	100	105	110	114	119	2 1.0 1.2
8.70		124	129	133	138	143	148	153	158	162	167	3 1.5 1.8
8.71		172	177	182	187	192	197	202	207	211	216	4 2.0 2.4
8.72		221	226	231	236	241	246	252	257	262	267	5 2.5 3.0
8.73		272	277	282	287	292	297	303	308	313	318	6 3.0 3.6
8.74		323	329	334	339	344	350	355	360	365	371	7 3.5 4.2
8.75		376	381	387	392	397	403	408	414	419	424	8 4.0 4.8
8.76		430	435	441	446	452	457	463	468	474	479	9 4.5 5.4
8.77		485	490	496	502	507	513	518	524	530	535	
8.78		541	547	552	558	564	570	575	581	587	593	I 7 8
8.79		599	604	610	616	622	628	634	639	645	651	2 1.4 1.6
8.80		657	663	669	675	681	687	693	699	705	711	3 2.1 2.4
8.81		717	723	729	735	742	748	754	760	766	772	4 2.8 3.2
8.82		779	785	791	797	803	810	816	822	829	835	5 3.5 4.0
8.83		841	848	854	860	867	873	879	886	892	899	6 4.2 4.8
8.84		905	912	918	925	931	938	944	951	957	964	7 4.9 5.6
8.85		971	977	984	991	997	*004	*011	*017	*024	*031	8 5.6 6.4
8.86	0.03	037	044	051	058	065	071	078	085	092	099	9 6.3 7.2
8.87		106	113	120	126	133	140	147	154	161	168	
8.88		175	183	190	197	204	211	218	225	232	240	
8.89		247	254	261	268	276	283	290	298	305	312	
8.90		320	327	334	342	349	357	364	371	379	386	I 9 10
8.91		394	401	409	417	424	432	439	447	455	462	2 1.8 2.0
8.92		470	478	485	493	501	509	516	524	532	540	3 2.7 3.0
8.93		548	555	563	571	579	587	595	603	611	619	4 3.6 4.0
8.94		627	635	643	651	659	667	675	683	691	700	5 4.5 5.0
8.95		708	716	724	732	741	749	757	765	774	782	6 5.4 6.0
8.96		790	799	807	816	824	832	841	849	858	866	7 6.3 7.0
8.97		875	883	892	901	909	918	926	935	944	953	8 7.2 8.0
8.98		961	970	979	987	996	*005	*014	*023	*032	*040	9 8.1 9.0
8.99	0.04	049	058	067	076	085	094	103	112	121	130	
9.00		139	148	157	167	176	185	194	203	213	222	
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE VI.

ADD.  $\{ \log b - \log a = A.$   
 $\log(a+b) = \log a + B.$

SUB.  $\{ \log a - \log b = B.$   
 $\log(a-b) = \log b + A.$

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
9.00	0.04	139	148	157	167	176	185	194	203	213	222	
9.01		231	240	250	259	268	278	287	297	306	315	1 0.9 1.0 1.1
9.02		325	334	344	353	363	373	382	392	401	411	2 1.8 2.0 2.2
9.03		421	430	440	450	460	469	479	489	499	509	3 2.7 3.0 3.3
9.04		519	528	538	548	558	568	578	588	598	608	4 3.6 4.0 4.4
9.05		618	628	639	649	659	669	679	689	700	710	5 4.5 5.0 5.5
9.06		720	731	741	751	762	772	782	793	803	814	6 5.4 6.0 6.6
9.07		824	835	845	856	867	877	888	898	909	920	7 6.3 7.0 7.7
9.08		931	941	952	963	974	985	995	*006	*017	*028	8 7.2 8.0 8.8
9.09	0.05	039	050	061	072	083	094	105	116	127	139	9 8.1 9.0 9.9
9.10		150	161	172	183	195	206	217	229	240	251	1 1.2 1.3 1.4
9.11		263	274	286	297	308	320	332	343	355	366	2 2.4 2.6 2.8
9.12		378	390	401	413	425	436	448	460	472	484	3 3.6 3.9 4.2
9.13		496	508	519	531	543	555	567	579	591	604	4 4.8 5.2 5.6
9.14		616	628	640	652	664	677	689	701	714	726	5 6.0 6.5 7.0
9.15		738	751	763	775	788	800	813	825	838	851	6 7.2 7.8 8.4
9.16		863	876	889	901	914	927	939	952	965	978	7 8.4 9.1 9.8
9.17		991	*004	*017	*030	*043	*056	*069	*082	*095	*108	8 9.6 10.4 11.2
9.18	0.06	121	134	147	161	174	187	200	214	227	240	9 10.8 11.7 12.6
9.19		254	267	281	294	308	321	335	348	362	376	
9.20		389	403	417	430	444	458	472	486	500	513	
9.21		527	541	555	569	583	597	612	626	640	654	
9.22		668	683	697	711	725	740	754	769	783	798	
9.23		812	827	841	856	870	885	900	914	929	944	
9.24		959	973	988	*003	*018	*033	*048	*063	*078	*093	
9.25		108	123	138	154	169	184	199	215	230	245	
9.26	0.07	261	276	291	307	322	338	354	369	385	400	
9.27		416	432	448	463	479	495	511	527	543	559	
9.28		575	591	607	623	639	655	671	687	704	720	
9.29		736	753	769	785	802	818	835	851	868	884	
9.30		901	918	934	951	968	985	*001	*018	*035	*052	
9.31	0.08	069	086	103	120	137	154	171	188	206	223	
9.32		240	257	275	292	309	327	344	362	379	397	
9.33		415	432	450	468	485	503	521	539	557	574	
9.34		592	610	628	646	664	683	701	719	737	755	
9.35		774	792	810	829	847	865	884	902	921	940	
9.36		958	977	996	*014	*033	*052	*071	*090	*108	*127	
9.37	0.09	146	165	184	204	223	242	261	280	299	319	
9.38		338	357	377	396	416	435	455	474	494	514	
9.39		533	553	573	593	612	632	652	672	692	712	
9.40		732	752	773	793	813	833	853	874	894	914	
9.41		935	955	976	996	*017	*038	*058	*079	*100	*120	
9.42	0.10	141	162	183	204	225	246	267	288	309	330	
9.43		351	373	394	415	437	458	479	501	522	544	
9.44		565	587	609	630	652	674	696	718	739	761	
9.45		783	805	827	849	872	894	916	938	960	983	
9.46	0.11	005	028	050	073	095	118	140	163	186	208	
9.47		231	254	277	300	323	345	368	392	415	438	
9.48		461	484	507	531	554	577	601	624	648	671	
9.49		695	719	742	766	790	814	837	861	885	909	
9.50		933	957	981	*005	*030	*054	*078	*102	*127	*151	
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

ADD. {  $\log b - \log a = A$ .  
           {  $\log(a + b) = \log a + B$ .

SUB. {  $\log a - \log b = B$ .  
           {  $\log(a - b) = \log b + A$ .

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
9.50	0.11	933	957	981	*005	*030	*054	*078	*102	*127	*151	27 28 29 30
9.51	0.12	175	200	224	249	274	298	323	348	372	397	1 2.7 2.8 2.9 3.0
9.52	422	447	472	497	522	547	572	597	622	648	2 5.4 5.6 5.8 6.0	
9.53	673	698	724	749	775	800	826	851	877	903	3 8.1 8.4 8.7 9.3	
9.54	928	954	980	*006	*032	*058	*084	*110	*136	*162	4 10.8 11.2 11.6 12.0	
9.55	0.13	188	214	240	267	293	319	346	372	399	425	5 13.5 14.0 14.5 15.0
9.56	452	479	505	532	559	586	613	640	667	694	6 16.2 16.8 17.4 18.0	
9.57	721	748	775	802	829	857	884	911	939	966	7 18.9 19.6 20.3 21.0	
9.58	994	*021	*049	*077	*104	*132	*160	*188	*216	*244	8 21.6 22.4 23.2 24.0	
9.59	0.14	272	300	328	356	384	412	441	469	497	526	9 24.3 25.2 26.1 27.0
9.60	554	583	611	640	668	697	726	755	783	812	1 31 32 33 34	
9.61	841	870	899	928	957	986	*016	*045	*074	*104	2 6.2 6.4 6.6 6.8	
9.62	0.15	133	162	192	221	251	281	310	340	370	400	3 9.3 9.6 9.9 10.2
9.63	430	460	489	520	550	580	610	640	670	701	4 12.4 12.8 13.2 13.6	
9.64	731	761	792	822	853	884	914	945	976	*007	5 15.5 16.0 16.5 17.0	
9.65	0.16	037	068	099	130	161	192	224	255	286	317	6 18.6 19.2 19.8 20.4
9.66	349	380	411	443	474	506	538	569	601	633	7 21.7 22.4 23.1 23.8	
9.67	665	697	729	761	793	825	857	889	921	954	8 24.8 25.6 26.4 27.2	
9.68	986	*018	*051	*083	*116	*148	*181	*214	*247	*279	9 27.9 28.8 29.7 30.6	
9.69	0.17	312	345	378	411	444	477	510	544	577	610	1 35 36 37 38
9.70	643	677	710	744	777	811	845	878	912	946	2 7.0 7.2 7.4 7.6	
9.71	980	*014	*048	*082	*116	*150	*184	*218	*253	*287	3 10.5 10.8 11.1 11.4	
9.72	0.18	322	356	390	425	460	494	529	564	599	633	4 14.0 14.4 14.8 15.2
9.73	668	703	738	773	808	844	879	914	949	985	5 17.5 18.0 18.5 19.0	
9.74	0.19	020	056	091	127	163	198	234	270	306	342	6 21.0 21.6 22.2 22.8
9.75	378	414	450	486	522	558	595	631	667	704	7 24.5 25.2 25.9 26.6	
9.76	740	777	813	850	887	923	960	997	*034	*071	8 28.0 28.8 29.6 30.4	
9.77	0.20	108	145	182	220	257	294	331	369	406	444	9 31.5 32.4 33.3 34.2
9.78	481	519	557	594	632	670	708	746	784	822	1 3.9 4.0 4.1 4.2	
9.79	860	898	937	975	*013	*052	*090	*128	*167	*206	2 7.8 8.0 8.2 8.4	
9.80	0.21	244	283	322	361	399	438	477	516	556	595	3 11.7 12.0 12.3 12.6
9.81	634	673	712	752	791	831	870	910	949	989	4 15.5 16.0 16.4 16.8	
9.82	0.22	029	069	109	149	189	229	269	309	349	389	5 19.5 20.0 20.5 21.0
9.83	430	470	510	551	591	632	673	713	754	795	6 23.4 24.0 24.6 25.2	
9.84	836	877	918	959	*000	*041	*082	*123	*165	*206	7 27.3 28.0 28.7 29.4	
9.85	0.23	247	289	330	372	414	455	497	539	581	623	8 31.2 32.0 32.8 33.6
9.86	665	707	749	791	833	875	918	960	*003	*045	9 35.1 36.0 36.9 37.8	
9.87	0.24	088	130	173	216	258	301	344	387	430	473	1 4.3 4.4 4.5 4.6
9.88	516	559	603	646	689	733	776	819	863	907	2 8.6 8.8 9.0 9.2	
9.89	950	994	*038	*082	*126	*170	*214	*258	*302	*346	3 12.9 13.2 13.5 13.8	
9.90	0.25	390	434	479	523	568	612	657	701	746	791	4 17.2 17.6 18.0 18.4
9.91	836	881	926	970	*016	*061	*106	*151	*196	*242	5 21.5 22.0 22.5 23.0	
9.92	0.26	287	332	378	423	469	515	560	606	652	698	6 25.8 26.4 27.0 27.6
9.93	744	790	836	882	928	974	*021	*067	*114	*160	7 30.1 30.8 31.5 32.2	
9.94	0.27	207	253	300	346	393	440	487	534	581	628	8 34.4 35.2 36.0 36.8
9.95	675	722	769	817	864	911	959	*006	*054	*101	9 38.7 39.6 40.5 41.4	
9.96	0.28	149	197	245	292	340	388	436	484	532	581	1 4.7 4.8 4.9 5.0
9.97	629	677	726	774	822	871	920	968	*017	*066	2 9.4 9.6 9.8 10.0	
9.98	0.29	115	163	212	261	310	359	409	458	507	556	3 14.1 14.4 14.7 15.0
9.99	606	655	705	754	804	854	903	953	*003	*053	4 18.8 19.2 19.6 20.0	
0.00	0.30	103	153	203	253	303	354	404	454	505	555	5 28.2 28.8 29.4 30.0
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE V.

**ADD.**  $\left\{ \begin{array}{l} \log a - \log b = A. \\ \log(a+b) = \log b + B. \end{array} \right.$

**SUB.**  $\left\{ \begin{array}{l} \log a - \log b = B. \\ \log(a-b) = \log b + A. \end{array} \right.$

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
0.00	0.30	103	153	203	253	303	354	404	454	505	555	50 51 52 53
0.01	606	656	707	758	809	859	910	961	*012	*063	1 5.0 5.1 5.2 5.3	
0.02	0.31	115	166	217	268	320	371	422	474	526	577	2 10.0 10.2 10.4 10.6
0.03	629	681	732	784	836	888	940	992	*045	*097	3 15.0 15.3 15.6 15.9	
0.04	0.32	149	201	254	306	359	411	464	517	569	622	4 20.0 20.4 20.8 21.2
0.05	675	728	781	834	887	940	993	*046	*100	*153	5 25.0 25.5 26.0 26.5	
0.06	0.33	207	260	314	367	421	474	528	582	636	690	6 30.0 30.6 31.2 31.8
0.07	744	798	852	906	960	*015	*069	*123	*178	*232	7 35.0 35.7 36.4 37.1	
0.08	0.34	287	342	396	451	506	561	616	670	726	781	8 40.0 40.8 41.6 42.4
0.09	836	891	946	*001	*057	*112	*168	*223	*279	*334	9 45.0 45.9 46.8 47.7	
0.10	0.35	390	446	502	558	614	670	726	782	838	894	1 5.4 5.5 5.6 5.7
0.11	950	*007	*063	*119	*176	*233	*289	*346	*403	*459	2 10.8 11.0 11.2 11.4	
0.12	0.36	516	573	630	687	744	801	858	916	973	*030	3 16.2 16.5 16.8 17.1
0.13	0.37	088	145	203	260	318	375	433	491	549	607	4 21.0 22.0 22.4 22.8
0.14	665	723	781	839	897	955	*014	*072	*130	*189	6 32.4 33.0 33.6 34.2	
0.15	0.38	247	306	365	423	482	541	600	659	718	777	7 37.8 38.5 39.2 39.9
0.16	836	895	954	*013	*073	*132	*191	*251	*310	*370	8 43.2 44.0 44.8 45.6	
0.17	0.39	430	489	549	609	669	729	789	849	909	969	9 48.6 49.5 50.4 51.3
0.18	0.40	029	089	149	210	270	331	391	452	512	573	1 5.8 5.9 6.0 6.1
0.19	634	695	756	816	877	938	999	*061	*122	*183	2 21.6 22.8 23.0 23.2	
0.20	0.41	244	306	367	428	490	552	613	675	737	798	3 17.4 17.7 18.0 18.3
0.21	860	922	984	*046	*108	*170	*232	*294	*357	*419	4 23.2 23.6 24.0 24.4	
0.22	0.42	481	544	606	669	731	794	857	920	982	*045	5 29.0 29.5 30.0 30.5
0.23	0.43	108	171	234	297	360	423	487	550	613	677	6 34.8 35.4 36.0 36.6
0.24	740	804	867	931	995	*058	*122	*186	*250	*314	7 40.6 41.3 42.0 42.7	
0.25	0.44	378	442	506	570	634	698	763	827	891	956	8 46.4 47.2 48.0 48.8
0.26	0.45	020	085	149	214	279	344	408	473	538	603	9 52.2 53.1 54.0 54.9
0.27	668	733	799	864	929	994	*060	*125	*190	*256	1 6.2 6.3 6.4 6.5	
0.28	0.46	322	387	453	518	584	650	716	782	848	914	2 12.4 12.6 12.8 13.0
0.29	980	*046	*112	*178	*245	*311	*377	*444	*510	*577	3 18.6 18.9 19.2 19.5	
0.30	0.47	643	710	777	844	910	977	*044	*111	*178	*245	4 24.8 25.2 25.6 26.0
0.31	0.48	312	379	447	514	581	648	716	783	851	918	5 31.0 31.5 32.0 32.5
0.32	986	*054	*121	*189	*257	*325	*393	*461	*529	*597	6 37.2 37.8 38.4 39.0	
0.33	0.49	665	733	801	869	938	*006	*074	*143	*211	*280	7 43.4 44.1 44.8 45.5
0.34	0.50	349	417	486	555	624	692	761	830	899	968	8 49.6 50.4 51.2 52.0
0.35	0.51	037	107	176	245	314	384	453	522	592	661	9 55.8 56.7 57.6 58.5
0.36	731	801	870	940	*010	*080	*150	*220	*289	*360	1 19.8 20.1 20.4 20.7	
0.37	0.52	430	500	570	640	710	781	851	921	992	*062	2 26.4 26.8 27.2 27.6
0.38	0.53	133	204	274	345	416	486	557	628	699	770	3 33.0 33.5 34.0 34.5
0.39	841	912	983	*055	*126	*197	*268	*340	*411	*483	4 39.6 40.2 40.8 41.4	
0.40	0.54	554	626	697	769	841	912	984	*056	*128	*200	5 46.2 46.9 47.6 48.3
0.41	0.55	272	344	416	488	560	632	704	777	849	921	6 52.8 53.6 54.4 55.2
0.42	994	*066	*139	*211	*284	*357	*429	*502	*575	*648	7 59.4 60.0 61.2 62.1	
0.43	0.56	721	794	867	940	*013	*086	*159	*232	*305	*379	1 7.0 7.1 7.2 7.3
0.44	0.57	452	525	599	672	746	819	893	967	*040	*114	2 14.0 14.2 14.4 14.6
0.45	0.58	188	262	336	410	484	558	632	706	780	854	3 21.0 21.3 21.6 21.9
0.46	928	*003	*077	*151	*226	*300	*375	*449	*524	*598	4 28.0 28.4 28.8 29.2	
0.47	0.59	673	748	822	897	972	*047	*122	*197	*272	*347	5 35.0 35.5 36.0 36.5
0.48	0.60	422	497	572	648	723	798	874	949	*024	*100	6 42.0 42.6 43.2 43.8
0.49	0.61	175	251	327	402	478	554	630	705	781	857	7 49.0 49.7 50.4 51.1
0.50	933	*009	*085	*161	*237	*314	*390	*466	*542	*619	8 56.0 56.8 57.6 58.4	
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

## ADDITION AND SUBTRACTION LOGARITHMS.

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$$\text{ADD. } \begin{cases} \log a - \log b = A. \\ \log(a+b) = \log b + B. \end{cases}$$

$$\text{SUB. } \begin{cases} \log a - \log b = B. \\ \log(a-b) = \log b + A. \end{cases}$$

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.	
0.50	0.61	933	*009	*085	*161	*237	*314	*390	*466	*542	*619	74 75 76	
0.51	0.62	695	771	848	924	*001	*077	*154	*231	*307	*384	7.4 7.5 7.6	
0.52	0.63	461	538	615	692	768	845	923	*000	*077	*154	2 14.8 15.0 15.2	
0.53	0.64	231	308	386	463	540	618	695	773	850	928	3 22.2 22.5 22.8	
0.54	0.65	005	083	160	238	316	394	472	549	627	705	4 29.6 30.0 30.4	
0.55		783	861	939	*018	*096	*174	*252	*330	*409	*487	5 37.0 37.5 38.0	
0.56	0.66	565	644	722	801	879	958	*037	*115	*194	*273	6 44.4 45.0 45.6	
0.57	0.67	351	430	509	588	667	746	825	904	983	*062	7 51.8 52.5 53.2	
0.58	0.68	141	220	300	379	458	538	617	696	776	855	8 59.2 60.0 60.8	
0.59		935	*014	*094	*174	*253	*333	*413	*493	*573	*652	9 66.6 67.5 68.4	
0.60	0.69	732	812	892	972	*052	*132	*212	*293	*373	*453	77 78 79	
0.61	0.70	533	614	694	774	855	935	*016	*096	*177	*257	1 7.7 7.8 7.9	
0.62	0.71	338	419	499	580	661	742	823	904	984	*065	2 15.4 15.6 15.8	
0.63	0.72	146	227	308	390	471	552	633	714	796	877	3 23.1 23.4 23.7	
0.64		958	*040	*121	*202	*284	*365	*447	*529	*610	*692	4 30.8 31.2 31.6	
0.65	0.73	774	855	937	*019	*101	*183	*264	*346	*428	*510	5 38.5 39.0 39.5	
0.66	0.74	592	674	757	839	921	*003	*085	*168	*250	*332	6 46.2 46.8 47.4	
0.67	0.75	415	497	579	662	744	827	909	992	*075	*157	7 53.9 54.6 55.3	
0.68	0.76	240	323	406	488	571	654	737	820	903	986	8 61.6 62.4 63.2	
0.69	0.77	069	152	235	318	401	485	568	651	734	818	9 69.3 70.2 71.1	
0.70		901	984	*068	*151	*235	*318	*402	*485	*569	*653	80 81 82	
0.71	0.78	736	820	904	987	*071	*155	*239	*323	*407	*491	1 8.0 8.1 8.2	
0.72	0.79	575	659	743	827	911	995	*079	*163	*248	*332	2 16.0 16.2 16.4	
0.73	0.80	416	500	585	669	754	838	922	*007	*091	*176	3 24.0 24.3 24.6	
0.74	0.81	261	345	430	515	599	684	769	854	938	*023	4 32.0 32.4 32.8	
0.75	0.82	108	193	278	363	448	533	618	703	788	873	5 40.0 40.5 41.0	
0.76		959	*044	*129	*214	*300	*385	*470	*556	*641	*727	6 48.0 48.6 49.2	
0.77	0.83	812	898	983	*069	*154	*240	*325	*411	*497	*583	7 56.0 56.7 57.4	
0.78	0.84	668	754	840	926	*012	*097	*183	*269	*355	*441	8 64.0 64.8 65.6	
0.79	0.85	527	613	700	786	872	958	*044	*130	*217	*303	9 72.0 72.9 73.8	
0.80	0.86	389	476	562	648	735	821	908	994	*081	*167	83 84 85	
0.81	0.87	254	340	427	514	600	687	774	861	947	*034	1 8.3 8.4 8.5	
0.82	0.88	121	208	295	382	469	556	643	730	817	904	2 16.6 16.8 17.0	
0.83		991	*078	*165	*252	*339	*427	*514	*601	*689	*776	3 24.9 25.2 25.5	
0.84	0.89	863	951	*038	*125	*213	*300	*388	*475	*563	*651	4 33.2 33.6 34.0	
0.85	0.90	738	826	914	*001	*089	*177	*264	*352	*440	*528	5 41.5 42.0 42.5	
0.86	0.91	616	704	791	879	967	*055	*143	*231	*319	*408	6 49.8 50.4 51.0	
0.87	0.92	496	584	672	760	848	936	*025	*113	*201	*290	7 58.1 58.8 59.5	
0.88	0.93	378	466	555	643	732	820	908	997	*086	*174	8 66.4 67.2 68.0	
0.89	0.94	263	351	440	529	617	706	795	883	972	*061	9 74.7 75.6 76.5	
0.90	0.95	150	239	327	416	505	594	683	772	861	950	86 87 88	
0.91	0.96	039	128	217	306	395	485	574	663	752	841	1 8.6 8.7 8.8	
0.92		931	*020	*109	*198	*288	*377	*467	*556	*645	*735	2 17.2 17.4 17.6	
0.93	0.97	824	914	*003	*093	*182	*272	*362	*451	*541	*631	3 25.8 26.1 26.4	
0.94	0.98	720	810	900	980	*079	*169	*259	*349	*439	*528	4 34.4 34.8 35.2	
0.95	0.99	618	708	798	888	978	*068	*158	*248	*338	*428	5 43.0 43.5 44.0	
0.96	1.00	519	609	699	789	879	969	*060	*150	*240	*330	6 51.6 52.2 52.8	
0.97	1.01	421	511	601	692	782	873	963	*053	*144	*234	7 60.2 60.9 61.6	
0.98	1.02	325	415	506	597	687	778	868	959	*050	*140	8 68.8 69.6 70.4	
0.99	1.03	231	322	413	503	594	685	776	867	957	*048	9 77.4 78.3 79.2	
1.00		1.04	139	230	321	412	503	594	685	776	867	958	A. B. Prop. Pts.

TABLE VI.

ADD.  $\left\{ \begin{array}{l} \log a - \log b = A. \\ \log(a+b) = \log b + B. \end{array} \right.$

SUB.  $\left\{ \begin{array}{l} \log a - \log b = B. \\ \log(a-b) = \log b + A. \end{array} \right.$

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
1.00	1.04	139	230	321	412	503	594	685	776	867	958	
1.01	1.05	049	140	232	323	414	505	596	687	779	870	
1.02		961	*053	*144	*235	*326	*418	*509	*601	*692	*783	
1.03	1.06	875	966	*058	*149	*241	*332	*424	*516	*607	*699	
1.04	1.07	790	882	974	*065	*157	*249	*341	*432	*524	*616	
1.05	1.08	708	800	891	983	*075	*167	*259	*351	*443	*535	
1.06	1.09	627	719	811	903	995	*087	*179	*271	*363	*455	
1.07	1.10	548	640	732	824	916	*009	*101	*193	*285	*378	
1.08	1.11	470	562	655	747	839	932	*024	*117	*209	*301	
1.09	1.12	394	486	579	671	764	857	949	*042	*134	*227	
1.10	1.13	320	412	505	598	690	783	876	968	*061	*154	
1.11	1.14	247	340	432	525	618	711	804	897	990	*083	
1.12	1.15	175	268	361	454	547	640	733	826	920	*013	
1.13	1.16	106	199	292	385	478	571	665	758	851	944	
1.14	1.17	037	131	224	317	411	504	597	691	784	877	
1.15		971	*064	*157	*251	*344	*438	*531	*625	*718	*812	
1.16	1.18	905	999	*092	*186	*279	*373	*467	*560	*654	*748	
1.17	1.19	841	935	*020	*122	*216	*310	*403	*497	*591	*685	
1.18	1.20	779	872	966	*060	*154	*248	*342	*435	*529	*623	
1.19	1.21	717	811	905	999	*093	*187	*281	*375	*469	*563	
1.20	1.22	657	751	845	939	*034	*128	*222	*316	*410	*504	
1.21	1.23	599	693	787	881	975	*070	*164	*258	*352	*447	
1.22	1.24	541	635	730	824	918	*013	*107	*202	*296	*390	
1.23	1.25	485	579	674	768	863	957	*052	*146	*241	*335	
1.24	1.26	430	524	619	714	808	903	997	*092	*187	*281	
1.25	1.27	376	471	565	660	755	850	944	*039	*134	*229	
1.26	1.28	323	418	513	608	703	797	892	987	*082	*177	
1.27	1.29	272	367	462	557	652	746	841	936	*031	*126	
1.28	1.30	221	316	411	507	602	697	792	887	982	*077	
1.29	1.31	172	267	362	458	553	648	743	838	933	*029	
1.30	1.32	124	219	314	410	505	600	695	791	886	981	
1.31	1.33	077	172	267	363	458	553	649	744	840	935	
1.32	1.34	030	126	221	317	412	508	603	699	794	890	
1.33		985	*081	*176	*272	*367	*463	*559	*654	*750	*845	
1.34	1.35	941	*037	*132	*228	*324	*419	*515	*611	*706	*802	
1.35	1.36	898	994	*089	*185	*281	*377	*472	*568	*664	*760	
1.36	1.37	856	951	*047	*143	*239	*335	*431	*527	*622	*718	
1.37	1.38	814	910	*006	*102	*198	*294	*390	*486	*582	*678	
1.38	1.39	774	870	966	*062	*158	*254	*350	*446	*542	*638	
1.39	1.40	734	830	926	*032	*119	*215	*311	*407	*503	*599	
1.40	1.41	695	792	888	984	*080	*176	*273	*369	*465	*561	
1.41	1.42	658	754	850	946	*043	*139	*235	*332	*428	*524	
1.42	1.43	621	717	813	910	*006	*102	*199	*295	*391	*488	
1.43	1.44	584	681	777	874	970	*066	*163	*259	*356	*452	
1.44	1.45	549	645	742	838	935	*031	*128	*225	*321	*418	
1.45	1.46	514	611	707	804	901	997	*094	*190	*287	*384	
1.46	1.47	480	577	674	770	867	964	*060	*157	*254	*350	
1.47	1.48	447	544	641	737	834	931	*028	*124	*221	*318	
1.48	1.49	415	512	608	705	802	899	996	*093	*189	*286	
1.49	1.50	383	480	577	674	771	868	964	*061	*158	*255	
1.50	1.51	352	449	546	643	740	837	934	*031	*128	*225	
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

95 96

97

91 92  
2 18.2 18.4  
3 27.3 27.6  
4 36.4 36.8  
5 45.5 46.0  
6 54.6 55.2  
7 63.7 64.4  
8 72.8 73.6  
9 81.9 82.893  
1 9.3  
2 18.6  
3 27.9  
4 37.2  
5 46.5  
6 55.8  
7 65.1  
8 74.4  
9 83.794  
1 9.4  
2 18.8  
3 28.2  
4 37.6  
5 47.0  
6 56.4  
7 65.8  
8 75.2  
9 84.695 96  
2 19.0 19.2  
3 28.5 28.8  
4 38.0 38.4  
5 47.5 48.0  
6 57.0 57.6  
7 66.5 67.2  
8 76.0 76.8  
9 85.5 86.497  
1 9.7  
2 19.4  
3 29.1  
4 38.8  
5 48.5  
6 58.2  
7 67.9  
8 77.6  
9 87.3

ADD.  $\begin{cases} \log a - \log b = A. \\ \log(a+b) = \log b + B. \end{cases}$

SUB.  $\begin{cases} \log a - \log b = B. \\ \log(a-b) = \log b + A. \end{cases}$

A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.
1.50	1.51	352	449	546	643	740	837	934	*031	*128	*225	
1.51	1.52	322	419	516	613	710	807	904	*001	*008	*195	
1.52	1.53	292	389	486	583	680	778	875	972	*069	*166	
1.53	1.54	263	360	457	555	652	749	846	943	*040	*138	
1.54	1.55	235	332	429	526	624	721	818	915	*013	*110	
1.55	1.56	207	304	402	499	596	693	791	888	*085	*083	
1.56	1.57	180	277	375	472	569	667	764	861	959	*056	
1.57	1.58	153	251	348	446	543	640	738	835	933	*030	1   97
1.58	1.59	128	225	322	420	517	615	712	810	907	*005	2   9.7
1.59	1.60	102	200	297	395	492	590	687	785	882	980	3   19.4
1.60	1.61	077	175	273	370	468	565	663	760	858	956	4   29.1
1.61	1.62	053	151	248	346	444	541	639	737	834	932	5   38.8
1.62	1.63	030	127	225	322	420	518	616	713	811	909	6   58.2
1.63	1.64	006	104	202	299	397	495	593	690	788	886	7   67.9
1.64	984	*081	*179	*277	*375	*473	*570	*668	*766	*864		8   77.6
1.65	1.65	962	*059	*157	*255	*353	*451	*548	*646	*744	*842	9   87.3
1.66	1.66	940	*038	*136	*233	*331	*429	*527	*625	*723	*821	
1.67	1.67	919	*017	*115	*212	*310	*408	*506	*604	*702	*800	
1.68	1.68	898	996	*094	*192	*290	*388	*486	*584	*682	*780	
1.69	1.69	878	976	*074	*172	*270	*368	*466	*564	*662	*760	
1.70	1.70	858	956	*054	*152	*250	*348	*446	*544	*642	*741	
1.71	1.71	839	937	*035	*133	*231	*329	*427	*525	*623	*722	1   98
1.72	1.72	820	918	*016	*114	*212	*310	*409	*507	*605	*703	2   9.8
1.73	1.73	801	899	998	*096	*194	*292	*390	*489	*587	*685	3   19.6
1.74	1.74	783	881	980	*078	*176	*274	*373	*471	*569	*667	4   29.4
1.75	1.75	766	864	962	*060	*159	*257	*355	*453	*552	*650	5   39.2
1.76	1.76	748	847	945	*043	*141	*240	*338	*436	*535	*633	6   49.0
1.77	1.77	731	830	928	*026	*125	*223	*321	*420	*518	*616	7   58.8
1.78	1.78	715	813	912	*010	*108	*207	*305	*403	*502	*600	8   68.6
1.79	1.79	699	797	896	994	*092	*191	*289	*388	*486	*584	9   78.4
1.80	1.80	683	781	880	978	*077	*175	*274	*372	*471	*569	
1.81	1.81	667	766	864	963	*061	*160	*258	*357	*455	*554	
1.82	1.82	652	751	849	948	*046	*145	*244	*342	*441	*539	
1.83	1.83	638	736	835	933	*032	*130	*229	*328	*426	*525	
1.84	1.84	623	722	820	919	*018	*116	*215	*313	*412	*511	
1.85	1.85	609	708	806	905	*004	*102	*201	*299	*398	*497	
1.86	1.86	595	694	793	891	990	*089	*187	*286	*385	*483	
1.87	1.87	582	681	779	878	977	*075	*174	*273	*371	*470	1   99
1.88	1.88	569	667	766	865	964	*062	*161	*260	*358	*457	2   19.8
1.89	1.89	556	655	753	852	951	*050	*148	*247	*346	*445	3   29.7
1.90	1.90	543	642	741	840	938	*037	*136	*235	*333	*432	4   39.6
1.91	1.91	531	630	729	827	926	*025	*124	*223	*321	*420	5   49.5
1.92	1.92	519	618	717	815	914	*013	*112	*211	*310	*408	6   59.4
1.93	1.93	507	606	705	804	903	*002	*100	*199	*298	*397	7   69.3
1.94	1.94	496	595	694	792	891	990	*089	*188	*287	*386	8   79.2
1.95	1.95	485	583	682	781	880	979	*078	*177	*276	*375	9   89.1
1.96	1.96	474	573	671	770	869	968	*067	*166	*265	*364	
1.97	1.97	463	562	661	760	859	958	*057	*156	*254	*353	
1.98	1.98	452	551	650	749	848	947	*046	*145	*244	*343	
1.99	1.99	442	541	640	739	838	937	*036	*135	*234	*333	
2.00	2.00	432	531	630	729	828	927	*026	*125	*224	*323	
A.	B.	0	1	2	3	4	5	6	7	8	9	Prop. Pts.

TABLE VI.

$\log a - \log b = A.$

$\log a - \log b = B.$

$\log(a + b) = \log a + (B - A).$

$\log(a - b) = \log a - (B - A).$

A.	B.	B-A.	A.	B.	B-A.	A.	B.	B-A.
I. 9823	I. 9868	.00450	2.0337	2.0377	.00400	2.0920	2.0955	.00350
.9833	.9878	449	.0348	.0388	399	.0932	.0967	349
.9842	.9887	448	.0359	.0399	398	.0945	.0980	348
.9852	.9897	447	.0370	.0410	397	.0957	.0992	347
.9862	.9907	446	.0381	.0421	396	.0970	.1005	346
I. 9872	I. 9917	.00445	2.0392	2.0432	.00395	2.0982	2.1017	.00345
.9882	.9926	444	.0403	.0443	394	.0995	.1029	344
.9891	.9935	443	.0414	.0454	393	.1008	.1042	343
.9901	.9945	442	.0425	.0465	392	.1020	.1054	342
.9911	.9955	441	.0437	.0476	391	.1033	.1067	341
I. 9921	I. 9965	.00440	2.0448	2.0487	.00390	2.1046	2.1080	.00340
.9931	.9975	439	.0459	.0498	389	.1059	.1093	339
.9941	.9985	438	.0470	.0509	388	.1072	.1106	338
.9951	.9995	437	.0481	.0520	387	.1085	.1119	337
.9961	2.0005	436	.0493	.0532	386	.1098	.1132	336
I. 9971	2.0015	.00435	2.0504	2.0543	.00385	2.1111	2.1144	.00335
.9981	.0024	434	.0515	.0553	384	.1124	.1157	334
.9991	.0034	433	.0527	.0565	383	.1137	.1170	333
2.0001	.0044	432	.0538	.0576	382	.1150	.1183	332
.0011	.0054	431	.0550	.0588	381	.1163	.1196	331
2.0021	2.0065	.00430	2.0561	2.0600	.00380	2.1176	2.1209	.00330
.0032	.0075	429	.0573	.0611	379	.1190	.1223	329
.0042	.0085	428	.0584	.0622	378	.1203	.1236	328
.0052	.0095	427	.0596	.0634	377	.1216	.1249	327
.0062	.0105	426	.0607	.0645	376	.1229	.1262	326
2.0073	2.0115	.00425	2.0619	2.0656	.00375	2.1243	2.1275	.00325
.0083	.0125	424	.0630	.0667	374	.1256	.1288	324
.0093	.0135	423	.0642	.0679	373	.1270	.1302	323
.0104	.0146	422	.0654	.0691	372	.1283	.1315	322
.0114	.0156	421	.0666	.0703	371	.1297	.1329	321
2.0124	2.0166	.00420	2.0677	2.0714	.00370	2.1310	2.1342	.00320
.0135	.0177	419	.0689	.0726	369	.1324	.1356	319
.0145	.0187	418	.0701	.0738	368	.1338	.1370	318
.0156	.0198	417	.0713	.0750	367	.1351	.1383	317
.0166	.0208	416	.0725	.0762	366	.1365	.1397	316
2.0177	2.0218	.00415	2.0737	2.0773	.00365	2.1379	2.1410	.00315
.0187	.0228	414	.0749	.0785	364	.1393	.1424	314
.0198	.0239	413	.0761	.0797	363	.1407	.1438	313
.0208	.0249	412	.0773	.0809	362	.1421	.1452	312
.0219	.0260	411	.0785	.0821	361	.1435	.1466	311
2.0229	2.0270	.00410	2.0797	2.0833	.00360	2.1449	2.1480	.00310
.0240	.0281	409	.0809	.0845	359	.1463	.1494	309
.0251	.0292	408	.0821	.0857	358	.1477	.1508	308
.0261	.0302	407	.0833	.0869	357	.1491	.1522	307
.0272	.0313	406	.0845	.0881	356	.1505	.1536	306
2.0283	2.0324	.00405	2.0858	2.0893	.00355	2.1520	2.1550	.00305
.0294	.0334	404	.0870	.0905	354	.1534	.1564	304
.0305	.0345	403	.0882	.0917	353	.1548	.1578	303
.0315	.0355	402	.0895	.0930	352	.1563	.1593	302
.0326	.0366	401	.0907	.0942	351	.1577	.1607	301
2.0337	2.0337	.00400	2.0920	2.0955	.00350	2.1592	2.1622	.00300
A.	B.	B-A.	A.	B.	B-A.	A.	B.	B-A.

$\log a - \log b = A.$

$\log a - \log b = B.$

$\log(a + b) = \log a + (B - A).$

$\log(a - b) = \log a - (B - A).$

A.	B.	B-A.	A.	B.	B-A.	A.	B.	B-A.
2.1592	2.1622	.00300	2.2386	2.2411	.00250	2.3358	2.3378	.00200
.1606	.1636	299	.2403	.2428	249	.3379	.3399	199
.1621	.1651	298	.2421	.2446	248	.3401	.3421	198
.1635	.1665	297	.2439	.2464	247	.3423	.3443	197
.1650	.1680	296	.2456	.2481	246	.3446	.3466	196
2.1665	2.1694	.00295	2.2474	2.2498	.00245	2.3468	2.3487	.00195
.1680	.1709	294	.2492	.2516	244	.3490	.3509	194
.1694	.1723	293	.2510	.2534	243	.3513	.3532	193
.1710	.1739	292	.2528	.2552	242	.3535	.3554	192
.1724	.1753	291	.2546	.2570	241	.3558	.3577	191
2.1739	2.1768	.00290	2.2564	2.2588	.00240	2.3581	2.3600	.00190
.1754	.1783	289	.2582	.2606	239	.3604	.3623	189
.1770	.1799	288	.2600	.2624	238	.3627	.3646	188
.1785	.1814	287	.2618	.2642	237	.3650	.3669	187
.1800	.1829	286	.2637	.2661	236	.3673	.3692	186
2.1815	2.1844	.00285	2.2656	2.2679	.00235	2.3697	2.3715	.00185
.1830	.1858	284	.2674	.2697	234	.3720	.3738	184
.1846	.1874	283	.2693	.2716	233	.3744	.3762	183
.1861	.1889	282	.2711	.2734	232	.3768	.3786	182
.1877	.1905	281	.2730	.2753	231	.3792	.3810	181
2.1892	2.1920	.00280	2.2749	2.2772	.00230	2.3816	2.3834	.00180
.1908	.1936	279	.2768	.2791	229	.3840	.3858	179
.1923	.1951	278	.2787	.2810	228	.3865	.3883	178
.1939	.1967	277	.2806	.2829	227	.3889	.3907	177
.1955	.1983	276	.2825	.2848	226	.3914	.3932	176
2.1971	2.1998	.00275	2.2845	2.2867	.00225	2.3939	2.3956	.00175
.1987	.2014	274	.2864	.2886	224	.3964	.3981	174
.2002	.2029	273	.2884	.2906	223	.3989	.4006	173
.2019	.2046	272	.2903	.2925	222	.4014	.4031	172
.2035	.2062	271	.2923	.2945	221	.4039	.4056	171
2.2051	2.2078	.00270	2.2943	2.2965	.00220	2.4065	2.4082	.00170
.2067	.2094	269	.2962	.2984	219	.4090	.4107	169
.2083	.2110	268	.2982	.3004	218	.4116	.4133	168
.2099	.2126	267	.3002	.3024	217	.4142	.4159	167
.2116	.2143	266	.3022	.3044	216	.4168	.4185	166
2.2132	2.2159	.00265	2.3043	2.3064	.00215	2.4195	2.4211	.00165
.2149	.2175	264	.3063	.3084	214	.4221	.4237	164
.2165	.2191	263	.3083	.3104	213	.4248	.4264	163
.2182	.2208	262	.3104	.3125	212	.4275	.4291	162
.2198	.2224	261	.3124	.3145	211	.4302	.4318	161
2.2215	2.2241	.00260	2.3145	2.3166	.00210	2.4329	2.4345	.00160
.2232	.2258	259	.3166	.3187	209	.4356	.4372	159
.2249	.2275	258	.3187	.3208	208	.4383	.4399	158
.2266	.2292	257	.3208	.3229	207	.4411	.4427	157
.2283	.2309	256	.3229	.3250	206	.4439	.4455	156
2.2300	2.2325	.00255	2.3250	2.3271	.00205	2.4467	2.4482	.00155
.2317	.2342	254	.3271	.3291	204	.4495	.4510	154
.2334	.2359	253	.3293	.3313	203	.4523	.4538	153
.2351	.2376	252	.3314	.3334	202	.4552	.4567	152
.2369	.2394	251	.3336	.3356	201	.4581	.4596	151
2.2386	2.2411	.00250	2.3358	2.3378	.00200	2.4609	2.4624	.00150
A.	B.	B-A.	A.	B.	B-A.	A.	B.	B-A.

TABLE VI.

$\log a - \log b = A.$

$\log a - \log b = B.$

$\log(a + b) = \log a + (B - A).$

$\log(a - b) = \log a - (B - A).$

A.	B.	B-A.	A.	B.	B-A.	A.	B.	B-A.
2.4609	2.4624	.00150	2.6373	2.6383	.000100	2.9385	2.9390	.00050
.4638	.4653	149	.6416	.6426	.00099	.9474	.9479	49
.4668	.4683	148	.6401	.6471	98	.9563	.9568	48
.4697	.4712	147	.6505	.6515	97	.9655	.9660	47
.4727	.4742	146	.6550	.6560	96	.9748	.9753	46
2.4757	2.4772	.00145	2.6596	2.6606	.00095	2.9844	2.9848	.00045
.4787	.4801	144	.6642	.6651	94	2.9941	2.9945	44
.4817	.4831	143	.6688	.6697	93	3.0041	3.0045	43
.4848	.4862	142	.6735	.6744	92	.0143	.0147	42
.4878	.4892	141	.6783	.6792	91	.0248	.0252	41
2.4910	2.4924	.00140	2.6831	2.6840	.00090	3.0356	3.0360	.00040
.4941	.4955	139	.6880	.6889	89	.0466	.0470	39
.4972	.4986	138	.6928	.6937	88	.0578	.0582	38
.5004	.5018	137	.6978	.6987	87	.0694	.0698	37
.5036	.5050	136	.7028	.7037	86	.0813	.0817	36
2.5068	2.5081	.00135	2.7079	2.7088	.00085	3.0935	3.0939	.00035
.5100	.5113	134	.7131	.7139	84	.1061	.1064	34
.5133	.5146	133	.7183	.7191	83	.1191	.1194	33
.5165	.5178	132	.7236	.7244	82	.1324	.1327	32
.5199	.5212	131	.7289	.7297	81	.1463	.1466	31
2.5232	2.5245	.00130	2.7343	2.7351	.00080	3.1606	3.1609	.00030
.5266	.5279	129	.7398	.7406	79	.1753	.1756	29
.5299	.5312	128	.7453	.7461	78	.1905	.1908	28
.5333	.5346	127	.7509	.7517	77	.2063	.2066	27
.5368	.5381	126	.7566	.7574	76	.2226	.2229	26
2.5402	2.5415	.00125	2.7623	2.7631	.00075	3.2396	3.2399	.00025
.5437	.5449	124	.7682	.7689	74	.2575	.2577	24
.5472	.5484	123	.7741	.7748	73	.2760	.2762	23
.5508	.5520	122	.7801	.7808	72	.2952	.2954	22
.5544	.5556	121	.7862	.7869	71	.3154	.3156	21
2.5580	2.5592	.00120	2.7923	2.7930	.00070	3.3366	3.3368	.00020
.5616	.5628	119	.7985	.7992	69	.3590	.3592	19
.5653	.5665	118	.8050	.8057	68	.3825	.3827	18
.5690	.5702	117	.8114	.8121	67	.4072	.4074	17
.5727	.5739	116	.8180	.8187	66	.4335	.4337	16
2.5765	2.5776	.00115	2.8245	2.8252	.00065	3.4617	3.4619	.00015
.5803	.5814	114	.8313	.8319	64	.4917	.4918	14
.5841	.5852	113	.8381	.8387	63	.5237	.5238	13
.5880	.5891	112	.8451	.8457	62	.5587	.5588	12
.5919	.5930	111	.8521	.8527	61	.5964	.5965	11
2.5958	2.5969	.00110	2.8593	2.8599	.00060	3.6377	3.6378	.00010
.5998	.6009	109	.8666	.8672	59	.6835	.6836	09
.6038	.6049	108	.8741	.8747	58	.7345	.7346	08
.6079	.6090	107	.8816	.8822	57	.7925	.7926	07
.6120	.6131	106	.8893	.8899	56	.8595	.8596	06
2.6161	2.6172	.00105	2.8971	2.8977	.00055	3.9390	3.9391	.00005
.6202	.6212	104	.9051	.9056	54	4.0355	4.0355	04
.6244	.6254	103	.9132	.9137	53	4.1600	4.1600	03
.6287	.6297	102	.9215	.9220	52	4.3375	4.3375	02
.6329	.6339	101	.9300	.9305	51	4.6367	4.6367	01
2.6373	2.6383	.00100	2.9385	2.9390	.00050	∞	∞	.00000
A.	B.	B-A.	A.	B.	B-A.	A.	B.	B-A.

## TABLE VII.



## SQUARES OF NUMBERS.

No.	Square.								
0	0	20	400	40	1600	60	3600	80	6400
1	1	21	441	41	1681	61	3721	81	6561
2	4	22	484	42	1764	62	3844	82	6724
3	9	23	529	43	1849	63	3969	83	6889
4	16	24	576	44	1936	64	4096	84	7056
5	25	25	625	45	2025	65	4225	85	7225
6	36	26	676	46	2116	66	4356	86	7396
7	49	27	729	47	2209	67	4489	87	7569
8	64	28	784	48	2304	68	4624	88	7744
9	81	29	841	49	2401	69	4761	89	7921
10	100	30	900	50	2500	70	4900	90	8100
11	121	31	961	51	2601	71	5041	91	8281
12	144	32	1024	52	2704	72	5184	92	8464
13	169	33	1089	53	2809	73	5329	93	8649
14	196	34	1156	54	2916	74	5476	94	8836
15	225	35	1225	55	3025	75	5625	95	9025
16	256	36	1296	56	3136	76	5776	96	9216
17	289	37	1369	57	3249	77	5929	97	9409
18	324	38	1444	58	3364	78	6084	98	9604
19	361	39	1521	59	3481	79	6241	99	9801
20	400	40	1600	60	3600	80	6400	100	10000

	1◆◆	2◆◆	3◆◆	4◆◆	5◆◆	6◆◆	7◆◆	8◆◆	9◆◆		Diff.
00	100	400	900	1600	2500	3600	4900	6400	8100	00	1
01	102	404	906	1608	2510	3612	4914	6416	8118	01	3
02	104	408	912	1616	2520	3624	4928	6432	8136	04	5
03	106	412	918	1624	2530	3636	4942	6448	8154	09	7
04	108	416	924	1632	2540	3648	4956	6464	8172	16	9
05	110	420	930	1640	2550	3660	4970	6480	8190	25	11
06	112	424	936	1648	2560	3672	4984	6496	8208	36	13
07	114	428	942	1656	2570	3684	4998	6512	8226	49	15
08	116	432	948	1664	2580	3696	5012	6528	8244	64	17
09	118	436	954	1672	2590	3708	5026	6544	8262	81	19*
10	121	441	961	1681	2601	3721	5041	6561	8281	00	21
11	123	445	967	1689	2611	3733	5055	6577	8299	21	23
12	125	449	973	1697	2621	3745	5069	6593	8317	44	25
13	127	453	979	1705	2631	3757	5083	6609	8335	69	27
14	129	457	985	1713	2641	3769	5097	6625	8353	96	29*
15	132	462	992	1722	2652	3782	5112	6642	8372	25	31
16	134	466	998	1730	2662	3794	5126	6658	8390	56	33
17	136	470	1004	1738	2672	3806	5140	6674	8408	89	35*
18	139	475	1011	1747	2683	3819	5155	6691	8427	24	37
19	141	479	1017	1755	2693	3831	5169	6707	8445	61	39*
20	144	484	1024	1764	2704	3844	5184	6724	8464	00	41
21	146	488	1030	1772	2714	3856	5198	6740	8482	41	43
22	148	492	1036	1780	2724	3868	5212	6756	8500	84	45*
23	151	497	1043	1789	2735	3881	5227	6773	8519	29	47
24	153	501	1049	1797	2745	3893	5241	6789	8537	76	49*
25	156	506	1056	1806	2756	3906	5256	6806	8556	25	51
26	158	510	1062	1814	2766	3918	5270	6822	8574	76	53*
27	161	515	1069	1823	2777	3931	5285	6839	8593	29	55
28	163	519	1075	1831	2787	3943	5299	6855	8611	84	57*
29	166	524	1082	1840	2798	3956	5314	6872	8630	41	59*
30	169	529	1089	1849	2809	3969	5329	6889	8649	00	61
31	171	533	1095	1857	2819	3981	5343	6905	8667	61	63*
32	174	538	1102	1866	2830	3994	5358	6922	8686	24	65
33	176	542	1108	1874	2840	4006	5372	6938	8704	89	67*
34	179	547	1115	1883	2851	4019	5387	6955	8723	56	69*
35	182	552	1122	1892	2862	4032	5402	6972	8742	25	71
36	184	556	1128	1900	2872	4044	5416	6988	8760	96	73*
37	187	561	1135	1909	2883	4057	5431	7005	8779	69	75*
38	190	566	1142	1918	2894	4070	5446	7022	8798	44	77*
39	193	571	1149	1927	2905	4083	5461	7039	8817	21	79*
40	196	576	1156	1936	2916	4096	5476	7056	8836	00	81
41	198	580	1162	1944	2926	4108	5490	7072	8854	81	83*
42	201	585	1169	1953	2937	4121	5505	7089	8873	64	85*
43	204	590	1176	1962	2948	4134	5520	7106	8892	49	87*
44	207	595	1183	1971	2959	4147	5535	7123	8911	36	89*
45	210	600	1190	1980	2970	4160	5550	7140	8930	25	91*
46	213	605	1197	1989	2981	4173	5565	7157	8949	16	93*
47	216	610	1204	1998	2992	4186	5580	7174	8968	09	95*
48	219	615	1211	2007	3003	4199	5595	7191	8987	04	97*
49	222	620	1218	2016	3014	4212	5610	7208	9006	01	99*
50	225	625	1225	2025	3025	4225	5625	7225	9025	00	

	1◆◆	2◆◆	3◆◆	4◆◆	5◆◆	6◆◆	7◆◆	8◆◆	9◆◆		Diff.
50	225	625	1225	2025	3025	4225	5625	7225	9025	00	1
51	228	630	1232	2034	3036	4238	5640	7242	9044	01	3
52	231	635	1239	2043	3047	4251	5655	7259	9063	04	5
53	234	640	1246	2052	3058	4264	5670	7276	9082	09	7
54	237	645	1253	2061	3069	4277	5685	7293	9101	16	9
55	240	650	1260	2070	3080	4290	5700	7310	9120	25	11
56	243	655	1267	2079	3091	4303	5715	7327	9139	36	13
57	246	660	1274	2088	3102	4316	5730	7344	9158	49	15
58	249	665	1281	2097	3113	4329	5745	7361	9177	64	17
59	252	670	1288	2106	3124	4342	5760	7378	9196	81	19*
60	256	676	1296	2116	3136	4356	5776	7396	9216	00	21
61	259	681	1303	2125	3147	4369	5791	7413	9235	21	23
62	262	686	1310	2134	3158	4382	5806	7430	9254	44	25
63	265	691	1317	2143	3169	4395	5821	7447	9273	69	27
64	268	696	1324	2152	3180	4408	5836	7464	9292	96	29*
65	272	702	1332	2162	3192	4422	5852	7482	9312	25	31
66	275	707	1339	2171	3203	4435	5867	7499	9331	56	33
67	278	712	1346	2180	3214	4448	5882	7516	9350	89	35*
68	282	718	1354	2190	3226	4462	5898	7534	9370	24	37
69	285	723	1361	2199	3237	4475	5913	7551	9389	61	39*
70	289	729	1369	2209	3249	4489	5929	7569	9409	00	41
71	292	734	1376	2218	3260	4502	5944	7586	9428	41	43
72	295	739	1383	2227	3271	4515	5959	7603	9447	84	45*
73	299	745	1391	2237	3283	4529	5975	7621	9467	29	47
74	302	750	1398	2246	3294	4542	5990	7638	9486	76	49*
75	306	756	1406	2256	3306	4556	6006	7656	9506	25	51*
76	309	761	1413	2265	3317	4569	6021	7673	9525	76	53*
77	313	767	1421	2275	3329	4583	6037	7691	9545	29	55
78	316	772	1428	2284	3340	4596	6052	7708	9564	84	57*
79	320	778	1436	2294	3352	4610	6068	7726	9584	41	59*
80	324	784	1444	2304	3364	4624	6084	7744	9604	00	61
81	327	789	1451	2313	3375	4637	6099	7761	9623	61	63*
82	331	795	1459	2323	3387	4651	6115	7779	9643	24	65
83	334	800	1466	2332	3398	4664	6130	7796	9662	89	67*
84	338	806	1474	2342	3410	4678	6146	7814	9682	56	69*
85	342	812	1482	2352	3422	4692	6162	7832	9702	25	71*
86	345	817	1489	2361	3433	4705	6177	7849	9721	96	73*
87	349	823	1497	2371	3445	4719	6193	7867	9741	69	75*
88	353	829	1505	2381	3457	4733	6209	7885	9761	44	77*
89	357	835	1513	2391	3469	4747	6225	7903	9781	21	79*
90	361	841	1521	2401	3481	4761	6241	7921	9801	00	81
91	364	846	1528	2410	3492	4774	6256	7938	9820	81	83*
92	368	852	1536	2420	3504	4788	6272	7956	9840	64	85*
93	372	858	1544	2430	3516	4802	6288	7974	9860	49	87*
94	376	864	1552	2440	3528	4816	6304	7992	9880	36	89*
95	380	870	1560	2450	3540	4830	6320	8010	9900	25	91*
96	384	876	1568	2460	3552	4844	6336	8028	9920	16	93*
97	388	882	1576	2470	3564	4858	6352	8046	9940	09	95*
98	392	888	1584	2480	3576	4872	6368	8064	9960	64	97*
99	396	894	1592	2490	3588	4886	6384	8082	9980	01	99*
100	400	900	1600	2500	3600	4900	6400	8100	10000	00	



TABLE VIII.—DECIMALS OF DAY INTO HOURS, ETC.

101

D.	H. M. S.	H. M. S. 100	H.M.S. 100 <sup>2</sup>	D.	H. M. S.	H. M. S. 100	H.M.S. 100 <sup>2</sup>
d.	h. m. s.	m. s.	s.	d.	h. m. s.	m. s.	s.
0.01	0 14 24	0 8.64	0.09	0.51	12 14 24	7 20.64	4.41
0.02	0 28 48	0 17.28	0.17	0.52	12 28 48	7 29.28	4.49
0.03	0 43 12	0 25.92	0.26	0.53	12 43 12	7 37.92	4.58
0.04	0 57 36	0 34.56	0.35	0.54	12 57 36	7 46.56	4.67
0.05	1 12 0	0 43.20	0.43	0.55	13 12 0	7 55.20	4.75
0.06	1 26 24	0 51.84	0.52	0.56	13 26 24	8 3.84	4.84
0.07	1 40 48	1 0.48	0.60	0.57	13 40 48	8 12.48	4.92
0.08	1 55 12	1 9.12	0.69	0.58	13 55 12	8 21.12	5.01
0.09	2 9 36	1 17.76	0.78	0.59	14 9 36	8 29.76	5.10
0.10	2 24 0	1 26.40	0.86	0.60	14 24 0	8 38.40	5.18
0.11	2 38 24	1 35.04	0.95	0.61	14 38 24	8 47.04	5.27
0.12	2 52 48	1 43.68	1.04	0.62	14 52 48	8 55.68	5.36
0.13	3 7 12	1 52.32	1.12	0.63	15 7 12	9 4.32	5.44
0.14	3 21 36	2 0.96	1.21	0.64	15 21 36	9 12.96	5.53
0.15	3 36 0	2 9.60	1.30	0.65	15 36 0	9 21.60	5.62
0.16	3 50 24	2 18.24	1.38	0.66	15 50 24	9 30.24	5.70
0.17	4 4 48	2 26.88	1.47	0.67	16 4 48	9 38.88	5.79
0.18	4 19 12	2 35.52	1.56	0.68	16 19 12	9 47.52	5.88
0.19	4 33 36	2 44.16	1.64	0.69	16 33 36	9 56.16	5.96
0.20	4 48 0	2 52.80	1.73	0.70	16 48 0	10 4.80	6.05
0.21	5 2 24	3 1.44	1.81	0.71	17 2 24	10 13.44	6.13
0.22	5 16 48	3 10.08	1.90	0.72	17 16 48	10 22.08	6.22
0.23	5 31 12	3 18.72	1.99	0.73	17 31 12	10 30.72	6.31
0.24	5 45 36	3 27.36	2.07	0.74	17 45 36	10 39.36	6.39
0.25	6 0 0	3 36.00	2.16	0.75	18 0 0	10 48.00	6.48
0.26	6 14 24	3 44.64	2.25	0.76	18 14 24	10 56.64	6.57
0.27	6 28 48	3 53.28	2.33	0.77	18 28 48	11 5.28	6.65
0.28	6 43 12	4 1.92	2.42	0.78	18 43 12	11 13.92	6.74
0.29	6 57 36	4 10.56	2.51	0.79	18 57 36	11 22.56	6.83
0.30	7 12 0	4 19.20	2.59	0.80	19 12 0	11 31.20	6.91
0.31	7 26 24	4 27.84	2.68	0.81	19 26 24	11 39.84	7.00
0.32	7 40 48	4 36.48	2.76	0.82	19 40 48	11 48.48	7.08
0.33	7 55 12	4 45.12	2.85	0.83	19 55 12	11 57.12	7.17
0.34	8 9 36	4 53.76	2.94	0.84	20 9 36	12 5.76	7.26
0.35	8 24 0	5 2.40	3.02	0.85	20 24 0	12 14.40	7.34
0.36	8 38 24	5 11.04	3.11	0.86	20 38 24	12 23.04	7.43
0.37	8 52 48	5 19.68	3.20	0.87	20 52 48	12 31.68	7.52
0.38	9 7 12	5 28.32	3.28	0.88	21 7 12	12 40.32	7.60
0.39	9 21 36	5 36.96	3.37	0.89	21 21 36	12 48.96	7.69
0.40	9 36 0	5 45.60	3.46	0.90	21 36 0	12 57.60	7.78
0.41	9 50 24	5 54.24	3.54	0.91	21 50 24	13 6.24	7.86
0.42	10 4 48	6 2.88	3.63	0.92	22 4 48	13 14.88	7.95
0.43	10 19 12	6 11.52	3.72	0.93	22 19 12	13 23.52	8.04
0.44	10 33 36	6 20.16	3.80	0.94	22 33 36	13 32.16	8.12
0.45	10 48 0	6 28.80	3.89	0.95	22 48 0	13 40.80	8.21
0.46	11 2 24	6 37.44	3.97	0.96	23 2 24	13 49.44	8.29
0.47	11 16 48	6 46.08	4.06	0.97	23 16 48	13 58.08	8.38
0.48	11 31 12	6 54.72	4.15	0.98	23 31 12	14 6.72	8.47
0.49	11 45 36	7 3.36	4.23	0.99	23 45 36	14 15.36	8.55
0.50	12 0 0	7 12.00	4.32	1.00	24 0 0	14 24.00	8.64

TABLE IX.—ARC INTO TIME AND VICE VERSA.

v	h. m.	o	h. m.	o	h. m.	o	h. m.	o	h. m.	o	h. m.	i	m. s.	u	s.
0 0 0	60 4 q	20	8 0	180	12 0	240	16 0	300	20 0	0 0	0 0	0	0	0	0.000
1 0 4	61 4 4	121	8 4	181	12 4	241	16 4	301	20 4	1 0	0 4	1	0	0.066	
2 0 8	62 4 8	122	8 8	182	12 8	242	16 8	302	20 8	2 0	0 8	2	0	0.133	
3 0 12	63 4 12	123	8 12	183	12 12	243	16 12	303	20 12	3 0	0 12	3	0	0.200	
4 0 16	64 4 16	124	8 16	184	12 16	244	16 16	304	20 16	4 0	0 16	4	0	0.266	
5 0 20	65 4 20	125	8 20	185	12 20	245	16 20	305	20 20	5 0	0 20	5	0	0.333	
6 0 24	66 4 24	126	8 24	186	12 24	246	16 24	306	20 24	6 0	0 24	6	0	0.400	
7 0 28	67 4 28	127	8 28	187	12 28	247	16 28	307	20 28	7 0	0 28	7	0	0.466	
8 0 32	68 4 32	128	8 32	188	12 32	248	16 32	308	20 32	8 0	0 32	8	0	0.533	
9 0 36	69 4 36	129	8 36	189	12 36	249	16 36	309	20 36	9 0	0 36	9	0	0.600	
10 0 40	70 4 40	130	8 40	190	12 40	250	16 40	310	20 40	10 0	0 40	10	0	0.666	
11 0 44	71 4 44	131	8 44	191	12 44	251	16 44	311	20 44	11 0	0 44	11	0	0.733	
12 0 48	72 4 48	132	8 48	192	12 48	252	16 48	312	20 48	12 0	0 48	12	0	0.800	
13 0 52	73 4 52	133	8 52	193	12 52	253	16 52	313	20 52	13 0	0 52	13	0	0.866	
14 0 56	74 4 56	134	8 56	194	12 56	254	16 56	314	20 56	14 0	0 56	14	0	0.933	
15 1 0	75 5 0	135	9 0	195	13 0	255	17 0	315	21 0	15 0	1 0	15	1	1.000	
16 1 4	76 5 4	136	9 4	196	13 4	256	17 4	316	21 4	16 0	1 4	16	1	1.066	
17 1 8	77 5 8	137	9 8	197	13 8	257	17 8	317	21 8	17 0	1 8	17	1	1.133	
18 1 12	78 5 12	138	9 12	198	13 12	258	17 12	318	21 12	18 0	1 12	18	1	1.200	
19 1 16	79 5 16	139	9 16	199	13 16	259	17 16	319	21 16	19 0	1 16	19	1	1.266	
20 1 20	80 5 20	140	9 20	200	13 20	260	17 20	320	21 20	20 0	1 20	20	1	1.333	
21 1 24	81 5 24	141	9 24	201	13 24	261	17 24	321	21 24	21 0	1 24	21	1	1.400	
22 1 28	82 5 28	142	9 28	202	13 28	262	17 28	322	21 28	22 0	1 28	22	1	1.466	
23 1 32	83 5 32	143	9 32	203	13 32	263	17 32	323	21 32	23 0	1 32	23	1	1.533	
24 1 36	84 5 36	144	9 36	204	13 36	264	17 36	324	21 36	24 0	1 36	24	1	1.600	
25 1 40	85 5 40	145	9 40	205	13 40	265	17 40	325	21 40	25 0	1 40	25	1	1.666	
26 1 44	86 5 44	146	9 44	206	13 44	266	17 44	326	21 44	26 0	1 44	26	1	1.733	
27 1 48	87 5 48	147	9 48	207	13 48	267	17 48	327	21 48	27 0	1 48	27	1	1.800	
28 1 52	88 5 52	148	9 52	208	13 52	268	17 52	328	21 52	28 0	1 52	28	1	1.866	
29 1 56	89 5 56	149	9 56	209	13 56	269	17 56	329	21 56	29 0	1 56	29	1	1.933	
30 2 0	90 6 0	150	10 0	210	14 0	270	18 0	330	22 0	30 0	2 0	30	2	2.000	
31 2 4	91 6 4	151	10 4	211	14 4	271	18 4	331	22 4	31 0	2 4	31	2	2.066	
32 2 8	92 6 8	152	10 8	212	14 8	272	18 8	332	22 8	32 0	2 8	32	2	2.133	
33 2 12	93 6 12	153	10 12	213	14 12	273	18 12	333	22 12	33 0	2 12	33	2	2.200	
34 2 16	94 6 16	154	10 16	214	14 16	274	18 16	334	22 16	34 0	2 16	34	2	2.266	
35 2 20	95 6 20	155	10 20	215	14 20	275	18 20	335	22 20	35 0	2 20	35	2	2.333	
36 2 24	96 6 24	156	10 24	216	14 24	276	18 24	336	22 24	36 0	2 24	36	2	2.400	
37 2 28	97 6 28	157	10 28	217	14 28	277	18 28	337	22 28	37 0	2 28	37	2	2.466	
38 2 32	98 6 32	158	10 32	218	14 32	278	18 32	338	22 32	38 0	2 32	38	2	2.533	
39 2 36	99 6 36	159	10 36	219	14 36	279	18 36	339	22 36	39 0	2 36	39	2	2.600	
40 2 40	100 6 40	160	10 40	220	14 40	280	18 40	340	22 40	40 0	2 40	40	2	2.666	
41 2 44	101 6 44	161	10 44	221	14 44	281	18 44	341	22 44	41 0	2 44	41	2	2.733	
42 2 48	102 6 48	162	10 48	222	14 48	282	18 48	342	22 48	42 0	2 48	42	2	2.800	
43 2 52	103 6 52	163	10 52	223	14 52	283	18 52	343	22 52	43 0	2 52	43	2	2.866	
44 2 56	104 6 56	164	10 56	224	14 56	284	18 56	344	22 56	44 0	2 56	44	2	2.933	
45 3 0	105 7 0	165	11 0	225	15 0	285	19 0	345	23 0	45 0	3 0	45	3	3.000	
46 3 4	106 7 4	166	11 4	226	15 4	286	19 4	346	23 4	46 0	3 4	46	3	3.066	
47 3 8	107 7 8	167	11 8	227	15 8	287	19 8	347	23 8	47 0	3 8	47	3	3.133	
48 3 12	108 7 12	168	11 12	228	15 12	288	19 12	348	23 12	48 0	3 12	48	3	3.200	
49 3 16	109 7 16	169	11 16	229	15 16	289	19 16	349	23 16	49 0	3 16	49	3	3.266	
50 3 20	110 7 20	170	11 20	230	15 20	290	19 20	350	23 20	50 0	3 20	50	3	3.333	
51 3 24	111 7 24	171	11 24	231	15 24	291	19 24	351	23 24	51 0	3 24	51	3	3.400	
52 3 28	112 7 28	172	11 28	232	15 28	292	19 28	352	23 28	52 0	3 28	52	3	3.466	
53 3 32	113 7 32	173	11 32	233	15 32	293	19 32	353	23 32	53 0	3 32	53	3	3.533	
54 3 36	114 7 36	174	11 36	234	15 36	294	19 36	354	23 36	54 0	3 36	54	3	3.500	
55 3 40	115 7 40	175	11 40	235	15 40	295	19 40	355	23 40	55 0	3 40	55	3	3.666	
56 3 44	116 7 44	176	11 44	236	15 44	296	19 44	356	23 44	56 0	3 44	56	3	3.733	
57 3 48	117 7 48	177	11 48	237	15 48	297	19 48	357	23 48	57 0	3 48	57	3	3.800	
58 3 52	118 7 52	178	11 52	238	15 52	298	19 52	358	23 52	58 0	3 52	58	3	3.866	
59 3 56	119 7 56	179	11 56	239	15 56	299	19 56	359	23 56	59 0	3 56	59	3	3.933	

TABLE Xa.—TO CONVERT MEAN INTO SIDEREAL TIME.

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Mean T. h. m.	Correction. + m. s.	Mean T. h. m.	Correction. + m. s.	Mean T. h. m.	Correction. + m. s.	Corr. for min. and sec. m. s. s.
0 0	0 0.00	8 0	1 18.85	16 0	2 37.70	0 10 0.03
10	1.64	10	20.50	10	39.35	20 0.05
20	3.29	20	22.14	20	40.99	30 0.08
30	4.93	30	23.78	30	42.63	40 0.11
40	6.57	40	25.42	40	44.28	50 0.14
50	8.21	50	27.07	50	45.92	1 0 0.16
						10 0.19
I 0	0 9.86	9 0	1 28.71	17 0	2 47.56	20 0.22
10	11.50	10	30.35	10	49.20	30 0.25
20	13.14	20	31.99	20	50.85	40 0.27
30	14.78	30	33.64	30	52.49	50 0.30
40	16.43	40	35.28	40	54.13	2 0 0.33
50	18.07	50	36.92	50	55.77	10 0.36
						20 0.38
2 0	0 19.71	10 0	1 38.56	18 0	2 57.42	30 0.41
10	21.36	10	40.21	10	59.06	40 0.44
20	23.00	20	41.85	20	3 0.70	50 0.47
30	24.64	30	43.49	30	2.34	3 0 0.49
40	26.28	40	45.14	40	3.99	10 0.52
50	27.93	50	46.78	50	5.63	20 0.55
						30 0.57
3 0	0 29.57	11 0	1 48.42	19 0	3 7.27	40 0.60
10	31.21	10	50.06	10	8.92	50 0.63
20	32.86	20	51.71	20	10.56	3 0 0.66
30	34.50	30	53.35	30	12.20	10 0.68
40	36.14	40	54.99	40	13.84	20 0.71
50	37.78	50	56.64	50	15.49	30 0.74
						40 0.77
4 0	0 39.43	12 0	1 58.28	20 0	3 17.13	50 0.79
10	41.07	10	59.92	10	18.77	3 0 0.82
20	42.71	20	2 1.56	20	20.42	10 0.85
30	44.35	30	3.21	30	22.06	20 0.88
40	46.00	40	4.85	40	23.70	30 0.90
50	47.64	50	6.49	50	25.34	40 0.93
						50 0.96
5 0	0 49.28	13 0	2 8.13	21 0	3 26.99	6 0 0.99
10	50.92	10	9.78	10	28.63	10 1.01
20	52.57	20	11.42	20	30.27	20 1.04
30	54.21	30	13.06	30	31.91	30 1.07
40	55.85	40	14.70	40	33.56	40 1.10
50	57.50	50	16.35	50	35.20	50 1.12
						3 0 1.15
6 0	0 59.14	14 0	2 17.99	22 0	3 36.84	10 1.18
10	1 0.78	10	19.63	10	38.48	20 1.21
20	2.42	20	21.28	20	40.13	30 1.23
30	4.07	30	22.92	30	41.77	40 1.26
40	5.71	40	24.56	40	43.41	50 1.29
50	7.35	50	26.20	50	45.06	3 0 1.31
						10 1.34
7 0	1 9.00	15 0	2 27.85	23 0	3 46.70	10 1.37
10	10.64	10	29.49	10	48.34	20 1.40
20	12.28	20	31.13	20	49.98	30 1.42
30	13.92	30	32.77	30	51.63	40 1.45
40	15.57	40	34.42	40	53.27	50 1.48
50	17.21	50	36.06	50	54.91	10 1.50
						20 1.53
						30 1.56
						40 1.59
						50 1.62

TABLE Xb.—TO CONVERT SIDEREAL INTO MEAN TIME.

Sid. T. h. m.	Correction. m. s.	Sid. T. h. m.	Correction. m. s.	Sid. T. h. m.	Correction. m. s.	Corr. for min. and sec. m. s. s.
0 0 0	0.00	8 0 1	18.64	16 0 2	37.27	0 10 0.03
10	1.64	10	20.28	10	38.91	20 0.05
20	3.28	20	21.91	20	40.55	30 0.08
30	4.92	30	23.55	30	42.19	40 0.11
40	6.55	40	25.19	40	43.83	50 0.14
50	8.19	50	26.83	50	45.46	1 0 0.16
						10 0.19
1 0 0	9.83	9 0 1	28.47	17 0 2	47.10	20 0.22
10	11.47	10	30.10	10	48.74	30 0.25
20	13.11	20	31.74	20	50.38	40 0.27
30	14.74	30	33.38	30	52.02	50 0.30
40	16.38	40	35.02	40	53.66	2 0 0.33
50	18.02	50	36.66	50	55.29	10 0.35
						20 0.38
2 0 0	19.66	10 0 1	38.30	18 0 2	56.93	30 0.41
10	21.30	10	39.93	10	58.57	40 0.44
20	22.94	20	41.57	20	0.21	50 0.47
30	24.57	30	43.21	30	1.85	3 0 0.49
40	26.21	40	44.85	40	3.48	10 0.52
50	27.85	50	46.49	50	5.12	20 0.55
						30 0.57
						40 0.60
						50 0.63
3 0 0	29.49	11 0 1	48.12	19 0 3	6.76	4 0 0.66
10	31.13	10	49.76	10	8.40	10 0.68
20	32.76	20	51.40	20	10.04	20 0.71
30	34.40	30	53.04	30	11.68	30 0.74
40	36.04	40	54.68	40	13.32	40 0.76
50	37.68	50	56.32	50	14.95	50 0.79
						5 0 0.82
4 0 0	39.32	12 0 1	57.96	20 0 3	16.59	10 0.85
10	40.96	10	59.59	10	18.23	20 0.87
20	42.60	20	1.23	20	19.87	30 0.90
30	44.23	30	2.87	30	21.51	40 0.93
40	45.87	40	4.51	40	23.14	50 0.96
50	47.51	50	6.15	50	24.78	6 0 0.98
						10 1.01
						20 1.04
5 0 0	49.15	13 0 2	7.78	21 0 3	26.42	30 1.06
10	50.79	10	9.42	10	28.06	40 1.09
20	52.42	20	11.06	20	29.70	50 1.12
30	54.06	30	12.70	30	31.34	7 0 1.15
40	55.70	40	14.34	40	32.97	10 1.17
50	57.34	50	15.98	50	34.61	20 1.20
						30 1.23
6 0 0	58.98	14 0 2	17.61	22 0 3	36.25	40 1.20
10	1 0.62	10	19.25	10	37.89	50 1.28
20	2.25	20	20.89	20	39.53	8 0 1.31
30	3.89	30	22.53	30	41.16	10 1.34
40	5.53	40	24.17	40	42.80	20 1.37
50	7.17	50	25.80	50	44.44	30 1.39
						40 1.42
						50 1.45
7 0 1	8.81	15 0 2	27.44	23 0 3	46.08	9 0 1.47
10	10.44	10	29.08	10	47.72	10 1.50
20	12.08	20	30.72	20	49.36	20 1.53
30	13.72	30	32.36	30	51.00	30 1.56
40	15.36	40	34.00	40	52.63	40 1.58
50	17.00	50	35.64	50	54.27	50 1.61



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